

**Social Interactions, Mechanisms, and
Equilibrium: Evidence from a Model of
Study Time and Academic Achievement**

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Social interactions, mechanisms, and equilibrium:

Evidence from a model of study time and academic achievement

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Abstract

We develop and estimate a model of study time choices of students on a social network. The model is designed to exploit unique data collected in the Berea Panel Study. Study time data allow us to quantify an intuitive mechanism for academic social interactions: own study time may depend on friend study time. Social network data allow study time choices and resulting academic achievement to be embedded in an estimable equilibrium framework. New data on study propensities allow us to directly address potential sorting into friendships based on typically unobserved determinants of study time. We develop a specification test that exploits the equilibrium nature of social interactions and use it to show that our study propensity measures substantially address endogeneity concerns. We find friend study time strongly affects own study time, and, therefore, student achievement. We examine how network structure interacts with student characteristics to affect academic achievement. Sorting on friend characteristics appears important in explaining variation across students in study time and achievement, and determines the aggregate achievement level.

Keywords: social networks, peer effects, homophily, time-use

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1 Introduction

Peer effects are widely believed to be important for determining academic achievement. Much of the existing research in this context has focused on establishing a causal link between peer characteristics and academic outcomes, in an effort to provide evidence about whether peers matter. However, though crucial for policymaking, direct evidence on the mechanisms generating peer effects is limited. In this paper we exploit unique data on college students from the Berea Panel Study (BPS) to study peer effects in an academic setting. We focus on what is likely the most relevant set of peers in our higher education context, a student’s friends.

The goal of this paper is to better understand how peer effects are generated. One step is to provide direct evidence about a mechanism underlying peer influences in our context. This is in the spirit of Manski (2000), who stresses that, in order to understand relationships between own and peer outcomes, it is important to clearly define mechanisms and to obtain direct evidence about their relevance. Motivated by recent research hypothesizing that student effort is likely to be an input that is readily influenced by peers in the short run (Stinebrickner and Stinebrickner (2006), Calvó-Armengol et al. (2009), Cooley Fruehwirth (2013), and De Giorgi and Pellizzari (2014)), we focus on study time as an explicit mechanism through which peer effects could arise in college.¹

Another step is to better understand the role social networks play in the propagation of peer effects. Not only may student i ’s study time be influenced by i ’s peers, but i ’s peers’ study time may be influenced by i . Moreover, these types of feedback effects could work indirectly through students in the social network who are not directly connected to student i . We focus on how the distribution of feedback effects depends on three interrelated components. First, the graph describing links in a social network, which we refer to as the “network structure”, may be important in and of itself (Calvó-Armengol et al. (2009), Jackson and Yariv (2011)). Second, students with different characteristics may differ in how much they are affected by their peers (Sacerdote (2011)). Third, students may form links based on these characteristics. In particular, students may link to others with similar characteristics, i.e., the network may exhibit “homophily.” Together, the network structure and the specific manner in which heterogeneous students are arranged on the network may determine how changes in behavior propagate throughout the network and affect equilibrium outcomes.

To take these important next steps, we estimate an equilibrium model of study time

¹For a non-education (financial) example of research that is interested in understanding why peer effects exist, see Bursztyn et al. (2014). Richards-Shubik (2014) separates supply and demand mechanisms in a model of sexual initiation.

choice and resulting grade determination, given a social network. Estimating such a model entails substantial data challenges. First, we need student-level data on study time. Unfortunately, because collecting reliable time-use information is very difficult in annual surveys, available data sources typically do not contain this type of information. Second, equilibrium outcomes depend on the entire social network, necessitating data characterizing the full set of peer connections as well as data on characteristics that likely determine study time choices. Among existing sources of social network data, perhaps only one, the National Longitudinal Survey of Adolescent Health (Add-Health), could potentially provide a full view of a social network in an educational setting where academic outcomes and student characteristics are also observed. Unfortunately, because the Add-Health dataset has a primary focus on adolescent health and risk-related behaviors, it does not contain information about time spent studying. Thus, to the best of our knowledge, there is no other data source that is able to both fully characterize a social network of students and provide direct evidence about a central input in the grade production function that has been hypothesized to generate social interactions.

Our project is made possible by unique data from the Berea Panel Study (BPS), which were collected specifically to overcome these current data limitations. The BPS surveyed full cohorts of students at Berea College, which allows us to characterize the entire social network. The BPS is also unique in its high frequency of contact with students each year, allowing the collection of eight time-use diaries, which allow us to characterize study time, and the measurement of friendships in each semester, which we use to define peers. We combine these survey data with administrative data that include pre-college characteristics and college grades.

We develop our model to exploit these unique data. The social network is known at the beginning of a period. Subsequently, all students in the social network simultaneously choose their study time to maximize their own achievement, net of studying costs. A student's studying cost depends on her own study time and friend study time, e.g., it may be more fun to study if your friends are studying (alternatively, students may conform to their friends). Cost functions are allowed to be heterogeneous across students. Achievement depends on a student's own study time and may also be heterogeneous across students, conditional on own study time.

The social interactions literature has paid close attention to the endogeneity problem that is present if there exist correlated unobserved variables, that is, unobserved information related to both peer group membership (in our context, friendship choices) and outcomes of interest (Manski (1993), Moffitt (2001), Epple and Romano (2011)). In our case, where we focus on a social interaction in study time choices, a relationship between friends' study

times could arise because friends influence each other (peer effects) or because students with similar unobserved determinants of study time become friends (correlated unobserved variables). Institutional details, together with empirical checks we conduct, suggest that correlated shocks arising through, e.g., coursework and dormitories, are not the most salient type of correlated unobserved variables. The most relevant type of correlated unobserved variable would seem to be an unobserved individual characteristic, which could be thought of as a student's propensity to study.

We adopt a two-step approach for dealing with this endogeneity problem. First, we take advantage of a unique opportunity to directly measure students' propensities to study. Specifically, the day before freshman classes began, we collected information about how much a student actually studied in high school and how much the student expected to study in college. We find that both high school study time and expected college study time have strong correlations with study time in college and are also strongly related to friendship patterns in our data.

One cannot know *a priori* whether our study propensity data address the above endogeneity concern in a satisfactory manner, meaning we need some way to assess how well our data have measured typical correlated unobserved variables. Given the importance of this assessment, our second step is to develop a specification test based on our model. Our specification test is designed to detect unobserved determinants of study time, exploiting the fact that the equilibrium nature of social interactions implies that such unobserved determinants would generate cross-sectional dependence in residuals. Crucially, our test is useful even when unobserved determinants lead to inconsistently estimated parameters.

We estimate the model using data from two semesters. Under the baseline specification, in which we use our study propensity data to estimate the model, we find no evidence of the cross-sectional residual correlation described above. However, we do find significant cross-sectional residual correlations when we re-estimate the model excluding our study propensity data, i.e., using only measures of student characteristics that are typically available to researchers. This suggests that our specification test has the power to detect unobserved determinants of study time. Therefore, these findings provide evidence that our study propensity measures play an important role in addressing endogeneity concerns.

Our estimates provide strong evidence that friend study time has a substantial effect on one's own study time. We also find that one's own study time is an important determinant of one's own achievement. We estimate students to have different best response functions, i.e., they react differently to changes in friend study time. Hereafter, we will often refer to this as heterogeneity in *reactiveness*. This heterogeneity potentially has equilibrium implications, as it implies complementarities in students' choice of study time. We estimate that two

students with 75th percentile reactivity, when paired with each other, would study almost twice as much as would two students with 25th percentile reactivity, when paired with each other.

The extent to which heterogeneity in reactivity affects total production depends on the relationship between own and friend reactivity. Therefore, it is also important to take into account the social network to understand social interactions.² We use our estimated model to perform two counterfactual exercises. First, we examine how the network structure, combined with homophilous sorting into friendships, affects the response to changes in friend study time. We exogenously increase (shock) the study time of each student and assess how study times and achievement change for other students in the social network. There is substantial heterogeneity in study time responses depending on which student is shocked, with larger impacts associated with more central students and students connected to more reactive peers. The specific manner in which students with different characteristics are arranged on the network is important for responses. This exercise also provides a natural framework for quantifying the importance of equilibrium interactions. On average, equilibrium responses produce a network-wide aggregate response that is 2.7 times larger than their partial equilibrium counterparts, which only consider a shock's effect on immediate neighbors.

Our framework allows us to provide further evidence about the importance of homophily in determining outcomes. As Golub and Jackson (2012) note, despite a large amount of work documenting the existence of homophily and a smaller literature examining its origins, the literature modeling the effect of homophily is in its infancy.³ In our second counterfactual, we examine how achievement would differ if friend characteristics were identically distributed across students, instead of being strongly correlated with one's own characteristics, or homophilous, as in the data. On average, women, blacks, and students with above-median high school GPAs have high propensities to study and tend, in the data, to sort into friendships with students similar to themselves. Therefore, these groups tend to see declines in their friends' propensities to study in the counterfactual. Due to the estimated heterogeneity in best response functions and the lack of assortative matching in the counterfactual networks, these groups' losses are not offset by gains of their complements.

The remainder of this paper is organized as follows. Section 2 discusses related literature.

²Kline and Tamer (2011) discuss the importance of distinguishing between estimates of technological parameters and the equilibrium effects of social interactions.

³Jackson (2008) provides a discussion of work documenting the existence of homophily; see Camargo et al. (2010) for a specific example. For theoretical models of homophily's origins see Currarini et al. (2009), Currarini et al. (2010), and Bramoullé et al. (2012). Badev (2013) allows for homophily in his empirical study of friendship formation and smoking behavior.

Section 3 contains a description of the BPS data. Section 4 presents our model. Section 5 presents our empirical specification. Section 6 develops our specification test and Section 7 discusses estimation results. Section 8 presents the results from our counterfactual exercises and Section 9 concludes.

2 Related Literature

Academic Peer Effects and Social Interactions Models There is an extensive literature on academic peer effects, which has been recently surveyed by Epple and Romano (2011) and Sacerdote (2011). As discussed in Sacerdote (2011), papers in this literature typically do not directly examine mechanisms through which peer effects are generated. Cooley Fruehwirth (2013), Calvó-Armengol et al. (2009), De Giorgi and Pellizzari (2014), and Tincani (2016) all stress the importance of equilibrium models of students' effort choices, but lack direct data on student effort. Cooley Fruehwirth (2013) and Calvó-Armengol et al. (2009) estimate parameters of their respective models, identifying effort through residual variation in peer outcomes. De Giorgi and Pellizzari (2014) and Tincani (2016) test the implications of different theoretical models of social interactions using student achievement data.

In terms of goals, perhaps the paper closest to ours is Calvó-Armengol et al. (2009). As in that paper, we develop a model that takes the social network as given to understand how effort choices, made on the social network, affect academic achievement. Calvó-Armengol et al. (2009), lacking direct input data, consider an environment in which a socially determined input choice is linked to network topology. This provides a behavioral foundation to the Katz-Bonacich centrality measure. Our contribution is the direct measurement of an input that likely affects achievement (study effort) and variables that likely are related to sorting into friendships and the choice of this input (study propensity measures, like high school study time and expected study time). These data are crucial for thoroughly investigating the mechanism considered in this paper. They allow us to examine how the input of interest (study effort) influences the output of interest (achievement). They also allow us to quantify how the input of interest is influenced by peers. Our theoretical model differs from that in Calvó-Armengol et al. (2009) in potentially important ways that are testable. We allow for heterogeneous best response functions, which our data on input choices allow us to identify. We also allow for nonlinearity in best response functions, which would break the connection between network topology and equilibrium outcomes required in Calvó-Armengol et al. (2009).

Our approach complements that of Calvó-Armengol et al. (2009) by allowing for a richer understanding of social interactions. In our framework, someone concerned about a student's

low effort level may have an incentive to get the student to have more studious friends. Because we allow inputs to depend on student characteristics, there may be winners and losers from changes in peer group composition. Moreover, potentially heterogeneous reactivity would allow total achievement to change, depending on the type of sorting in the baseline. Such questions could not be assessed using the framework of Calvó-Armengol et al. (2009), where counterfactuals are limited to changes in link structure.

There is a growing literature studying peer effects that has focused on modeling the formation of social networks, an important and notoriously difficult problem (see Christakis et al. (2010), Mele (2013), Badev (2013), de Paula et al. (2016), Sheng (2014), and Hsieh and Lee (2016)). We cannot study how the network would change in response to a policy because we do not model how friendships are formed. Therefore, in our counterfactuals, we examine fully-specified networks of interest, such as those in the data and randomly generated networks, in which student and friend characteristics are independent.

Specification Test The specification test we develop is informative about the presence of unobserved determinants of study time of the sort discussed in the introduction, even when parameter estimates are biased. Our specification test exploits the fact that, in equilibrium, all unobserved determinants of study time will typically enter all students' outcome equations. This type of error structure has precedent in a social interactions context (see, e.g., Calvó-Armengol et al. (2009) and Blume et al. (2015)).⁴ Our contribution is that we develop a specification test designed to detect unobserved variables of interest and show how it can have the power to do so, even in the presence of inconsistently estimated parameters.

Goldsmith-Pinkham and Imbens (2013) posit a model of network formation and, within this model, derive a testable implication of endogenous network formation (see Boucher and Fortin (2016) for further discussion). In contrast, we do not test for a specific model of network formation. Rather, the goal of our specification test is to detect unobserved determinants of study time that we believe to be relevant to our context, taking as given the network. Therefore, we view our work as complementary to that of Goldsmith-Pinkham and Imbens (2013).

3 Data

The BPS is a longitudinal survey that was designed by Todd Stinebrickner and Ralph Stinebrickner to provide detailed information about educational outcomes in college and labor

⁴There is a related literature on spatial autoregressive models; see Pinkse et al. (2002) and Lee (2004), for example.

market outcomes in the early post-college period. The BPS survey design involved collecting information about all students who entered Berea College in the fall of 2000 and the fall of 2001. Baseline surveys were conducted immediately before the start of first year classes and students were subsequently surveyed 10-12 times each year during school. As has been discussed in previous work that uses the BPS, caution is appropriate when considering exactly how results from the BPS would generalize to other specific institutions (e.g., Stinebrickner and Stinebrickner (2006, 2013)). At the same time, from an academic standpoint, Berea has much in common with many four-year colleges. It operates under a standard liberal arts curriculum and the students at Berea, which is in central Kentucky, are similar in academic quality to, for example, students at the University of Kentucky (Stinebrickner and Stinebrickner (2008b)).

Our study is made possible by three types of information that are available in the BPS. First, the BPS elicited each student’s closest friends. Our analysis utilizes friendship observations from the end of the first semester and the end of the second semester. The survey question for the end of the first semester is shown in Appendix A.1. The survey question for the end of the second semester is identical (except for the date). Our friendship survey questions have a full-semester flavor to them, as they asked students to list the four people who had been their best friends that semester. Second, the BPS collected detailed time-use information eight times each year; for our sample, this was done using the twenty-four hour time diary shown in Appendix A.1. Finally, questions on the baseline survey reveal the number of hours that a student studied per week in high school and how much the student expects to study per week in college. We refer to these variables as our study propensity measures. The survey data are merged with detailed administrative data on race, sex, high school grade point average (GPA), college entrance exam scores, and college GPA in each semester.

This paper focuses on the freshman year for students in the 2001 entering cohort.⁵ We focus on understanding grade outcomes during the freshmen year for two primary reasons. First, under the general liberal arts curriculum, students tend to have similar course loads in their first year. Second, we are able to characterize the network most completely in the first year both because survey response rates are very high in the first year and because over 80% of friends reported by students in their freshman year are themselves freshmen.⁶ These

⁵ We focus on this cohort because the survey contains more comprehensive time-use and friendship information for them. Information about time use was collected using time diaries for the 2001 cohort, while, for the 2000 cohort, this information was collected using questions that asked respondents to “think carefully about how much time was spent studying” in the last twenty-four hours. First semester friendship information was collected at the end of the first semester for the 2001 cohort, while, for the 2000 cohort, first semester friendship information was collected retrospectively during the second semester.

⁶ Approximately 88% of all entering students in the 2001 cohort completed our baseline survey, and

advantages tend to fade in subsequent years as friendships change (in part, due to dropout after the first year) and students' programs of study specialize.

3.1 Sample Construction

Our focus is on students who stayed in school for the full first year. There were a total of 331 students who fit this description. Our estimation sample consists of the 307 students (i.e., 93% of the 331) with friends in each semester. A student j is deemed to be a friend of student i if either i lists j as a friend or j lists i as a friend. This means that a student can have friends in a particular semester even if the student did not complete the friendship question in that semester. However, pooling the two semesters, we find that about 85% of the students in our final sample reported friendship information directly, via the friendship survey.

3.2 Descriptive Statistics

Tables 1-3 contain descriptive statistics for the sample. Table 1 shows descriptive statistics of student characteristics. The first row in each of the six panels shows overall descriptive statistics for the variable of interest described in the first column. Forty-four percent of students are male, 18% of students are black, the mean high school grade point average for the sample is 3.39, the mean combined score on the American College Test (ACT) is 23.26, and, on average, students studied 11.24 hours per week in high school and expect to study 24.96 hours per week in college. The subsequent rows in each panel show descriptive statistics for the variable of interest in the first column for different groups. For example, the third panel shows that, on average, males have lower high school grade point averages than females (3.24 vs. 3.51) and blacks have lower high school grade point averages than nonblacks (3.14 vs. 3.45). The fifth panel shows that blacks studied more, on average, in high school than other students (15.29 vs. 10.36).⁷

Table 2 shows descriptive statistics of outcomes during the first year. The first rows of panels 1 and 2, respectively, show that, on average, students study 3.45 hours per day in the first semester and 3.48 hours per day in the second semester. The subsequent rows of the first two panels show that, on average, males study less than females, blacks study more than nonblacks, and students with above-median high school GPAs study more than students

response rates remained high for the eleven subsequent surveys that were administered during the freshman year.

⁷The first two differences in means are significantly different at the 0.001 level. The averages of high school study time for blacks and nonblacks are significantly different at the 0.01 level.

with below-median high school GPAs.⁸ The first rows of panels 3 and 4, respectively, show that the average first semester GPA is 2.89 and the average second semester GPA is 2.93. The subsequent rows of the third and fourth panels show that males, blacks, and students with below-median high school GPAs all have lower average GPAs than their counterparts.⁹

As described at the beginning of this section, we define friendship as the union of reported links between two students that semester.¹⁰ Table 3 summarizes friend data for those who have at least one friend in each semester, stratified by the same characteristics as in Table 1. The top panel shows that students have 3.3 friends on average. The mean masks considerable variation: the minimum number of friends is one, while the maximum number of friends is 10. The second and third panels show that male and black students (and, therefore, female and nonblack students) sort strongly towards students with the same characteristics. For example, 74% of the friends of male students are male, while only 18% of the friends of female students are male. Similarly, 69% of the friends of black students are black, while only 7% of the friends of nonblack students are black. The fourth and fifth panels show that male and black students have friends with lower incoming GPAs and lower combined ACT scores. The sixth and seventh panels show that males have friends who studied less in high school and expect to study less in college (compared to females), while blacks have friends who studied more in high school and expect to study more in college (compared to nonblacks).

The last panel of Table 3 describes friend study time. Consistent with own study time in Table 2, the first row shows that, on average, friend study time is 3.5 hours per day. The second and third rows of the last panel show that average friend study time is much lower for males than for females (3.16 vs. 3.76 hours per day).

Table 4 shows other network characteristics. Both the probability that a first-semester friendship no longer exists in the second semester and the probability that a second-semester friendship was not present in the first semester are 0.51. Consistent with the findings from Table 3, the correlations on the right side of the table show substantial sorting on the basis of observable characteristics.

Table 5 presents descriptive OLS regression results predicting own study time (left column) and GPA (right column), pooling observations over both semesters. The study time regression shows evidence of significant partial correlations of one's own study time (computed as the average amount the student reports studying in the time diaries within a

⁸Pooling observations from both semesters, the first and last differences in means are significantly different at a 0.05 level and, given the relatively small number of black students, the middle difference in means is significant at a 0.10 level.

⁹Pooling observations from both semesters, all of these differences are significant at a 0.05 level.

¹⁰Therefore, the number of friends may exceed that elicited in the survey in Appendix A.1.

Table 1: Own summary statistics

Variable	Group	N	Mean	SD	Min	q1	q2	q3	Max
(1) Male indicator	all	307	0.44	0.5	0	0	0	1	1
	given black	55	0.45	0.5	0	0	0	1	1
	given nonblack	252	0.43	0.5	0	0	0	1	1
	given above-med. HS GPA	155	0.33	0.47	0	0	0	1	1
	given below-med. HS GPA	152	0.55	0.5	0	0	1	1	1
(2) Black indicator	all	307	0.18	0.38	0	0	0	0	1
	given male	134	0.19	0.39	0	0	0	0	1
	given female	173	0.17	0.38	0	0	0	0	1
	given above-med. HS GPA	155	0.10	0.31	0	0	0	0	1
	given below-med. HS GPA	152	0.26	0.44	0	0	0	1	1
(3) HS GPA	all	307	3.39	0.47	1.68	3.09	3.5	3.8	4
	given male	134	3.24	0.51	1.68	2.9	3.21	3.7	4
	given female	173	3.51	0.4	2.13	3.3	3.6	3.85	4
	given black	55	3.14	0.46	2.24	2.78	3.1	3.52	4
	given nonblack	252	3.45	0.46	1.68	3.19	3.53	3.8	4
	given above-med. HS GPA	155	3.77	0.17	3.5	3.6	3.8	3.9	4
	given below-med. HS GPA	152	3.00	0.35	1.68	2.8	3.08	3.29	3.47
(4) ACT	all	307	23.26	3.61	14	21	23	26	33
	given male	134	22.54	3.77	14	20	23	25	31
	given female	173	23.82	3.39	17	21	24	26	33
	given black	55	19.91	2.51	14	18	20	21	25
	given nonblack	252	23.99	3.4	14	22	24	26	33
	given above-med. HS GPA	155	24.45	3.53	17	22	25	27	33
	given below-med. HS GPA	152	22.04	3.28	14	20	22	24	31
(5) HS study	all	307	11.24	11.35	0	4	8	15	70
	given male	134	11.43	11.94	0	3.12	8	15	70
	given female	173	11.10	10.9	0	4	9	15	70
	given black	55	15.29	14	0	5	10.5	20	70
	given nonblack	252	10.36	10.51	0	3	7	14	70
	given above-med. HS GPA	155	10.66	10.44	0	4	8	14.5	70
	given below-med. HS GPA	152	11.84	12.21	0	3.38	8.25	15	70
(6) Expected study	all	307	24.96	11.61	0	17	23	31	64
	given male	134	22.72	11.08	0.97	16	20.75	27.38	64
	given female	173	26.68	11.74	0	19	25.5	33	57.5
	given black	55	28.56	13.56	0	19	25	38.5	57.5
	given nonblack	252	24.17	11.01	0	17	22.5	30.62	64
	given above-med. HS GPA	155	25.18	10.47	0	18	23.5	32	56
	given below-med. HS GPA	152	24.72	12.69	0	16	22.25	30.12	64

Note: The rows in each panel show descriptive statistics for the variable of interest in the first column, for the group in the second column. GPA is measured in GPA points (0-4). HS study and expected study are measured in hours/week.

semester) with own sex and own high school GPA. As for our study propensity measures, we estimate a positive, significant partial correlation between own study time and own high school study time. We do not estimate a significant correlation between own study time and expected study time when both propensity measures are included. However, when expected

Table 2: Own summary statistics for outcomes, by semester

Variable	Group	N	Mean	SD	Min	q1	q2	q3	Max
(1) Sem. 1 Own study	all	296	3.45	1.67	0	2.33	3.29	4.50	10.33
	given male	129	3.16	1.76	0	2.00	2.92	4.09	8.66
	given female	167	3.67	1.56	0	2.62	3.38	4.62	10.33
	given black	53	3.80	1.63	0	2.84	3.67	4.78	8.33
	given nonblack	243	3.37	1.67	0	2.25	3.25	4.37	10.33
	given above-med. HS GPA	153	3.60	1.7	0	2.41	3.34	4.75	8.58
	given below-med. HS GPA	143	3.28	1.61	0	2.25	3.22	4.04	10.33
(2) Sem. 2 Own study	all	278	3.48	1.6	0	2.23	3.34	4.75	9.00
	given male	117	3.19	1.67	0	2	3	4.34	9.00
	given female	161	3.68	1.52	0	2.58	3.41	4.79	7.75
	given black	50	3.75	1.55	0	2.74	3.5	4.96	7.33
	given nonblack	228	3.42	1.60	0	2.17	3.33	4.67	9.00
	given above-med. HS GPA	145	3.69	1.47	0	2.66	3.67	4.83	7.92
	given below-med. HS GPA	133	3.25	1.7	0	2.00	3.08	4.38	9.00
(3) Sem. 1 GPA	all	307	2.89	0.78	0	2.49	3.06	3.46	4.00
	given male	134	2.72	0.80	0.30	2.17	2.80	3.29	4.00
	given female	173	3.02	0.74	0	2.66	3.13	3.55	4.00
	given black	55	2.42	0.78	0	1.82	2.57	2.84	4.00
	given nonblack	252	3.00	0.74	0.3	2.58	3.11	3.55	4.00
	given above-med. HS GPA	155	3.19	0.62	0.52	2.81	3.29	3.69	4.00
	given below-med. HS GPA	152	2.59	0.8	0	2.00	2.66	3.12	4.00
(4) Sem. 2 GPA	all	301	2.93	0.78	0	2.53	3.05	3.46	4.00
	given male	131	2.74	0.84	0	2.38	2.82	3.33	4.00
	given female	170	3.07	0.71	0.44	2.66	3.20	3.54	4.00
	given black	53	2.58	0.86	0.44	2.22	2.62	3.33	3.78
	given nonblack	248	3	0.75	0.00	2.58	3.08	3.5	4.00
	given above-med. HS GPA	155	3.21	0.66	0	2.82	3.36	3.74	4.00
	given below-med. HS GPA	146	2.63	0.79	0.26	2.15	2.66	3.24	4.00

Note: The rows in each panel show descriptive statistics for the variable of interest in the first column, for the group in the second column. GPA is measured in GPA points (0-4). Own study is measured in hours/day.

study time is the only study propensity measure included, we find that it has a positive, significant partial correlation with own study time (t-statistic of 2.2). The overall contribution of these two variables is substantial, with their omission reducing R-squared from 0.169 to 0.087 (see Table 12 in the appendix). Our novel measures of the propensity to study clearly have content. One's own study time also has a significant positive partial correlation with friend study time (computed as the average over friends of their own study times). The GPA regression shows that own GPA has a significant positive partial correlation with being female, being nonblack, and having above-median high school GPA. Own GPA also has a significant partial correlation with own study time.

Table 3: Average friend summary statistics, pooled over both semesters

Variable	Group	N	Mean	SD	Min	q1	q2	q3	Max
(1) Num. friends	all	614	3.31	1.58	1	2	3	4	10
	given male	268	3.22	1.59	1	2	3	4	10
	given female	346	3.38	1.57	1	2	3	4	9
	given black	110	3.21	1.35	1	2	3	4	7
	given nonblack	504	3.33	1.62	1	2	3	4	10
	given above-med. HS GPA	310	3.34	1.62	1	2	3	4	10
	given below-med. HS GPA	304	3.28	1.53	1	2	3	4	8
	(2) Frac. male friends	all	614	0.43	0.39	0	0	0.33	0.75
given male		268	0.74	0.31	0	0.5	0.82	1	1
given not male		346	0.18	0.25	0	0	0	0.33	1
given black		110	0.43	0.4	0	0	0.33	0.83	1
given not black		504	0.42	0.39	0	0	0.33	0.75	1
given above-med. HS GPA		310	0.35	0.38	0	0	0.25	0.67	1
given below-med. HS GPA		304	0.5	0.39	0	0	0.5	1	1
(3) Frac. black friends		all	614	0.18	0.32	0	0	0	0.25
	given male	268	0.18	0.32	0	0	0	0.25	1
	given not male	346	0.17	0.33	0	0	0	0.2	1
	given black	110	0.69	0.38	0	0.43	1	1	1
	given not black	504	0.07	0.16	0	0	0	0	1
	given above-med. HS GPA	310	0.10	0.22	0	0	0	0	1
	given below-med. HS GPA	304	0.26	0.39	0	0	0	0.45	1
	(4) Friend HS GPA	all	614	3.37	0.32	2.24	3.2	3.41	3.62
given male		268	3.29	0.33	2.25	3.07	3.34	3.53	4
given not male		346	3.44	0.29	2.24	3.29	3.46	3.64	4
given black		110	3.18	0.34	2.25	2.96	3.19	3.41	4
given not black		504	3.42	0.30	2.24	3.25	3.45	3.63	4
given above-med. HS GPA		310	3.46	0.27	2.65	3.29	3.46	3.63	4
given below-med. HS GPA		304	3.29	0.35	2.24	3.08	3.35	3.55	3.92
(5) Friend ACT		all	614	23.29	2.63	16	21.67	23.33	25
	given male	268	22.72	2.64	16.33	21	23	24.64	31
	given not male	346	23.74	2.54	16	22	23.67	25.5	32
	given black	110	21.2	2.53	16	19.33	21	22.5	29
	given not black	504	23.75	2.43	16.33	22.25	23.67	25.33	32
	given above-med. HS GPA	310	23.79	2.42	17.5	22.23	23.67	25.33	32
	given below-med. HS GPA	304	22.78	2.74	16	21	23	25	30
	(6) Friend HS study	all	614	11.03	7.64	0	6	9.5	14.47
given male		268	10.53	7.37	0.5	5.17	9	14	37.33
given not male		346	11.41	7.83	0	6.5	9.79	14.6	70
given black		110	14.62	7.31	2.5	9.18	13.92	18.75	37
given not black		504	10.24	7.49	0	5.5	8.68	13.19	70
given above-med. HS GPA		310	11.48	8.44	0.5	6	9.7	14	70
given below-med. HS GPA		304	10.57	6.7	0	6	9.17	14.64	37.33
(7) Friend expected study		all	614	24.82	7.4	0	19.75	23.55	29.62
	given male	268	22.89	6.97	4.06	18.23	21.65	27.05	55
	given not male	346	26.33	7.38	0	21.02	25.06	31.38	52
	given black	110	28.05	8.53	12	21.35	28.9	33.79	51
	given not black	504	24.12	6.94	0	19.5	23	28.2	55
	given above-med. HS GPA	310	24.72	7.42	0	20	23.55	29.48	55
	given below-med. HS GPA	304	24.93	7.39	10.5	19.31	23.61	29.81	52
	(8) Friend study	all	614	3.5	1.72	0	2.47	3.26	4.28
given male		268	3.16	1.49	0.5	2.21	3	3.88	8.46
given not male		346	3.76	1.83	0	2.65	3.51	4.5	11.93
given black		110	3.78	1.77	0.5	2.7	3.52	4.47	10.81
given not black		504	3.44	1.7	0	2.4	3.2	4.24	11.93
given above-med. HS GPA		310	3.64	1.79	0	2.56	3.36	4.41	11.93
given below-med. HS GPA		304	3.36	1.64	0.5	2.36	3.17	4.13	10.81

Note: The rows in each panel show descriptive statistics for the variable of interest in the first column, for the group in the second column. GPA is measured in GPA points (0-4). Own and friend HS study and expected study are measured in hours/week. Own and friend study are measured in hours/day. The variable "Friend z " for student i in period t is the average of the variable z across i 's friends in period t .

4 Model

Students are indexed by $i = 1, \dots, N$ and time periods (semesters) by $t = 1, 2$. We denote the study time of student i in time period t as s_{it} and let S_t define a column vector collecting all students' study times during that period. We treat the adjacency matrix representing the network of friendships as pre-determined. This matrix in period t , denoted A_t , has a main diagonal of zeros and an (i, j) entry of one if student i has j as a friend and zero otherwise.¹¹

¹¹Other than its being full rank, we impose no restrictions on A_t . Though in our baseline empirical specification we use the union of reported links (i.e., $A_t(i, j) = 1$ if either i reports being friends with j , or

Table 4: Network characteristics

		Correlations between own and avg. of friends	
Friendship transitions		Black	0.74
Prob. friendship reported first semester but not second		Male	0.71
0.51		HS GPA	0.23
Prob. second semester friendship is new	0.51	Combined ACT	0.31
		HS study time	0.23
		Expected study time	0.14

Note: Pooled over both semesters

Table 5: Study time and GPA OLS regressions

	<i>Dependent variable:</i>	
	Own study (1)	GPA (2)
Male	-0.369** (0.171)	-0.131* (0.076)
Black	0.116 (0.214)	-0.225** (0.109)
HS GPA	0.413** (0.188)	0.437*** (0.081)
ACT	-0.032 (0.023)	0.040*** (0.013)
HS study	0.043*** (0.008)	0.001 (0.004)
Expected study	-0.002 (0.009)	-0.006 (0.003)
Friend study	0.166*** (0.039)	
Own study		0.090*** (0.022)
Constant	1.915** (0.759)	0.417 (0.362)
Observations	574	571
R ²	0.169	0.259

Note: *p<0.1; **p<0.05; ***p<0.01. Standard errors clustered at the student level are in parentheses. GPA is measured in GPA points (0-4). Own and friend HS study and expected study are measured in hours/week. Own and friend study are measured in hours/day. The variable “Friend z” for student i in period t is the average of the variable z across i ’s friends in period t .

The average study time of i 's friends during period t is

$$s_{-it} = \frac{\sum_{j=1}^N A_t(i, j) s_{jt}}{\sum_{j=1}^N A_t(i, j)}. \quad (1)$$

Taking into account their friends, students make decisions about how much to study in a particular semester by considering the costs and benefits of studying. The benefits of studying come from the accumulation of human capital. The production function for human capital, which we will also refer to as achievement, $y(\cdot)$, is:

$$y(s_{it}, \mu_{yi}) = \beta_1 + \beta_2 s_{it} + \mu_{yi}, \quad (2)$$

where μ_{yi} is a “human capital type” which allows the amount a person learns in school to vary across people, conditional on her own study level. As will be discussed in Section 5, in practice, this type will be constructed using observable characteristics that have consistently been found to influence academic performance. We adopt a value-added formulation for the evolution of human capital, i.e., the human capital type is assumed to a sufficient statistic for the history of prior inputs.

The cost of studying, $c(\cdot)$, is determined by:

$$c(s_{it}, s_{-it}, \mu_{si}) = \theta_1 s_{it} + \theta_2 \gamma(\mu_{si}) s_{it} + \frac{\theta_3 s_{it}}{s_{-it}^{\tau_s}} + \frac{\theta_4 \gamma(\mu_{si}) s_{it}}{s_{-it}^{\tau_s}} + \frac{\theta_5 s_{it}^2}{2 s_{-it}^{\tau_s}}, \quad (3)$$

where friend study time enters the cost function by reducing the cost of one's own studying, with curvature given by the exponent τ_s . As we show below, this cost function produces a best response function with desirable properties. Studying may be less arduous when one's friends are studying. We discuss below how this specification of the cost function is observationally equivalent with one in which social interactions are instead driven by conformity forces. The term μ_{si} is i 's “study type,” which allows the disutility from studying to vary across students, conditional on own and friend study levels. As will be discussed in Section 5, in practice, this type will be constructed from observable characteristics that help explains one's study time choices. Study types enter the model through $\gamma(\cdot)$. We define

$$\gamma(\mu_{si}) = \frac{1}{\exp(\tau_{\mu,1} \mu_{si} + \tau_{\mu,2} \mu_{si}^2)}, \quad (4)$$

which allows the cost function to have intercepts and slopes that vary across people of different study types. We refer to $\gamma(\mu_{si})$ as the “effective study type”. We do not include a

 vice versa), the model could also accommodate non-reciprocal links (i.e., i may link to j without j linking to i).

fixed cost of studying because very few students report zero study time over the semester.

With knowledge of $\{A_1, A_2\}$, all students' human capital types $\{\mu_{yi}\}_{i=1}^N$ and all students' study time types $\{\mu_{si}\}_{i=1}^N$, students simultaneously choose study times to maximize utility, which we assume to be separable across periods:¹²

$$u(s_{i1}, s_{i2}) = \left\{ \sum_{t=1}^2 y(s_{it}, \mu_{yi}) - c(s_{it}, s_{-it}, \mu_{si}) \right\}. \quad (5)$$

4.1 Model Solution

Each student's decision problem is additively separable across time periods, meaning each student can solve each period's problem separately.¹³ Student i 's best response to friend study time in t is given by:

$$s_{it} = \arg \max_{s \in [0, 24]} \{y(s, \mu_{yi}) - c(s, s_{-it}, \mu_{si})\}, \quad (6)$$

with the natural constraints that study time is nonnegative and cannot exceed 24 hours per day. The first order condition of (6) with respect to own study time yields $\frac{\partial y}{\partial s} = \frac{\partial c}{\partial s}$, i.e., the utility-maximizing study time equates the marginal return for increasing study time with the marginal cost. Expanding the first order condition gives:

$$\beta_2 = \theta_1 + \theta_2 \gamma(\mu_{si}) + \theta_3 \frac{1}{s_{-it}^{\tau_s}} + \theta_4 \frac{\gamma(\mu_{si})}{s_{-it}^{\tau_s}} + \theta_5 \frac{s_{it}}{s_{-it}^{\tau_s}}. \quad (7)$$

Solving for own study time yields the best response function, which expresses student i 's study time as a function of friend study time, at an interior solution:

$$s_{it} = -\frac{\theta_3}{\theta_5} - \frac{\theta_4}{\theta_5} \gamma(\mu_{si}) + \frac{(\beta_2 - \theta_1)}{\theta_5} s_{-it}^{\tau_s} - \frac{\theta_2}{\theta_5} \gamma(\mu_{si}) s_{-it}^{\tau_s}. \quad (8)$$

Equation (3) shows that the term associated with θ_5 introduces curvature into the student's cost function. If θ_5 were zero, the student's objective in (6) would be linear in own study time and there would not exist an interior best response to friend study time. Equation (8) also shows that one of the preference parameters θ must be normalized. Therefore, we normalize θ_5 to one, resulting in the final form of the student best response function, for an

¹²The alternative assumption, where students know only the current adjacency matrix when choosing their study times and calculate expectations over the future adjacency matrix, would have identical predictions in our model. See Section 4.1.

¹³If utility were nonlinear in semester achievement or the argument of the cost function were study time over the whole year, the problem would no longer be separable across time periods. We assume student utility is linear in achievement because non-linearity of utility in achievement would be difficult to separate from non-linearity in the cost function without relying on functional form restrictions.

interior solution:

$$s_{it} = -\theta_3 - \theta_4\gamma(\mu_{si}) + (\beta_2 - \theta_1)s_{-it}^{\tau_s} - \theta_2\gamma(\mu_{si})s_{-it}^{\tau_s} \equiv \psi(s_{-it}, \mu_{si}). \quad (9)$$

Note that while best response functions depend on study type μ_{si} , it is sometimes notationally convenient to suppress the study type and write the best response function as $\psi_i(s_{-it})$. Own study time is increasing linearly in the productivity of own study time β_2 and may also be increasing in own effective study type, μ_{si} , depending on θ_2 and θ_4 . We restrict parameters so that own study time has a strictly positive intercept and is a weakly increasing and weakly concave function of friend study time.¹⁴

As shown in Section 4.1.1, concave best response functions ensure existence of a unique equilibrium for the study time game. As shown in equations (8) and (9), the separable form we adopt for the cost function has the benefit of producing a closed-form solution for the student best response function. We show in Appendix B.1 that concavity of the best response function would result from any cost function possessing the natural properties of being strictly convex in s_{it} and weakly concave in s_{-it} .

4.1.1 Equilibrium

Definition 1 (Period Nash equilibrium). *A pure strategy Nash equilibrium in study times $S^* = [s_1^*, s_2^*, \dots, s_N^*]'$ satisfies $s_i^* = \psi(s_{-i}^*, \mu_{si})$, for $i \in N$, given adjacency matrix A .*

Claim 1. *Let k be a number strictly greater than 24 . There exists a unique pure strategy Nash equilibrium if $\psi_i : R^N \mapsto R$ are weakly concave and weakly increasing, $\psi_i(0) > 0$, and $\psi_i(k) < k$ for $i \in N$.*

Proof. See Appendix B.2. □

We compute the equilibrium by iterating best responses.

4.2 Model Discussion

4.2.1 Friend Study Time

We define friend study time as the average study times of one's friends. Our framework could also accommodate specifications where friend study time was defined to be the total study

¹⁴ The strictly positive intercept restriction corresponds to $\min_{i \in N} \{-\theta_3 - \theta_4\gamma(\mu_{si})\} > 0$. The weakly increasing restriction corresponds to $\min_{i \in N} \{(\beta_2 - \theta_1) - \theta_2\gamma(\mu_{si})\} \geq 0$. Weak concavity corresponds to further requiring $\tau_s \leq 1$. These restrictions, combined with $s_{it} \leq 24$, are sufficient to have the well-behaved equilibrium described in Section 4.1.1. In practice, however, we are able to estimate the model using weaker restrictions, described in Section 5.

time of one’s friends. Indeed, we previously estimated a specification of our model in which the denominator of (1) was $\alpha \sum_{j=1}^N A_t(i, j) + (1 - \alpha)$, where $\alpha \in [0, 1]$, $\alpha = 1$ corresponds to the average of friends’ study times, and $\alpha = 0$ corresponds to the total of friends’ study times. We define friend study time to be the average of friends’ study times because we found α to be 1.

4.2.2 Other Mechanisms Generating Social Interactions

Conformity Our specification of the cost function allows friend study effort to reduce one’s own cost of studying. Others have allowed social interactions to emerge from a cost of deviating from peer actions, i.e., from a force producing conformity (see, e.g., Brock and Durlauf (2001), Moffitt (2001), Blume et al. (2015)). We show in Appendix B.3.1 that such a specification would be observationally equivalent to the one we adopt.

Production Complementarities Another proposed mechanism is that social interactions arise through production complementarities, where increases in peer inputs increase the marginal product of one’s own input (e.g., Calvó-Armengol et al. (2009)). We show in Appendix B.3.2 that, in the typical case, where one only had data on either the input (e.g., study effort) or output (e.g., achievement), our cost-reduction-based specification (or, equivalently, a conformity-based specification) would be observationally equivalent to a specification exhibiting production complementarities. This point is also made by Blume et al. (2015). However, because we measure both inputs and outcomes, we can check for evidence of production complementarities. As we discuss in Section 7.4, we do not find such evidence in our context.

4.2.3 Dynamic Behavior

We assume the human capital type is constant between the periods. Though it is feasible to extend our static framework to a dynamic framework allowing the human capital type to evolve between periods, the benefits of doing this are mitigated by two facts: (1) each model period corresponds to a semester, which is shorter than the period typically considered when estimating value-added production functions in an educational context (see Hanushek (1979) and Todd and Wolpin (2003) for discussions of issues related to the estimation of education production functions), and (2) we study students during their freshman year, which, under the liberal-arts curriculum at Berea, is typically before they start taking specialized course material (meaning second semester coursework does not build heavily on first semester coursework). Consistent with these facts, as we discuss in Section 7.5, we find

that out-of-sample outcomes, simulated from parameters estimated on only first-semester data, fit second-semester data quite well.

5 Estimation

The model provides a mapping from the adjacency matrix A_t and all the students' types $\{(\mu_{si}, \mu_{yi})\}_{i=1}^N$ to a unique equilibrium in study times for all students, S_t^* . The equilibrium study times S_t^* generate achievement in equilibrium y_{it}^* , via the production function $y(s_i, \mu_{yi})$. The model is operationalized by parameterizing a student's types as linear combinations of observable characteristics collected in a vector x_i . That is, $\mu_{si} = x_i' \omega_s$ and $\mu_{yi} = x_i' \omega_y$, where the parameter vectors ω_s and ω_y respectively determine study and human capital types.¹⁵ The vector x_i includes indicators for being black and being male, along with high school GPA, combined ACT score, average hours per week of study time in high school, and expected hours per week of study time in college. This allows us to express each student's equilibrium study time and achievement as a function of A_t and all students' characteristics, which we collect in a matrix X . Given the full set of (model) parameters $\Gamma = (\beta_1, \beta_2, \theta_1, \theta_2, \theta_3, \theta_4, \omega_s, \omega_y, \tau_{\mu,1}, \tau_{\mu,2}, \tau_s)'$, we write these outcomes for individual i as

$$s_{it}^* = \psi(s_{-it}^*, \mu_{si}) = \delta_i^s(A_t, X; \Gamma) \quad (10)$$

and

$$y_{it}^* = y(s_{it}^*, \mu_{yi}) = \delta_i^y(A_t, X; \Gamma), \quad (11)$$

where s_{-it}^* is defined by applying equation (1) to S_t^* and A_t .

Our measure of achievement, denoted \tilde{y}_{it} , is the student's semester grade point average (GPA), which is measured on a four-point scale. In our data, 7% of student-semester observations have a GPA of four and 1% have a GPA of zero. Therefore, we take a Tobit approach to modeling GPA. We define latent GPA as $y_{it}^* + \eta_{yit}$, where η_{yit} is a Gaussian measurement error that is IID and independent from A and X . Our Tobit model, with censoring at zero and four, is

$$\tilde{y}_{it} = \begin{cases} 4 & \text{if } y_{it}^* + \eta_{yit} \geq 4 \\ 0 & \text{if } y_{it}^* + \eta_{yit} \leq 0 \\ y_{it}^* + \eta_{yit} & \text{otherwise.} \end{cases} \quad (12)$$

The GPA component of the likelihood function for individual i at time t is the likelihood for

¹⁵We set coefficient on high school GPA in the study type $\omega_{s, \text{HS GPA}} = 1$ to identify $\gamma(\cdot)$.

this Tobit model:

$$L_{it}^y = \Phi \left(\frac{0 - \delta_i^y(A_t, X; \Gamma)}{\sigma_{\eta_y}} \right)^{\mathbf{1}_{\{\tilde{y}_{it}=0\}}} \times \left(1 - \Phi \left(\frac{4 - \delta_i^y(A_t, X; \Gamma)}{\sigma_{\eta_y}} \right) \right)^{\mathbf{1}_{\{\tilde{y}_{it}=4\}}} \times \frac{1}{\sigma_{\eta_y}} \phi \left(\frac{\tilde{y}_{it} - \delta_i^y(A_t, X; \Gamma)}{\sigma_{\eta_y}} \right), \quad (13)$$

where Φ and ϕ denote the CDF and PDF, respectively, of the standard normal distribution.

The likelihood function also takes into account study time outcomes. Our measures of s_{it}^* come from up to four 24-hour time diaries completed by each student i in semester t . We use R_{it} to denote the set of reports for student i in semester t . Study time report r for student i in semester t is denoted \tilde{s}_{rit} , and is allowed to be a noisy measure of s_{it}^* .¹⁶ Because approximately 5% of our study time observations are zero, we use a Tobit approach for reported study time. Defining latent study time as $s_{it}^* + \eta_{srit}$, reported study time is

$$\tilde{s}_{rit} = \begin{cases} 0 & \text{if } s_{it}^* + \eta_{srit} \leq 0 \\ s_{it}^* + \eta_{srit} & \text{otherwise.} \end{cases} \quad (14)$$

The likelihood contribution for report r of student i in semester t is

$$L_{rit}^s = \Phi \left(\frac{0 - \delta_i^s(A_t, X; \Gamma)}{\sigma_{\eta_s}} \right)^{\mathbf{1}_{\{\tilde{s}_{rit}=0\}}} \times \frac{1}{\sigma_{\eta_s}} \phi \left(\frac{\tilde{s}_{rit} - \delta_i^s(A_t, X; \Gamma)}{\sigma_{\eta_s}} \right). \quad (15)$$

The total likelihood contribution for student i is therefore¹⁷

$$L_i = \left(\prod_t \prod_{r \in R_{it}} L_{rit}^s \right) \times \left(\prod_t L_{it}^y \right), \quad (16)$$

the sum of which across students we maximize to obtain our estimated parameters.¹⁸

6 Specification Test

This section develops a specification test that has power against alternative data generating processes that have unobserved determinants of study time. It presents the test statistic,

¹⁶Stinebrickner and Stinebrickner (2004) document how reported study time varies within semesters.

¹⁷We allow for dependence in both types of measurement errors between semesters.

¹⁸Note that the theoretical model assumes best response functions are strictly positive, nondecreasing, and weakly concave. These restrictions are difficult to directly impose in terms of restrictions on the parameter space when there is heterogeneity in best response functions. Therefore, we adopt an indirect approach, of verifying whether best response functions derived from posited parameters satisfy the restrictions. Specifically, when estimating the model, we use the weaker restrictions that the 75th percentile effective study type's best-response function is nonnegative and that equilibrium study times are strictly positive; we also impose the natural upper bound on daily study time (24 hours a day). As we show in Section 7, none of these restrictions are close to binding at our estimated parameters.

shows how to calculate the residuals used to compute it, and shows how to decompose these residuals in a way that facilitates our analysis of when the test has power. We develop the test assuming there is one study time report and one period, which allows us to drop the corresponding subscripts, and that there is no censoring in observed study times. We show how we implement our test using more than one study time report and more than one period in Section 7.2.

Let $\widehat{\Gamma}$ denote the vector of estimated parameters and let \tilde{s}_i denote i 's reported study time. The study time residual for student i is

$$\widehat{\eta}_{si} = \tilde{s}_i - \delta_i^s(A, X; \widehat{\Gamma}), \quad (17)$$

and the average of i 's friends' residuals is

$$\widehat{\eta}_{s,-i} = \frac{\sum_{j=1}^N A(i, j) \widehat{\eta}_{sj}}{\sum_{j=1}^N A(i, j)}. \quad (18)$$

Consider the following regression of a student's own residual on the average of her friends' residuals:

$$\widehat{\eta}_{si} = a + b\widehat{\eta}_{s,-i} + \xi. \quad (19)$$

Under the null hypothesis of proper specification, the error terms in our study time regression are IID, so the true value of b is zero. Our test statistic is simply the t-statistic for a test of $b = 0$ in regression (19), $\widehat{b}/SE(\widehat{b})$, which has a limiting standard normal distribution under the null.

Our claim is that this specification test will have power against alternatives where omitted variables are present. Intuitively, if there are important unobserved variables influencing students' decisions, they will generally induce cross-sectional correlation across students because they will enter students' best responses in equilibrium. Therefore, an absence of correlation in residuals across students is consistent with a lack of omitted variables. We show this more formally now.

Consider the following scenario with an (potentially) omitted variable. We examine the special case with $\tau_s = 1$. As we show in Section 7, this case is consistent with our baseline empirical results, where we find that best response functions are linear.

Using a composite parameter $c \equiv [\beta_2 - \theta_1]$, define the subset of parameters identified by just equation (9), the student's policy function, as $\Gamma_2 = (c, \theta_2, \theta_3, \theta_4, \omega_s, \tau_{\mu,1}, \tau_{\mu,2})'$. To simplify notation, we refer to the terms in (9), $[-\theta_3 - \theta_4\gamma(\mu_{si})]$ and $[(c - \theta_2\gamma(\mu_{si}))s_{-i}]$, as $f_1(x_i; \Gamma_2)$ and $f_2(x_i; \Gamma_2)$, respectively. As in Section 5, x_i contains student i 's observed characteristics, which enter the policy function through effective study type $\gamma(\mu_{si})$. The

equation for an individual student is

$$s_i = f_1(x_i; \Gamma_2) + f_2(x_i; \Gamma_2)s_{-i}. \quad (20)$$

In order to represent the system of equations for all students in a vector S , use $F_1(X; \Gamma_2)$ to denote a column vector stacking the $f_1(x_i; \Gamma_2)$ for all i . We use the notation $W(X; \Gamma_2)$ for a matrix that has zeros in the same positions as the zeros in A and nonzero entries in locations where A has ones. In place of the ones in row i of A , $W(X; \Gamma_2)$ contains

$$\frac{1}{\sum_{j=1}^N A(i, j)} [f_2(x_i; \Gamma_2)]. \quad (21)$$

The system of equations is thus:

$$S = F_1(X; \Gamma_2) + W(X; \Gamma_2)S. \quad (22)$$

Note that (22) is simply a re-written version of the baseline model we developed in Section 4. Solving for S , we obtain the equilibrium vector of study times

$$S^* = (I - W(X; \Gamma_2))^{-1} [F_1(X; \Gamma_2)], \quad (23)$$

where the right side corresponds to the vector stacking $\delta_i^s(A, X; \Gamma)$ for all students.¹⁹

Incorporating our measurement error η_s , we obtain the data generating process for observed study time \tilde{S} under the *null hypothesis* of correct specification:

$$\tilde{S} = (I - W(X; \Gamma_2))^{-1} [F_1(X; \Gamma_2)] + \eta_s. \quad (24)$$

Now consider an alternative in which the model was misspecified. In particular, suppose a vector of characteristics V was omitted by the econometrician but was observed by all students, entering the best response system in the following manner:

$$S = F_1(X; \Gamma_2) + W(X; \Gamma_2)S + V. \quad (25)$$

Again solving for S , the equilibrium system of equations has the following form:

$$S^* = (I - W(X; \Gamma_2))^{-1} [F_1(X; \Gamma_2) + V]. \quad (26)$$

In general, the matrix $(I - W(X; \Gamma_2))^{-1}$ will have many non-zero entries because students will typically be directly or indirectly connected to many other students. Therefore, many, if not

¹⁹ Note that, as it expresses outcomes as a reduced form in terms of X and A , the specification test would not be affected by the inclusion of “contextual effects” in the typical additively separable manner.

all, elements of V will influence a given student's equilibrium study time in this alternative.

Decompose V into two components according to:

$$V = \Pi(X) + u, \quad (27)$$

where we assume that u is mean independent of X (and, hence, $F_1(X; \Gamma_2)$) and $W(X; \Gamma_2)$. We are agnostic about correlation patterns in u . For example, students with high x_i may have high, low, or average values of u . However, it may be the case that when a student has a high x_i and a high u_i , she is likely to also have a friend with a high u_j . Substituting this expression for V into (26) and incorporating our measurement error η_s gives the data generating process for observed study time under the *alternative hypothesis*:

$$\begin{aligned} \tilde{S} &= (I - W(X; \Gamma_2))^{-1} [F_1(X; \Gamma_2) + \Pi(X) + u] + \eta_s \\ &= (I - W(X; \Gamma_2))^{-1} [F_1(X; \Gamma_2) + \Pi(X)] + (I - W(X; \Gamma_2))^{-1} u + \eta_s. \end{aligned} \quad (28)$$

It is convenient to re-write (28) with a composite error ϵ :

$$\begin{aligned} \tilde{S} &= (I - W(X; \Gamma_2))^{-1} [F_1(X; \Gamma_2)] + \epsilon, \\ \text{where } \epsilon &= (I - W(X; \Gamma_2))^{-1} \Pi(X) + (I - W(X; \Gamma_2))^{-1} u + \eta_s. \end{aligned} \quad (29)$$

By definition, residuals must be computed using estimates of Γ_2 , rather than the true value. To derive the residuals $\tilde{\epsilon}$, consider the least squares estimator of Γ_2 in the study time regression, $\hat{\Gamma}_2$, i.e., the estimate of Γ_2 that minimizes $\epsilon' \epsilon$ in (29). The fitted values for \tilde{S} using $\hat{\Gamma}_2$ are $(I - W(X; \hat{\Gamma}_2))^{-1} [F_1(X; \hat{\Gamma}_2)]$. Let $\tilde{\Gamma}_2$ denote the probability limit of $\hat{\Gamma}_2$. In large samples, the fitted values of \tilde{S} based on our estimator would then be $(I - W(X; \tilde{\Gamma}_2))^{-1} [F_1(X; \tilde{\Gamma}_2)]$, which we can add and subtract from (29), resulting in

$$\tilde{S} = (I - W(X; \tilde{\Gamma}_2))^{-1} [F_1(X; \tilde{\Gamma}_2)] + \tilde{\epsilon}, \quad (30)$$

where

$$\begin{aligned} \tilde{\epsilon} &\approx \underbrace{\{(I - W(X; \Gamma_2))^{-1} [F_1(X; \Gamma_2) + \Pi(X)] - (I - W(X; \tilde{\Gamma}_2))^{-1} [F_1(X; \tilde{\Gamma}_2)]\}}_{\text{“prediction bias”}} \\ &+ \underbrace{(I - W(X; \Gamma_2))^{-1} u}_{\text{equilibrium propagation of } u} + \eta_s. \end{aligned} \quad (31)$$

The first term (“prediction bias”) in $\tilde{\epsilon}$ is due to the omission of $\Pi(\cdot)$, i.e., it represents a mean misspecification in (30). As we show below, there will not necessarily be a prediction bias. The second term is due to the influence of u upon equilibrium study effort. This second

term is what our specification test is designed to detect. $\widehat{\Gamma}_2$ will, in general, be inconsistent for Γ_2 if $\Pi(\cdot) \neq 0$.

In general, our test will have power, i.e., the ability to detect the type of alternative (25), because the error $\tilde{\epsilon}$ will exhibit cross-sectional correlation when $V \neq 0$. We show this by considering cases (i) without prediction bias and (ii) with prediction bias.

There would be no prediction bias (i.e., we would be in case (i)) if there exists a $\ddot{\Gamma}_2$ such that $F_1(X; \ddot{\Gamma}_2)$ nests $F_1(X; \Gamma_2) + \Pi(X)$.²⁰ In principle, this nesting could be accomplished by adopting a sufficiently flexible functional form for $F_1(\cdot; \cdot)$. Therefore, in this case, although elements of Γ_2 may be inconsistently estimated (i.e., $\text{plim } \widehat{\Gamma}_2 \neq \Gamma_2$), residuals obtained from (30) would only include components based on u and η_s . That is, bias in $\widehat{\Gamma}_2$ would not pervade to the residuals.²¹ Of course, in practice, it may be necessary to impose restrictions on $F_1(X; \cdot)$, meaning there may potentially be prediction bias in study time. We discuss this in case (ii).

Case (i): No prediction bias: Consider first the case with no prediction bias, leaving us to focus on the u component of $\tilde{\epsilon}$ in (31). In general, the term $(I - W(X; \Gamma_2))^{-1}u$ will exhibit cross-sectional dependence because its elements are linear combinations of many of the components of u .

In order for there to be no cross-sectional covariance in $(I - W(X; \Gamma_2))^{-1}u$, the shocks u would need to have a covariance matrix that was orthogonalized by $(I - W(X; \Gamma_2))^{-1}$. For example, consider the case where u was generated according to

$$u = (I - W(X; \Gamma_2))e, \tag{32}$$

with e IID and $E[ee'] = I$. For reasonable ranges of $W(X; \Gamma_2)$ in our application, such a u process would possess strong negative correlations among closely linked students. For example, consider our point estimate for Γ_2 , which we present in Section 7, and our baseline adjacency matrix for the first semester, A_1 . For the process in (32), in order for u to be orthogonalized by $(I - W(X; \Gamma_2))^{-1}$, the ratio of the average covariance of u between friends to the average variance across students would have to be -0.31.

The main focus of the literature is on the case of positive assortative matching.²² There-

²⁰This is because the u are mean independent from X and $W(X; \Gamma_2)$, which means that the least-squares estimate of Γ_2 , which minimizes $e'\epsilon$, would minimize the prediction bias component of $\tilde{\epsilon}$.

²¹For example, this would be true in the commonly considered case where we can write $F_1(X; \Delta_1) = X\Delta_1$ and $\Pi(X) = X\Delta_2$, where Δ_1 and Δ_2 are matrices of parameters, in which case the estimated $\widehat{\Delta}_1$ would have $\text{plim } \widehat{\Delta}_1 = \Delta_1 + \Delta_2$.

²²Epple and Romano (2011) contains a thorough discussion of sorting in the presence of peer effects. Zeitlin (2011) studies peer effects in a social learning context, finding that own and friend information shocks are negatively correlated. This finding is unsurprising in a learning environment, where one may gain more when

fore, we believe such a negative correlation is not the most salient one. Further note that the necessary orthogonalization could not occur when u are independent in the cross section. Moreover, even in the presence of negative cross-sectional correlations in u , only specific correlation structures could produce the necessary orthogonalization. In our example above, negative covariances in u that were either larger or smaller than -0.31 would generate correlated residuals ($\tilde{\epsilon}$). In summary, our test will have power to detect the omitted variables u as long as they do not have very specific covariance structures.

Case (ii): Prediction bias: In the case where there is a prediction bias in study time (which can only occur if there is an omitted variable bias, i.e., $\Pi(\cdot)$ is nonzero), our test would not have power if the first term in equation (31), the prediction bias term, offset cross-sectional correlations in $(I - W(X; \Gamma_2))^{-1}u$, such that there would be no cross-sectional covariance in ϵ . For example, negative covariances in the bias term could, in principle, exactly cancel with the positive covariances that we anticipate in $(I - W(X; \Gamma_2))^{-1}u$. Our strong prior is that this scenario is implausible, due to the positive covariances across friends in their values of x_i and the bias term being a smooth function of x_i . Intuitively, because friends have similar observed characteristics (x_i), the prediction errors of students and their friends—which would only exist due to the inability of $F_1(X; \cdot)$ to fit study time for students with certain observed characteristics—will likely be positively correlated. Most importantly, *prediction bias would have to exactly cancel out the u component* to not have power against the alternative hypothesis. Such a problematic scenario would be a knife-edge case.

To make the test developed above more concrete, in Appendix E we develop an example environment with dyadic, separate networks with homogeneous best responses. In addition to simplifying notation, the specification developed in Appendix E corresponds to case (i), i.e., there is no prediction bias.

7 Estimation Results

Table 6 contains parameter estimates. The top panel presents the parameters that enter the achievement production function. The key parameter is the marginal product of own study time on achievement, β_2 . The point estimate of 0.254 implies that increasing own study time by one hour per day increases achievement by about a quarter of a GPA point, *ceteris paribus*. It is reassuring that this result is quantitatively similar to that from Stinebrickner and Stinebrickner (2008a), who estimate that, for freshman at Berea, an extra hour per day of studying would increase GPA by 0.36 points (with a standard error of 0.183 points),

one's friends have different information.

using whether a randomly assigned roommate brought a video game as a shifter for one's own study time. Table 6 shows that students with high GPAs in high school and high ACT scores have significantly higher human capital, and black students have significantly lower human capital.

Table 6: Parameter Estimates

Parameter	Estimate	SE	Description
Production function: $y = \beta_1 + \beta_2 s_{it} + \mu_{yi}$ and $\mu_{yi} = x'_i \omega_y$			
β_1	-0.350	0.4185	intercept
β_2	0.254	0.0651	marginal product of own study time
$\omega_{y,HS\ GPA}$	0.470	0.0808	coefficient on HS GPA in human capital type
$\omega_{y,ACT}$	0.047	0.0112	coefficient on ACT in human capital type
$\omega_{y,Black}$	-0.213	0.1074	coefficient on Black in human capital type
$\omega_{y,Male}$	-0.037	0.0849	coefficient on Male in human capital type
$\omega_{y,HS\ study}$	-0.007	0.0042	coefficient on HS study in human capital type
$\omega_{y,expected\ study}$	-0.005	0.0035	coefficient on expected study in human capital type
Study cost function: $c = \theta_1 s_{it} + \theta_2 \gamma(\mu_{si}) s_{it} + \frac{\theta_3 s_{it}}{s_{-it}^{\tau_s}} + \frac{\theta_4 \gamma(\mu_{si}) s_{it}}{s_{-it}^{\tau_s}} + \frac{s_{it}^2}{2s_{-it}^{\tau_s}}$ and $\mu_{si} = x'_i \omega_s$			
θ_1	-1.074	0.1551	study cost terms
θ_2	0.874	0.2351	study cost terms
θ_3	-0.907	0.8097	study cost terms
θ_4	0.096	1.2800	study cost terms
τ_s	1.000	–	curvature on friend study time*
$\tau_{\mu,1}$	0.105	0.0601	linear term for study type
$\tau_{\mu,2}$	-0.003	0.0028	quadratic term for study type
$\omega_{s,HS\ GPA}$	1.000	–	coefficient on HS GPA in study type, fixed to 1
$\omega_{s,ACT}$	-0.063	0.0870	coefficient on ACT in study type
$\omega_{s,Black}$	-0.735	0.7459	coefficient on Black in study type
$\omega_{s,Male}$	-1.065	0.7892	coefficient on Male in study type
$\omega_{s,HS\ study}$	0.344	0.1554	coefficient on HS study in study type
$\omega_{s,expected\ study}$	0.005	0.0309	coefficient on expected study in study type
Shocks			
σ_{η_y}	0.721	0.0185	sd measurement error for human capital
σ_{η_s}	2.159	0.0377	sd measurement error for observed study time

* Recall that we allowed for $\tau_s \in [0, 1]$, but, finding it to be indistinguishable from 1, we fixed $\tau_s = 1$ and re-estimated.

As can be seen in equation (9), the curvature in the best response function is given by τ_s , the exponent on s_{-it} . We estimated the model allowing τ_s to be in the set $[0, 1]$, nesting

the assumption of a linear best response function (i.e., that $\tau_s=1$).²³ However, because our initial estimation provided evidence that τ_s is indistinguishable from 1, we re-estimated the model fixing $\tau_s=1$.

Estimates of the parameters in the study cost function appear in the second panel of Table 6. To ease their interpretation, we substitute them into the best response function, yielding

$$\widehat{\psi}(s_{-it}, \widehat{\mu}_{si}) = \{0.907 - 0.096\widehat{\gamma}(\widehat{\mu}_{si})\} + \{1.328 - 0.874\widehat{\gamma}(\widehat{\mu}_{si})\} s_{-it}. \quad (33)$$

The first bracketed term in equation (33) represents the intercept of the best response function for student i , i.e., how much this student would study even if her friends did not study at all. This term consists of $-\theta_3 = 0.907$, the common component of the intercept across students, and $-0.096\widehat{\gamma}(\widehat{\mu}_{si})$, the component characterizing variation in the intercept across students. Likewise, the second bracketed term in equation (33) reveals the slope, or *reactiveness*, of the best response function, that is, how a student's choice of study time depends on the study time of her friends. This term consists of $(\beta_2 - \theta_1) = 1.328$, the common component of the slope across students, and $-0.874\widehat{\gamma}(\widehat{\mu}_{si})$, the component characterizing variation in the slope across students. The negative point estimate for θ_1 means that the common slope component of student study times was higher than could be explained by only the marginal product of study time in producing achievement (β_2). With $\gamma(\mu_{si}) = \frac{1}{\exp(\tau_{\mu,1}\mu_{si} + \tau_{\mu,2}\mu_{si}^2)}$, the latter component in both the first and second bracketed terms depends on the estimated values of $\tau_{\mu,1} = 0.105$ and $\tau_{\mu,2} = -0.003$, which indicate that $\gamma(\cdot)$ is decreasing and convex in one's study type, μ_s . In turn, the value of one's study type, μ_s , is determined by the cost function parameters ω_s . As seen at the end of Table 6, study type is increasing in high school GPA and high school study time, but is smaller for males.²⁴

To provide a better sense of the total effect of peer study effort in the best response functions, Figure 1 plots best response functions for several effective study types, $\widehat{\gamma}(\widehat{\mu}_s)$: the lowest (lower dotted green line), 25th percentile (lower dashed purple line), median (dot-dashed red line), and 75th percentile (higher dashed purple line), and the highest (higher dotted green line). The table just below Figure 1 calculates equation (33) for each of these effective study types, presenting the type-specific intercept (i.e., the first bracketed term in equation (33)) in the top row and the coefficient on friend study time (i.e., the second bracketed term in equation (33)) in the bottom row. The first row shows that there is little heterogeneity in the intercepts of best response functions. The second row shows that

²³See Blume et al. (2015) for an extensive discussion of linear social interactions models. We have verified that (the row-normalized) A_t are not idempotent, facilitating estimation of linear best response functions.

²⁴Though black students study considerably more than nonblack students, the coefficient on being black is negative. Black students have much higher high school study levels, which we find to be an important determinant of study type.

reactiveness to peer study time is increasing in effective study type. It is important to note that, even for the lowest effective study type (lower dotted green line, or first column of the table), the effect of peer study time is positive. Combining the slope and intercept terms, one’s optimal study choice is increasing in study type. That is, the best response is always increasing in s_{-it} and is often substantial.²⁵

To get a sense of whether the estimated heterogeneity in reactivity is significant, in Table 7 we present 95% confidence intervals for differences in best response slopes for different groups of students. Females have significantly steeper best response functions than males, students with above-median high school GPAs have significantly steeper best response functions than those with below-median high school GPAs, and students with above-median high school study time have significantly steeper best response functions than those with below-median high school study time.

Table 7: Means and 95% confidence intervals for difference in slope of best response function, by group

Comparison	Mean	2.5%	97.5%
Female-Male	0.058	0.015	0.115
Black-Nonblack	0.014	-0.013	0.044
High HS GPA-Low HS GPA	0.034	0.015	0.056
High Study HS-Low Study HS	0.177	0.077	0.299

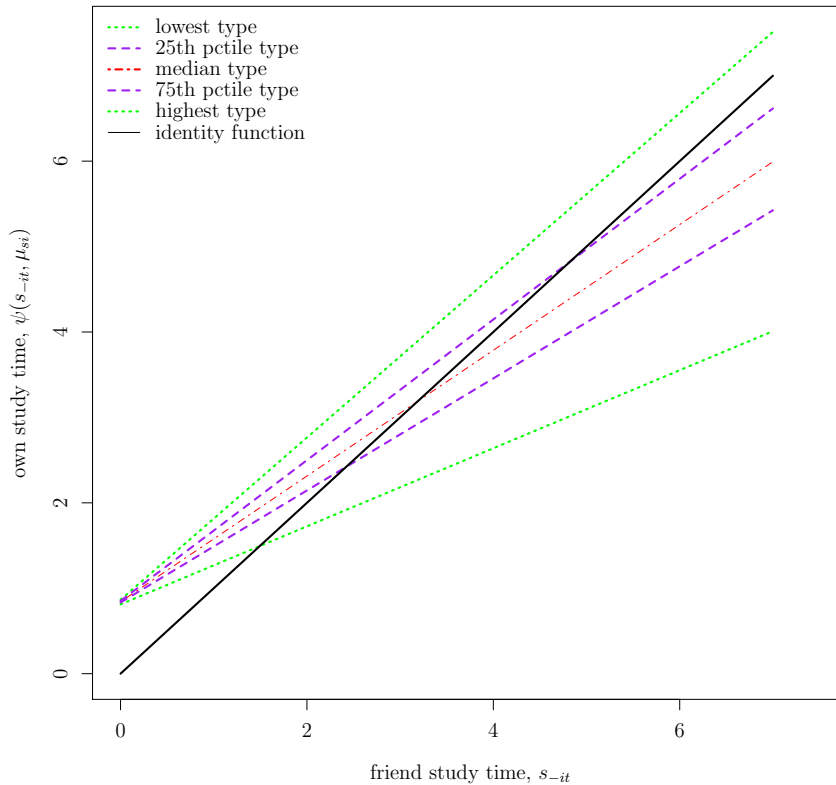
“High-” and “Low HS GPA” respectively refer to above- and below-median high school GPA. “High-” and “Low Study HS” respectively refer to above- and below-median high school study time.

In addition to describing individual heterogeneity in best response functions, Figure 1 provides evidence about the implications of this heterogeneity. To see this, note that the intersection of each best response function with the identity function indicates the equilibrium study outcome in a hypothetical scenario in which a student and someone of the same effective study type were paired. Therefore, by comparing where the different types’ best response functions intersect the identity function (solid black line), we can identify equilibria when each student is matched with someone of her respective study type. When two 75th percentile effective study types are paired they would study almost 5 hours each, almost twice the amount two 25th percentile types would study when paired. Our estimates indicate that the game exhibits a complementarity. If matched by study type, students may study more in total, and therefore, have higher total achievement. However, whether students will take advantage of this complementarity depends on how they sort into friendships.

Figure 2 shows that the model closely fits mean observed study time (left panel) and GPA

²⁵As noted in Section 5, we did not need to impose that best response functions are increasing in estimation.

Figure 1: Estimated study best response functions for different effective study types $\hat{\gamma}(\hat{\mu}_s)$



Effective study type $\hat{\gamma}(\hat{\mu}_s)$:	Lowest	25th pctile	Median	75th pctile	Highest
Intercept	0.81	0.83	0.84	0.85	0.87
Coefficient on s_{-it}	0.46	0.66	0.74	0.82	0.95

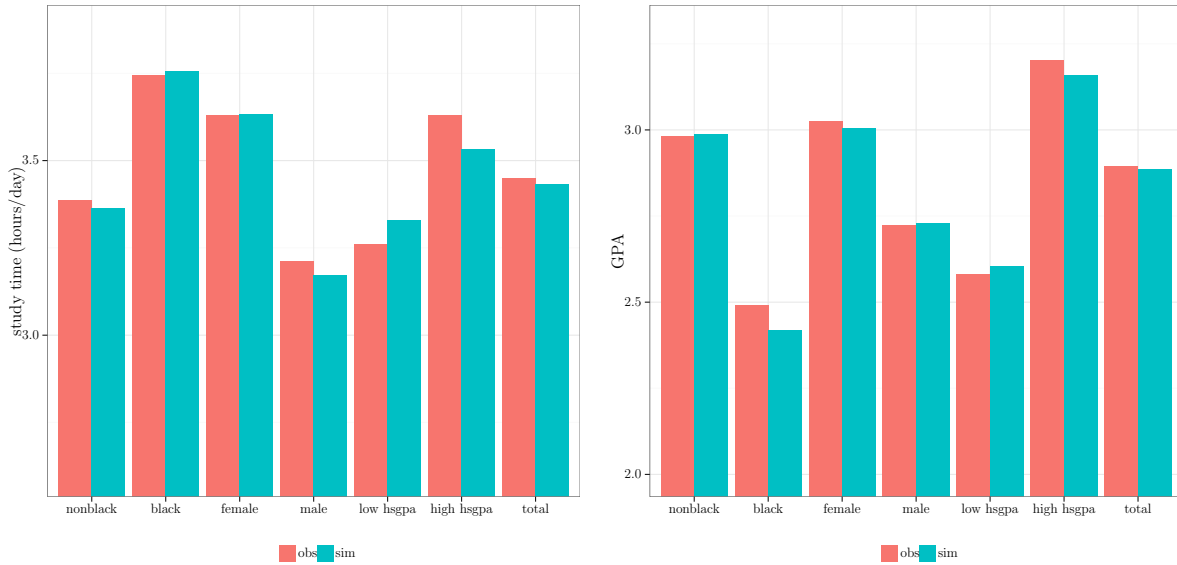
Note: Own and friend study times are measured in hours/day. Each column represents the estimated best response function for an effective study type. For example, the middle column indicates that the median effective study type has the estimated best response function $s_{it} = 0.84 + 0.74s_{-it}$.

(right panel), both in total and by student characteristics.²⁶ Even though the relationship between own and friend study time is not explicitly targeted (i.e., friend study time outcomes do not enter the likelihood), the model also closely captures this relationship. Figure 3 plots own versus friend study time, for both the data (solid red line) and simulated outcomes (dashed blue line).

In the remainder of this section we discuss potential endogeneity problems, present the results from our specification test, and present evidence about the robustness of our estimates.

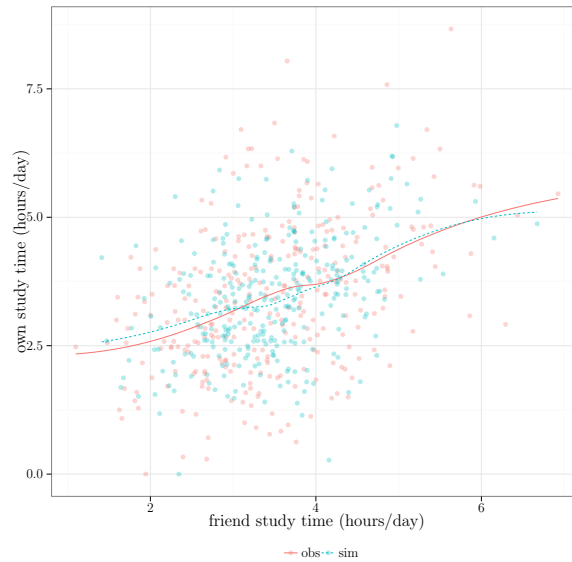
²⁶Model outcomes are simulated by first solving for equilibrium outcomes given $\hat{\Gamma}$ and then applying measurement errors, using the specification in Section 5.

Figure 2: Fit of mean study time (left) and GPA (right), by group



Note: “obs” are means computed using the data and “sim” are means of outcomes simulated from the model. “High-” and “Low HS GPA” respectively refer to above- and below-median high school GPA.

Figure 3: Fit of own study time against friend study time



Note: “obs” correspond to data and “sim” correspond to model simulations. Each point corresponds to a pair of own and friend study time (both are measured in hours/day). The lines are fitted values from a local quadratic regression. For each value of friend study time the fit is computed using the closest 75% of the observations via weighted least squares, with weights proportional to $(1 - (\text{distance}/\text{max. distance})^3)^3$. See `stat.smooth` in the R package `ggplot2` for details (Wickham (2009), R Core Team (2015)).

7.1 Endogeneity

Our primary endogeneity concerns arise from the potential for the relationship between a student’s study effort and that of her peers to be due, in part, to friendships being formed on the basis of potentially unobserved determinants of study time. One possible concern is that the relationship between own and friend study time is driven by institutional factors. One prominent example is that if students in science courses tend to study more and befriend students in their courses, there may be a spurious relationship between own and friend study time. We find that a version of the descriptive regression in Table 5, including both own and friend fraction of courses which are science, does not appreciably change the partial correlation between own and friend study time (0.166 vs. 0.160).²⁷ This is not surprising given that students may make friends outside their classes, the large majority of curriculum choices for freshman are required general or introductory classes, and there is not much variation in the number of classes taken.²⁸ In the same vein, dormitories are not specialized at Berea (e.g., there are not “study” dormitories or separate dormitories for student athletes).

Perhaps a more important concern is that students arrive at school with differing propensities to study, which affects how they sort into friendships. We address this concern by taking advantage of our survey collection to obtain direct measures of students’ propensities to study. Our baseline survey elicited information about: 1) how much a student expected to study in college and 2) how much a student studied in high school. As we discussed in Section 3.2, these measures of the propensity to study clearly have content, as they are strongly correlated with how much a student studies. We stress a crucial feature of this information on study propensity is that our survey design allowed this information to be collected immediately after students arrived on campus, before students could be influenced by their friendships at Berea.

As is always the case, it is difficult to know *a priori* whether observable characteristics can address potential endogeneity concerns. Therefore, we next present results from our specification test, which was designed to detect a wide variety of unobserved determinants of study time, in particular, those underlying endogeneity concerns.

7.2 Specification Test Results

To simplify exposition, in Section 6 we developed our specification test for one period and one study time report. This section starts by showing how we implement the test using our data for two periods (semesters) and multiple study time reports. Recall that predicted

²⁷See Table 13 in the appendix.

²⁸On average, students take about one additional course in their area of specialization per semester in their freshman year.

equilibrium study time for student i in semester t is $\delta_i^s(A_t, X; \hat{\Gamma})$.²⁹ We define i 's semester- t study time residual as the average residual over i 's semester- t study time reports, \tilde{s}_{rit} :

$$\hat{\eta}_{sit} \equiv \frac{1}{\sum_{r \in R_{it}} 1} \sum_{r \in R_{it}} \left(\tilde{s}_{rit} - \delta_i^s(A_t, X; \hat{\Gamma}) \right) = \tilde{s}_{it} - \delta_i^s(A_t, X; \hat{\Gamma}), \quad (34)$$

where \tilde{s}_{it} is i 's average study time over reports r in semester t . To implement the test, we average student's residuals over both semesters, i.e., $\hat{\eta}_{si} = \frac{\hat{\eta}_{si1} + \hat{\eta}_{si2}}{2}$. We then compute the average of friends' average residuals for each student in each semester according to $\hat{\eta}_{s,-it} = \frac{\sum_{j=1}^N A_t(i,j) \hat{\eta}_{sj}}{\sum_{j=1}^N A_t(i,j)}$.

Our test statistic is the t-statistic for a test of zero slope in a regression of $\hat{\eta}_{si}$ on $\hat{\eta}_{s,-it}$, pooled across semesters. Under the baseline specification, in which our new measures of study propensity (high school study time and expected study time) enter students' study types, our test statistic has a p-value of 0.716, corresponding to a correlation between own and friend study time residuals of 0.017.³⁰ Thus, our test results suggest that our model is well-specified. There is no evidence of an endogeneity problem arising from students positively sorting into friendships based on unobserved determinants of study time.

In the presence of an omitted characteristic that generates an endogeneity problem, our test should indicate a positive relationship in own and friends' residuals. To demonstrate that our test can detect a relationship in such a scenario, we construct an example where there is likely an endogeneity problem, by estimating a restricted version of our model in which we purposefully omit our novel measures of study propensity. Notably, this restricted specification uses only measures of student characteristics that are typically available to researchers. Because our empirical results show that these measures are both determinants of study time and also related to our measures of incoming human capital and friendship choices, their omission should generate a correlation across friends' residuals. The estimated correlation in this scenario is 0.208, and the test statistic for a slope coefficient of zero has a p-value of 1.12e-6, providing strong evidence against the null hypothesis of a slope of zero.

Taking these two residual correlations together, our test results suggest that our new measures of study propensity play a crucial role in addressing endogeneity concerns in our context.

Note that failing to reject the null model does not imply that we perfectly predict observed student study effort. Rather, failing to reject the null hypothesis means there are not

²⁹To be consistent with our specification test, we also re-estimate $\hat{\Gamma}$ assuming there is no censoring in study time and then use this estimate to compute the test statistic. Given the very small number of observations that were censored, the estimated $\hat{\Gamma}$ (and corresponding test statistics) are virtually identical between the censored and non-censored versions. Details are available upon request.

³⁰We use a distribution approximation for this test that allows correlation within students.

significant determinants of study time that would introduce detectable correlations between own and friend residuals. For example, independently distributed reporting errors, e.g., of the type we assume in Section 5, would create a divergence between model and reported study time.

7.3 Human Capital Spillovers (“Contextual Effects”)

We have focused on a mechanism wherein friend study time may affect one’s own study time, which in turn may affect one’s achievement via a production function. An alternative mechanism often considered in the literature involves peer human capital directly entering the achievement production technology (“contextual effects”). For example, friends with high human capital may provide quick and reliable answers to questions, or may know more about specific course requirements.

As a starting point, we augment the GPA prediction regression in Table 5, which regressed own GPA on own characteristics and own study time, by adding friend characteristics. Consistent with the results shown in Table 5, own study time remains a significant predictor of own GPA. However, friend characteristics are not significant predictors of students’ own GPAs; adding friend characteristics increases the adjusted R^2 of the regression from 0.246 to 0.247.³¹

Given the literature’s interest in direct transmission of peer characteristics and our ability to separately identify them from endogenous social interactions, it is worthwhile to look beyond the prediction equation described above, and estimate a specification allowing for friend incoming human capital to directly affect one’s achievement, via the production function. To this end, we re-estimated the model, extending the technology (2) to allow for direct human capital spillovers:

$$y(s_{it}, \mu_{yi}) = \beta_1 + \beta_2 s_{it} + \beta_3 \mu_{y,-i,t} + \mu_{yi}, \quad (35)$$

where $\mu_{y,-i,t} \equiv \frac{\sum_{j=1}^N A_t(i,j) \mu_{yj}}{\sum_{j=1}^N A_t(i,j)}$, i.e., the average of period- t -friend human capital types. A human capital spillover in the production of student achievement would correspond to $\beta_3 \neq 0$. As discussed in detail in Appendix C.1, we fail to reject that β_3 is zero, with a point estimate of $\hat{\beta}_3 = 0.111$ that has an accompanying standard error of 0.128. Based on a likelihood-ratio test, we would not reject the baseline model for that with contextual effects at any conventional significance level (the likelihood ratio test statistic has a p-value of 0.548).

Because we have data on both inputs and outcomes, there is more than one place in

³¹For example, the partial correlation coefficients for friend high school GPA, friend combined ACT score, and friend high school study have t-statistics of 0.75, .286, and -0.5, respectively.

which contextual effects could enter our model. We chose the above extension instead of, say, including a direct effect of friend characteristics in the cost function (3), because the results from our specification test do not provide strong evidence of omitted characteristics in the determination of study time choices. These results lead us to conclude that mechanisms involving a direct role of friends' incoming human capital are not motivated in our application.

7.4 Production Complementarities

As we show in Appendix B.3.2, our data on (study time) inputs and (achievement) outcomes allow us to separately identify production complementarities from cost-based mechanisms. Therefore, we check for evidence of production complementarities in own and friend study time, by adding an interaction of own and friend study time to the GPA prediction regression in Table 5. We find that the estimated interaction between own and friend study time is insignificant and very small, with a partial correlation coefficient of 0.005 and standard error of 0.01.

7.5 Dynamic Behavior and Model Validation

We discussed in Section 4.2.3 why it seemed reasonable to assume that the human capital type μ_{yi} was constant across semesters. In principle, however, first-semester achievement could increase students' human capital coming into the second semester, in which case, a model estimated using first-semester data may have difficulty fitting second-semester outcomes. On the other hand, if the out-of-sample fit turned out to be good, this would suggest a limit to the potential improvement in model fit from the addition of first-semester human capital or other dynamic considerations. Indeed, such an exercise could also be useful in discerning, more generally, whether the assumed micro-structure of our model (e.g., functional form assumptions, etc.) does a reasonably good job of capturing the key moving parts in our context.

Based on the above reasoning, we conducted an out-of-sample validation exercise by re-estimating our model using only data from the first semester and seeing how well it fit second-semester outcomes. As discussed in Appendix C.2, the second-semester fit is good. Therefore, we conclude that the static model may be appropriate for the relatively short time frame we consider in this paper.

8 Quantitative Findings

How much does it matter who your friends are? We use our estimated model to conduct two counterfactual exercises. First, we characterize how students respond to changes in friend study time by exogenously increasing (shocking) the study time of each student and measuring how outcomes would change for other students in the network. In addition to providing evidence about how network structure and student characteristics jointly determine how students are affected by their peers, this exercise provides a natural framework for quantifying the importance of equilibrium effects as well as the importance of heterogeneity in the effect of peers. Second, because peer effects are a function of not only how students respond to changes in peer inputs but also who is friends with whom, we examine how outcomes would differ if, instead of sorting into friendships as shown in Table 4, students were randomly assigned friends. This exercise provides a natural comparison point from which we can assess the importance of homophily in friendships.

Throughout this section, we compare outcomes between baseline and counterfactual scenarios for achievement, own study time, and friend study time. We use s_{it}^{cf} and s_{it}^{baseline} to denote student i 's study time in the counterfactual and baseline scenarios, respectively. We define the treatment effect on achievement for student i in period t as $\Delta_{it}^y \equiv y(s_{it}^{\text{cf}}, \mu_{yi}) - y(s_{it}^{\text{baseline}}, \mu_{yi})$. Treatment effects for own and friend study time are defined analogously.

8.1 Network Structure, Student Characteristics, and the Response to Peer Input Changes

To provide quantitative evidence about how students respond to changes in peer study time, we estimate the impulse response to an impulse of increasing study effort. Specifically, we increase (shock) the study time of a single student by one hour per day in a particular semester and examine the responses of all other students in the network in that semester. We summarize our findings when we perform this exercise 614 times (once for each of the 307 students in each of the two semesters).

The averages in the first row of Table 8 show how the mean effect of the study shock evaluated at the new equilibrium, i.e., taking into account the full set of feedback effects in the network, varies with a student's distance from the shocked student. For example, to obtain the number in the second column we first compute, for each student j in each of the two semesters t , the mean response in achievement for all students who are one link away from j when j is shocked in semester t . Averaging this mean response over all shocked students j and both semesters shows that students who are one link away from the shocked student have an average achievement gain of 0.078 GPA points. Similarly, the third, fourth,

and fifth columns, respectively, show that students who are two links, three links, and four links away from the shocked student, respectively, have average achievement gains of 0.022, 0.006, and 0.002 GPA points, respectively. The final column involves first computing, for each student j in each of the two semesters t , the *total* response in achievement, $\sum_{i \neq j} \Delta_{it}^y$, for all students (other than j) who are in the network when j is shocked in semester t . Averaging this total response over all students and semesters shows that, on average, the total effect of the shock is 0.52 GPA points.

Effects evaluated at the new equilibrium will be larger than partial equilibrium effects, which only take into account how the shock to a student influences students who are directly linked to her (i.e., iterating best response functions once). To quantify the importance of this difference, the second row of Table 8 shows the partial equilibrium effects. The average effect on students who are one link away from the shocked student is about 1/4 smaller under partial equilibrium than when than under the new equilibrium (0.059 vs. 0.078 GPA points), while, by definition, the effect on the (typically) large number of students who are two or more links away from the shocked student is zero in the partial equilibrium case. The last column shows that, on average, the total response of the shock is only 0.19 GPA points. Therefore, if we considered only partial equilibrium effects we would, on average, understate the achievement response by 64%.

Table 8: Average change in achievement (GPA points)

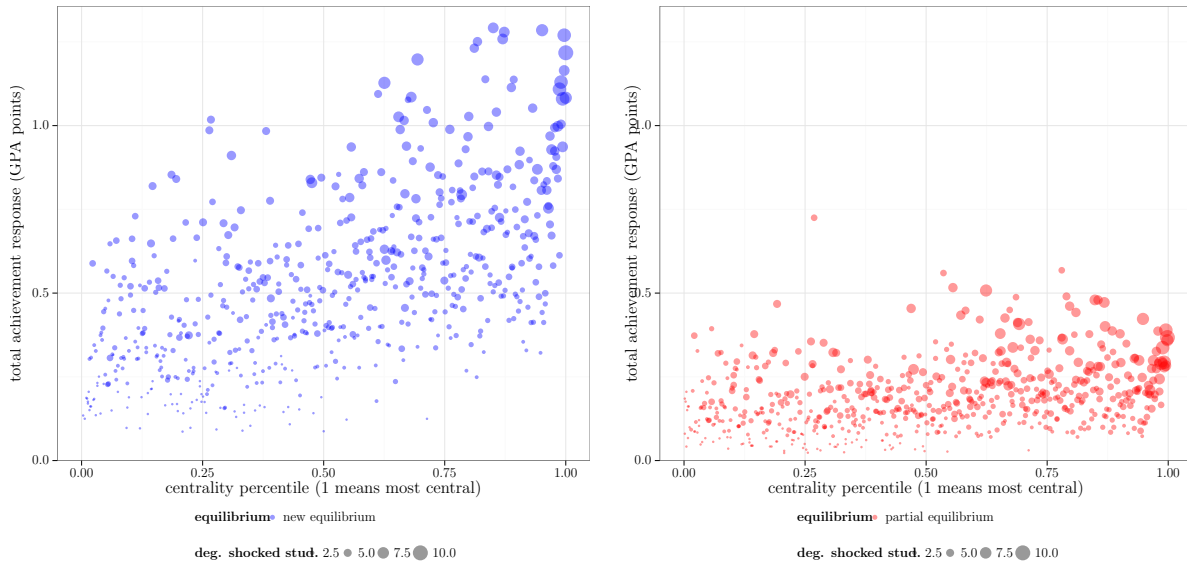
Dist. from shocked stud.:	Avg. response, by distance from shocked node					Total response
	0	1	2	3	4	
New equilibrium	0.254	0.078	0.022	0.006	0.002	0.52
Partial equilibrium	0.254	0.059	0.000	0.000	0.000	0.19

Note: The top row presents the mean effect on achievement (averaging over shocked students and semesters) at the new equilibrium, by distance from shocked student, where the shocked student has distance 0. The bottom row presents the mean effect on GPA immediately due to the impulse, by distance from shocked student. The mean total response, in the last column, is the average GPA response to shocking students j over periods t , excluding the effect on the shocked student, i.e., $\frac{1}{\sum_{j,t} 1} \sum_{j,t} \left(\sum_{i \neq j} \Delta_{it}^y \right)$.

We next examine how much the total response $\sum_{i \neq j} \Delta_{it}^y$ varies, depending on which student j is shocked in t . We find that the total response in achievement varies substantially depending on which student is shocked. For example, the first quartile, median, and third quartile of the total increase in achievement at the new equilibrium are 0.33, 0.49, and 0.66 GPA points, respectively. To get a better sense of why shocking different students can produce such different gains, the left panel of Figure 4 shows the relationship between the centrality of the shocked student and the total response at the new equilibrium.³² As

³²We use what is called a “closeness” centrality measure, given by the reciprocal of the sum of short-

Figure 4: Total achievement response (GPA points), by centrality of shocked student



Note: The vertical location of each dot represents the total achievement response to shocking a different student; the left panel presents the total gain at the new equilibrium and the right panel presents the partial equilibrium total gain. The x-axis indicates the shocked student’s centrality to other students and dot size denotes the degree of the shocked student.

before, this calculation excludes the mechanical gain in achievement experienced by the shocked student. Each dot records the total achievement response (y-axis) by the percentile centrality that semester, i.e., by how central the shocked student is (x-axis). The size of each (blue) dot shows the degree (i.e., number of friends) of the shocked student. Larger dots are concentrated at the top-right, and smaller ones at the bottom-left. That is, students with more friends tend to have higher centrality indices and larger achievement gains. Intuitively, because the effects of effort changes are stronger the closer students are, the total response is higher when the shocked student is more centrally located.³³ The right panel of Figure 4 plots partial equilibrium effects (red dots). We can see here that, though shocked students have the same degree (dot sizes), the average response is not as strongly increasing in centrality of the shocked student. This is the case because the equilibrium effects play a larger role the more densely connected the shocked student is to the rest of the network.

Figure 4 evinces variation in the total achievement response (i.e., the y-axis) to shocking different students who are similarly central (i.e., the x-axis) and who also have the same number of friends (i.e., dot sizes). We use two examples to illustrate how the structure of

est distances between that student and every other student in the graph. Average distance to others for unconnected students is set to the number of students (Csardi and Nepusz (2006), Freeman (1979)).

³³The notion that certain students may disproportionately affect other students is related to the concept of a “key player”, studied in Ballester et al. (2006).

the social network interacts with the distribution of best response functions to determine how changes in students' actions affect other students.

The left panel of Figure 5a shows the subgraph containing students within three degrees of the student whose shock creates the largest total achievement response (1.29 GPA points). The right panel shows the subgraph containing students within three degrees of the student whose shock creates the smallest total achievement response (0.087 GPA points). In each case, the shocked student is denoted by a red star. Squares represent males and circles represent females. Shapes corresponding to black students are shaded and those corresponding to nonblacks are unshaded. The area of the circle or square representing a student other than the shocked student is proportional to the slope of that student's best response function, where larger shapes correspond to more reactive students. Both subgraphs show homophilous sorting: black students tend to be friends with other black students (and nonblacks with nonblacks), males tend to be friends with males (and females with females). In general, students with steeper best response functions tend to be friends with each other.

Differences in the total response can be due to differences in link structure and how heterogeneous students are arranged on the network. The link structures of the subgraphs are very different. The shocked student in the left panel has more friends (6 vs. 1) and more students within three degrees (39 vs. 12).³⁴ In addition to the structure of links, how the heterogeneous students are arranged on the network matters. Although the average slope of best response functions is roughly similar between the subgraphs, 0.759 in the left vs. 0.698 in the right, the friends of the shocked student in the left panel have steeper best response functions than the friend of the shocked student in the right panel. In the right panel, the shock is immediately dampened by being passed through the student's only, relatively nonreactive friend.

Figure 5b shows the analogous plot, where the area of the shape is now proportional to the achievement gain for that student. The effect of the shock dies off in the same pattern illustrated by the first row of Table 8, that is, shapes further from the star tend to be smaller. Friends of the shocked student in the left subgraph gain much more than the friend of the shocked student in the right subgraph. Due to the much steeper best response functions of the shocked student's friends, the impulse dies out much less quickly in the left subgraph. Indeed, the gains for students who are two links from the shocked student in the left subgraph are about as large as the gain for the student directly connected to the shocked student in the right subgraph. This persistence comes from both the steeper best response functions of direct friends of the shocked student and the fact that many of them are also connected

³⁴We limit this illustration to students within three degrees based on the first row of Table 8, which shows the total impact dies off quite quickly in distance from the shocked student.

to each other, further augmenting the effects of the shock through feedback. This implies the effectiveness of policies targeting students may depend critically on how they fit into the arrangement of the social network.³⁵

8.2 The Effect of Sorting into Friendships

Section 8.1 studied how students respond to the input choices of others, taking into account the baseline network, which exhibits homophily. To directly examine homophily and, therefore, provide further evidence about the importance of peers, we compare achievement under the baseline social network with achievement under a counterfactual where friends are homogeneously distributed across students. In this counterfactual, for each semester, we maintain the marginal distribution of friends per student observed in the data, but replace reported links with random draws from the entire sample of students. We then form a counterfactual symmetrized A matrix in the same manner as it was formed for the actual data, as described in Section 3. Repeating this process 300 times for each of the two semesters produces 300 pairs of simulated adjacency matrices.³⁶

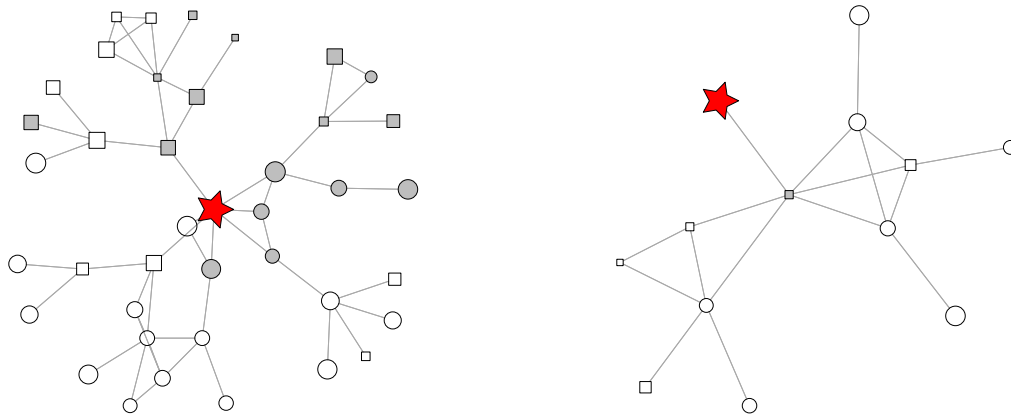
Table 9 summarizes changes in model outcomes between the baseline and counterfactual, averaged over all 300 simulated networks. Achievement is measured in GPA points and study times are in hours per day. The first column shows the average change in study time, across all students and all simulated networks, that results from moving to homogeneous (i.e., randomly assigned) friends. The first row shows that, on average, moving to this counterfactual would reduce own study time by 0.10 hours. Intuitively, students who in reality (i.e., under the baseline) have friends with high study types are most harmed by the move to a homogeneous distribution, which makes them much more likely to have lower study type friends. This explains why females, blacks, and students with above-median high school GPAs, who tend to be high study types and are seen in Table 4 to often have friends with high-study-type characteristics under the baseline, see own study time fall by 0.20, 0.25, and 0.15 hours, respectively. Conversely, males, who have less studious peers under the baseline, tend to study more when friends are homogenized. Importantly, the estimated complementarities, which arise due to the heterogeneity in best response functions combined with sorting into friendships based on effective study type, imply that the gains of lower study types are smaller than the losses of the higher study types. This explains the overall

³⁵See Fryer Jr (2011) for an example in which students are incentivized based on inputs to achievement.

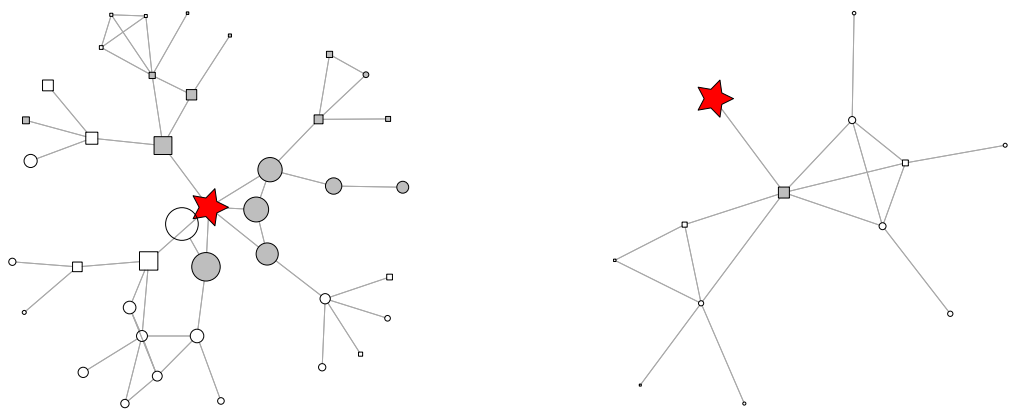
³⁶For example, in the first semester the algorithm starts with IID draws of counterfactual “friends per student” from the empirical marginal distribution of friends per student in A_1 , divided by two and rounded to the nearest integer, because A_1 has been union-symmetrized. The number of directed links per student is set to the student’s “friends per student” draw. Directed links are IID draws from the whole set of other students.

Figure 5: Subgraphs corresponding to students producing the largest and smallest total achievement responses

(a) Slope of best response functions for students within three degrees of the student producing largest total response when shocked (left) and smallest total response when shocked (right)



(b) Gain in achievement for students within three degrees of the student producing largest total response when shocked (left) and smallest total response when shocked (right)



Note: Red star indicates shocked student, males are square (females are circles), blacks are shaded (nonblacks are unshaded), and area of squares and circles is proportional to outcome of interest for corresponding students (i.e., (a) slope of best response function or (b) gain in achievement from shocking starred student)

decrease in own study time. Removing the sorting in the manner of our experiment does not merely re-allocate output, but also lowers total output. Accordingly, the standard deviation of own study time drops by 30%. A similar story drives both the overall results and the stratified results associated with changes in friend study time in the second column of Table 9.

The third column of Table 9 shows the average change in achievement across all students and all simulated networks that result from the changes in study time found in the first column. The first row shows that, on average, moving to the counterfactual would reduce achievement by 0.02 GPA points. However, as expected given the findings of study time, the declines are largest for black students, female students, and students with above-median high school GPAs. As before, the losses to these groups are not offset by the gains to other groups. Homogenizing the distribution of friends’ characteristics would increase the baseline GPA gap between nonblack and black students of 0.5 GPA points by 14%, reduce the baseline GPA gap between female and male students of 0.31 GPA points by almost 20%, and reduce the baseline GPA gap between students with above-median and below-median high school GPAs of 0.60 GPA points by 7%. Overall, homogenizing friends would reduce the standard deviation of achievement by 5%.

To gauge whether the effects reported above are significantly different from the baseline, we also report the range of the change in mean achievement, by group discussed above, across simulations. Figure 6 illustrates the 2.5th and 97.5th percentiles of the mean change for each group, along with the average mean changes presented in Col. (3) of Table 9. Intervals for black students, females, and students with above-median high school GPAs are all well below zero, as is the interval for the total change in achievement; only the group with below-median high school GPAs has an interval that contains zero. The significant effects indicated by these intervals reinforce our finding that sorting significantly affects student achievement.³⁷

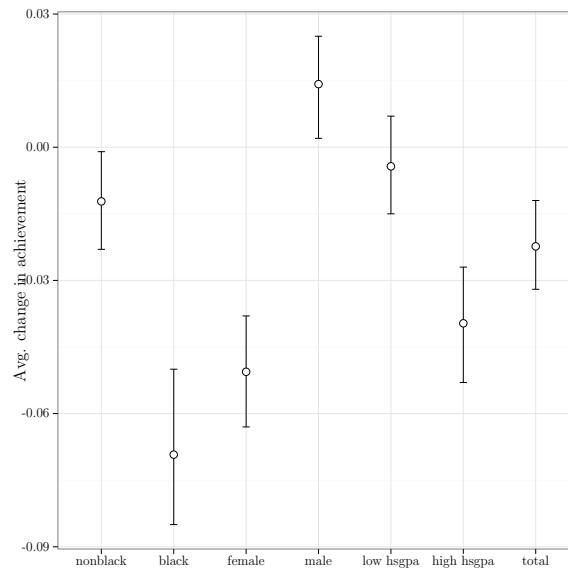
³⁷ We have also obtained results that incorporate the estimated uncertainty in our parameters. Even here, 95% confidence intervals for black students, females, and students with above-median high school GPAs are all below zero, as is the interval for the effect over all students (“total”), reinforcing the finding that sorting significantly affects student achievement. The reason that females and black students lose significantly more when friendships have been homogenized is that these groups have other characteristics associated with higher estimated study types (as do their friends). For example, Table 1 of the manuscript shows that females have high school GPAs that are, on average, over half a standard deviation higher than males, while having similar average high school study time. On average, black students have over 40% of a standard deviation higher high school study time than nonblack students.

Table 9: Average changes for study time (hours/day) and achievement (GPA points) resulting from counterfactual homogeneous distribution of friend characteristics, across simulated networks

	Own study time (1)	Friend study time (2)	Achievement (3)
Total	-0.10	-0.09	-0.02
Nonblack	-0.07	-0.04	-0.01
Black	-0.25	-0.36	-0.07
Female	-0.20	-0.25	-0.05
Male	0.05	0.12	0.01
Below-med. HS GPA	-0.03	0.02	0.00
Above-med. HS GPA	-0.15	-0.20	-0.04

Note: Means are computed over simulated networks.

Figure 6: Effect of homogenizing friends on average achievement (GPA points), across simulated networks



Note: The lower and upper ends of each bar respectively denote the 2.5th and 97.5th percentile of the mean change in achievement across all simulations, for the group indicated on the x-axis. The mean over all simulations for each group (presented in Col. (3) of Table 9) is denoted by a circle.

9 Conclusion

This paper presents an equilibrium model of student study time choices and the production of achievement. Social interactions are present because costs of study time for a student depend on the study times of that student's peers. We estimate this model and provide evidence that this mechanism is important in the production of academic achievement. Our approach was made possible by three key features of the BPS: direct measurements of study time, measurements of a social network for a cohort of Berea students, and measures of student propensities to study. We develop a specification test that can detect unobserved determinants of study time.

We use the structural model to examine counterfactuals that are informative about the role of network feedback effects and sorting in peer characteristics. Heterogeneity in student characteristics and how students are interconnected determine the distribution of responses to changes in a student's study time. Our results indicate that equilibrium effects, mediated by the whole social network, are quantitatively important in determining the responses of network-wide study time and achievement to shocks in study time. In addition, our results indicate that homophily, or sorting in peers' characteristics, plays an important role in the production of achievement. The results of our specification test suggest that our study propensity measures play a crucial role in addressing endogeneity concerns.

A Data

A.1 Survey questions

Figure 7: Time diary question

Survey #5 (Please complete both sides of this sheet) **CPO 1971** (3)

Question A.

Reminders: Be sure to put an arrow (→) next to the time that it is right now. And label this arrow with the words **YESTERDAY** and **START**.

Beginning with the **What were you doing** box next to the arrow, fill in your activities starting 24 hours ago (yesterday) and ending right before you began completing this survey.

Please use the 13 words listed in **BOLD** on the right of this page to describe your activities.

Time Period	What were you doing?	Time Period	What were you doing?
MORNING		EVENING	
6:00 AM		6:00 PM	
6:20 AM		6:20 PM	
6:40 AM		6:40 PM	
7:00 AM		7:00 PM	
7:20 AM		7:20 PM	
7:40 AM		7:40 PM	
8:00 AM		8:00 PM	
8:20 AM		8:20 PM	
8:40 AM		8:40 PM	
9:00 AM		9:00 PM	
9:20 AM		9:20 PM	
9:40 AM		9:40 PM	
10:00 AM		10:00 PM	
10:20 AM		10:20 PM	
10:40 AM		10:40 PM	
11:00 AM		11:00 PM	
11:20 AM		11:20 PM	
11:40 AM		11:40 PM	
AFTERNOON		NIGHT	
12:00 noon		12:00 midnight	
12:20 PM		12:20 AM	
12:40 PM		12:40 AM	
1:00 PM		1:00 AM	
1:20 PM		1:20 AM	
1:40 PM		1:40 AM	
2:00 PM		2:00 AM	
2:20 PM		2:20 AM	
2:40 PM		2:40 AM	
3:00 PM		3:00 AM	
3:20 PM		3:20 AM	
3:40 PM		3:40 AM	
4:00 PM		4:00 AM	
4:20 PM		4:20 AM	
4:40 PM		4:40 AM	
5:00 PM		5:00 AM	
5:20 PM		5:20 AM	
5:40 PM		5:40 AM	

LIST OF WORDS in bold

In Class

Attending class, attending labs, attending required class sessions

Studying (Outside of class time)

(refer to pg 2 for more details)

Athletics

(Intercollegiate or Intramural - games or practice)

Clubs

Exercising

Recreation

(reading which is unrelated to courses, listening to music, watching movie, spending time with friends, etc.)

Shopping

Eating

Sleeping

Partying

Personal

Working (in Labor position)

Other

(Please describe on your sheet)

Figure 8: Friends question

Question K. Please write down the **first and last names** of the four people that have been your best friends at Berea College during **this fall term (2001)**. That is, write down the names of the four people with whom you have been spending the most time during the fall term. Also please mention how many hours per week you spend with each person and how many hours you spend studying or talking about classes with each person. **Please include your boyfriend/girlfriend or husband/wife if they are among your four best friends. Also include your roommate if he/she is among your four best friends. Place a check next to the name of your boyfriend/girlfriend or husband/wife.**

Four best friends	Hours spent with this person in a typical week	Hours spent with this person studying /talking about classes in a typical week
1. _____	_____	_____
2. _____	_____	_____
3. _____	_____	_____
4. _____	_____	_____

Current Roommate: (Your roommate should be listed above also if he/she is one of four best friends.)

Question L. How would you describe your relationship with your roommate during **Fall term**? **Circle one.**

1. Good friends, spent a lot of time together.
2. Got along OK, but didn't spend much time together.
3. Didn't get along very well.
4. Had significant conflicts.
5. Did not have a roommate.

Question M. 1) Since the start of the fall term, did your father lose his job without being able to find a similarly paying replacement job? **Note:** Please answer NO if your father did not lose his job, lost his job but found a similarly paying new job, did not work at a job for pay, you do not know the status of your father, or your father is deceased.

Yes No Not applicable

2) Since the start of the fall term did your mother lose her job without being able to find a similarly paying replacement job? **Note:** Please refer to the **Note** in part 1) of this question.

Yes No Not applicable

Question N. Have you encountered any academic difficulties during the **fall term**? **Circle one.** Yes No

If you have encountered academic difficulties during the **fall term**, please circle the people that you discussed these problems with? Also indicate whether each circled item was helpful or not in providing encouragement.

- | | | |
|---|---------|-------------|
| 1. Parents | helpful | not helpful |
| 2. Family members other than parents | helpful | not helpful |
| 3. Friends at Berea | helpful | not helpful |
| 4. Friends not at Berea | helpful | not helpful |
| 5. Counselors, Advisers, or Teachers at Berea | helpful | not helpful |
| 6. Former high school or elementary teachers | helpful | not helpful |
| 7. Other (describe) _____ | helpful | not helpful |

B Additional Model Material

B.1 Concavity of Best Response Function

The optimal choice of study time for the period game solves the function $G(s, s_{-i}) = \frac{\partial c}{\partial s} - \beta_2 = 0$. To find how s varies with friend study time, use the Implicit Function Theorem:

$$\frac{\partial s}{\partial s_{-i}} = -\frac{\frac{\partial G}{\partial s_{-i}}}{\frac{\partial G}{\partial s}} = -\frac{\frac{\partial^2 c}{\partial s \partial s_{-i}}}{\frac{\partial^2 c}{\partial s^2}}.$$

If friend study time decreases the cost of increasing one's own study time, the numerator is positive. If the cost of studying is convex in own study time, the denominator is negative, meaning the overall sign is positive. Moreover, if friend study time enters $c(\cdot)$ in a weakly concave manner, e.g., $\tau_s \leq 1$, the numerator is weakly smaller in absolute value for larger values of s_{-i} , i.e., study time is weakly concave in friend study time.

B.2 Proof of Existence and Uniqueness of Equilibrium

Claim 2. *Let k be a number strictly greater than 24 . There exists a unique pure strategy Nash equilibrium if $\psi_i : R^N \mapsto R$ are weakly concave and weakly increasing, $\psi_i(0) > 0$, and $\psi_i(k) < k$ for $i \in N$.*

Proof. Define $\mathbf{S} = [0, k]^N$, i.e., a compact and convex set. Define a function Ψ :

$$\Psi : \mathbf{S} \mapsto \mathbf{S} = \begin{bmatrix} \psi_1(x_{-1}) \\ \psi_2(x_{-2}) \\ \vdots \\ \psi_N(x_{-N}) \end{bmatrix}.$$

Existence: $\Psi(\cdot)$ is a continuous self map on the compact set \mathbf{S} , so an equilibrium exists by Brouwer's Fixed Point Theorem.

Uniqueness: If $\Psi(\cdot)$ is strictly concave and weakly increasing we can apply Kennan (2001). Next, consider the case where $\Psi(\cdot)$ is linear, in which case we can prove $\Psi(\cdot)$ is a contraction. Write the linear form of $\Psi(\cdot)$ as

$$\Psi(X) = \begin{bmatrix} \alpha_{11} + \alpha_{21}x_{-1} \\ \alpha_{12} + \alpha_{22}x_{-2} \\ \vdots \\ \alpha_{1N} + \alpha_{2N}x_{-N} \end{bmatrix},$$

where, by assumption, $\max_{i \in N} \{\alpha_{2i}\} < 1$. Let distance be calculated according to the taxicab distance, i.e., $d(X_1, X_2) = \sum_{g \in N} |X_{1g} - X_{2g}|$ for $X_1, X_2 \in \mathbf{S}$. The Contraction Mapping Theorem holds if $d(\Psi(X_1), \Psi(X_2)) \leq bd(X_1, X_2)$, for $b \in (0, 1)$. Calculating this for the special case where Ψ is a linear map, we have

$$d(\Psi(X_1), \Psi(X_2)) = \sum_{i \in N} \alpha_{2i} |X_1 - X_2| \leq \max_{i \in N} \{\alpha_{2i}\} |X_1 - X_2| < d(X_1, X_2),$$

i.e., the condition for the Contraction Mapping Theorem is satisfied, where $b = \max_{i \in N} \{\alpha_{2i}\} \in (0, 1)$. \square

B.3 Other Mechanisms for Social Interactions

B.3.1 Conformity Specification of Cost Function

We refer the cost function specification in (3) as the “cost-reduction model”. Consider the alternative effort cost function, which we refer to as the “conformity model”:

$$c(s, s_{-i}, \mu_{si}) = (\delta_1 + \delta_2 \gamma(\mu_{si})) s + \frac{\delta_3}{2} s^2 + \frac{\delta_4}{2} (s - (1 + \delta_5 \gamma(\mu_{si})) s_{-i}^{\tau_s})^2. \quad (36)$$

Solving the student’s problem results in the best response function

$$s_i = \frac{\beta_2 - \delta_1}{\delta_3 + \delta_4} - \frac{\delta_2}{\delta_3 + \delta_4} \gamma(\mu_{si}) + \frac{\delta_4}{\delta_3 + \delta_4} s_{-i}^{\tau_s} + \frac{\delta_4 \delta_5}{\delta_3 + \delta_4} \gamma(\mu_{si}) s_{-i}^{\tau_s}. \quad (37)$$

If we make a similar normalization as was performed for the cost-reduction model, by setting $\delta_3 = 1$, we obtain

$$s_i = \underbrace{\frac{\beta_2 - \delta_1}{1 + \delta_4}}_{-\theta_3} + \underbrace{\frac{-\delta_2}{1 + \delta_4}}_{-\theta_4} \gamma(\mu_{si}) + \underbrace{\frac{\delta_4}{1 + \delta_4}}_{(\beta_2 - \theta_1)} s_{-i}^{\tau_s} + \underbrace{\frac{\delta_4 \delta_5}{1 + \delta_4}}_{-\theta_2} \gamma(\mu_{si}) s_{-i}^{\tau_s}. \quad (38)$$

That is, we can represent the parameters in equation (36) above in terms of parameters in (3), which are in braces beneath their counterparts in the conformity model in (38). Therefore, the distinction between the different formulations of the cost function—a cost of deviating from friend behavior vs. a cost (reduction) from studying with ones friends—has no empirical content.

What matters, then, is interpretation and intuition of the two cost specifications. The cost-reduction model captures the intuitive notion that friends studying more, i.e., a higher s_{-i} entering the denominator in the last three terms of equation (3), would reduce the cost of studying by making it more enjoyable. At the same time, it also makes intuitive sense that there would also be a private component to the cost of studying (the first two terms in

the expression). Note that τ_s also has an intuitive meaning in the cost-reduction model, as it represents the degree to which the utility gains from friends' studying diminish. If friends studying more reduces your marginal cost of studying because you enjoy spending time with them, then it would be natural to allow this benefit to decrease the more they study, i.e., $\tau_s < 1$.

Now consider the conformity model, first setting $\tau_s = 1$ and $\delta_5 = 0$. The interpretations of δ_1 and δ_2 are quite natural: students have private costs of studying, which may be heterogeneous. The interpretation of δ_4 is also quite natural: if positive, this creates a force inducing friends to behave similarly by conforming in their choice of study time.

Now consider $\tau_s < 1$ and assume $\delta_4 > 0$ (but maintain $\delta_5 = 0$). We believe the interpretation in this case for the conformity model is less clear than it is in the cost-reduction model. If $s > s_{-i}$ for a particular student then reducing τ_s would create a bigger cost of deviating. On the other hand, if $s < s_{-i}$ then reducing τ_s would decrease the cost of deviating. The interpretation of $\delta_5 \neq 0$ (maintain $\tau_s = 1$) is also slightly less clear, for similar reasons: The thing one is conforming to is not the same as one's choice: A student might choose to study four hours a day to "conform" to her friends who study five hours, not due to the private cost of studying. (Note that instead having the heterogeneous term outside the quadratic term (i.e., added to δ_4) would break the observational equivalence of the two cost functions.) Therefore, though in the homogeneous, linear model it does appear that conformity has a nice intuition, we believe the cost-reduction specification is a bit more intuitive when considering nonlinear and/or heterogeneous best response functions.

B.3.2 Production Complementarities

Suppose we did not have achievement data. For simplicity, consider the homogeneous, linear, best response specification (i.e., $\theta_2, \theta_4 = 0$); the following result also obtains in the more general specification of the cost function. Consider the following specification of our achievement equation:

$$y(s_{it}, \mu_{yi}) = \beta_1 + \beta_2 s_{it} + \beta_3 \frac{s_{it}}{s_{-it}} + \mu_{yi}, \quad (39)$$

where s_{it} is own study effort and s_{-it} is friend study effort. If $\beta_3 < 0$, then increases in peer effort increase the marginal product of one's own effort.³⁸ The student's problem would still

³⁸Note, one could instead have defined the production complementarity according to $\beta_3 s_{it} s_{-it}$, where $\beta_3 > 0$ would correspond to production complementarities. Though such a functional form would technically produce identification in the cost-reduction model we consider, it would not in the conformity model (where the interaction above, $\beta_3 s_{it}/s_{-it}$, for similar reasons, would produce identification via functional form).

be separable across periods, resulting in the best response function

$$s_{it} = (\beta_3 - \theta_3) + (\beta_2 - \theta_1)s_{-it}. \quad (40)$$

It is obvious from (40) that we cannot separately identify β_3 and θ_3 without having data on the marginal product of inputs (i.e., data on achievement outcomes). Indeed, this is the same argument that, without data on achievement, we could not identify the extent to which students study because it is enjoyable (θ_1) versus doing so because it affects their achievement (β_2). On the other hand, having both study time and achievement data would clearly allow one to identify the extent to which production complementarities underlie social interactions.

C Additional Estimation Results

C.1 Contextual Effects

This section presents the estimation results of our specification allowing for contextual effects in achievement, described in Section 7.3. Table 10 presents the baseline estimates (Col. (1)) and re-estimated parameters allowing for contextual effects (Col. (2)). We obtain a point estimate on the achievement contextual effect parameter of $\hat{\beta}_3 = 0.111$, which has a standard error of 0.128. That is, we cannot discern that contextual effects are different from zero, which is consistent with the similarity between the parameters estimated under the baseline (Col. (1)) and under the augmented technology (Col. (2)). Moreover, based on a likelihood-ratio test, we would not reject the baseline model for that with contextual effects at any conventional significance level (the likelihood ratio test statistic has a p-value of 0.548). Because we find a negligible effect of direct human capital spillovers, we have retained our baseline specification for the exposition of our results.

C.2 Out-of-Sample Validation

Table 11 presents the baseline parameter estimates (Col. (1)) and those obtained when using only first-semester data (Col. (2)). The sets of parameters are strikingly similar between the two columns; this is confirmed by their having very similar (first-semester-only) log likelihoods, which are presented at the bottom of each column. This suggests that the out-of-sample fit of second-semester outcomes may be reasonable when based on parameters estimated using only first-semester data.

To further investigate, we compare model fit for the first-semester data, which was used

Table 10: Parameters Under Baseline and Contextual Effects Specifications

	Baseline (1)	Contextual (2)
β_1	-0.350	-0.591
β_2	0.254	0.258
β_3	—	0.111
$\omega_{y,HS\ GPA}$	0.470	0.462
$\omega_{y,ACT}$	0.047	0.046
$\omega_{y,Black}$	-0.213	-0.182
$\omega_{y,Male}$	-0.037	-0.021
$\omega_{y,HS\ study}$	-0.007	-0.007
$\omega_{y,expected\ study}$	-0.005	-0.005
$\omega_{s,HS\ GPA}^*$	1.000	1.000
$\omega_{s,ACT}$	-0.063	-0.065
$\omega_{s,Black}$	-0.735	-0.720
$\omega_{s,Male}$	-1.065	-1.081
$\omega_{s,HS\ study}$	0.344	0.347
$\omega_{s,expected\ study}$	0.005	0.004
σ_η	2.159	2.159
σ_ϵ	0.721	0.721
τ_s^{**}	1.000	1.000
$\tau_{\mu,1}$	0.105	0.105
$\tau_{\mu,2}$	-0.003	-0.003
θ_1	-1.074	-1.068
θ_2	0.874	0.870
θ_3	-0.907	-0.918
θ_4	0.096	0.098
Log Likelihood:	-4696.36101	-4696.18025
LLR stat:		0.362
p-value:		0.548

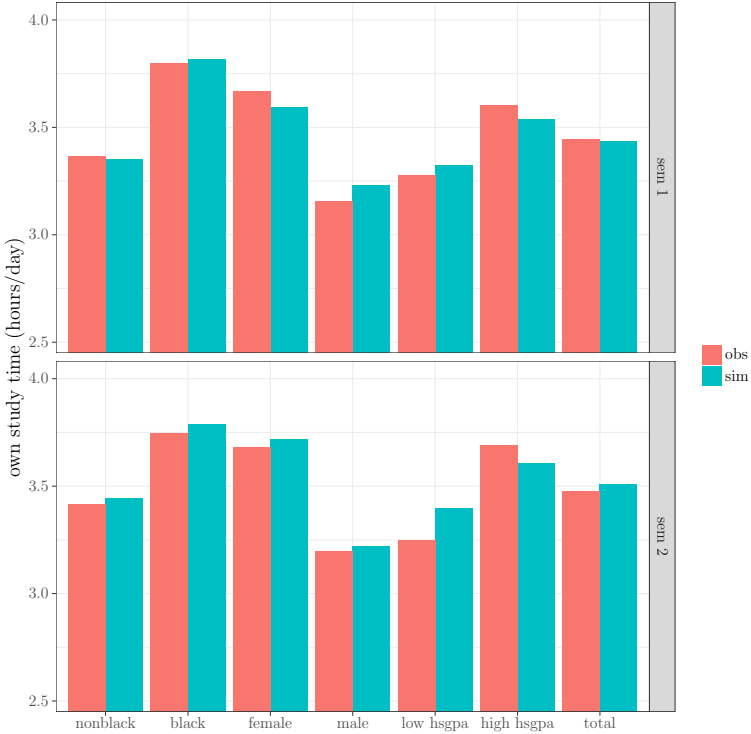
Note: *: Normalized to 1. **: Fixed to 1. Col. (1) presents estimates from baseline model, when achievement is defined according to (2). Col. (2) presents results allowing for contextual effects in achievement, where achievement is defined according to (35).

Table 11: Parameters Under Baseline and Only-First-Semester Data

	Baseline (1)	Only First Semester (2)
β_1	-0.350	-0.154
β_2	0.254	0.230
$\omega_{y,HS\ GPA}$	0.470	0.400
$\omega_{y,ACT}$	0.047	0.053
$\omega_{y,Black}$	-0.213	-0.278
$\omega_{y,Male}$	-0.037	-0.035
$\omega_{y,HS\ study}$	-0.007	-0.009
$\omega_{y,expected\ study}$	-0.005	-0.005
$\omega_{s,HS\ GPA}^*$	1.000	1.000
$\omega_{s,ACT}$	-0.063	-0.121
$\omega_{s,Black}$	-0.735	-0.765
$\omega_{s,Male}$	-1.065	-0.873
$\omega_{s,HS\ study}$	0.344	0.271
$\omega_{s,expected\ study}$	0.005	0.000
σ_η	2.159	2.203
σ_ϵ	0.721	0.709
τ_s^{**}	1.000	1.000
$\tau_{\mu,1}$	0.105	0.127
$\tau_{\mu,2}$	-0.003	-0.005
θ_1	-1.074	-1.103
θ_2	0.874	0.848
θ_3	-0.907	-1.138
θ_4	0.096	0.144
Log Likelihood: (first-semester)	-2375.58255	-2373.61342

Note: *: Normalized to 1. **: Fixed to 1. Col. (1) presents estimates from baseline model and the log likelihood in the first semester. Col. (2) presents results when parameters were estimated using only first-semester data and the log likelihood in the first semester.

Figure 9: In and-Out-of-sample fit; study time



to estimate model parameters, and the validation data from the second semester. We can see that the out-of-sample fit for study time (Figure 9), GPA (Figure 10), and own-vs.-friend study time (Figure 11) all seem quite good.

D Additional Tables

Figure 10: In- and-Out-of-sample fit; GPA

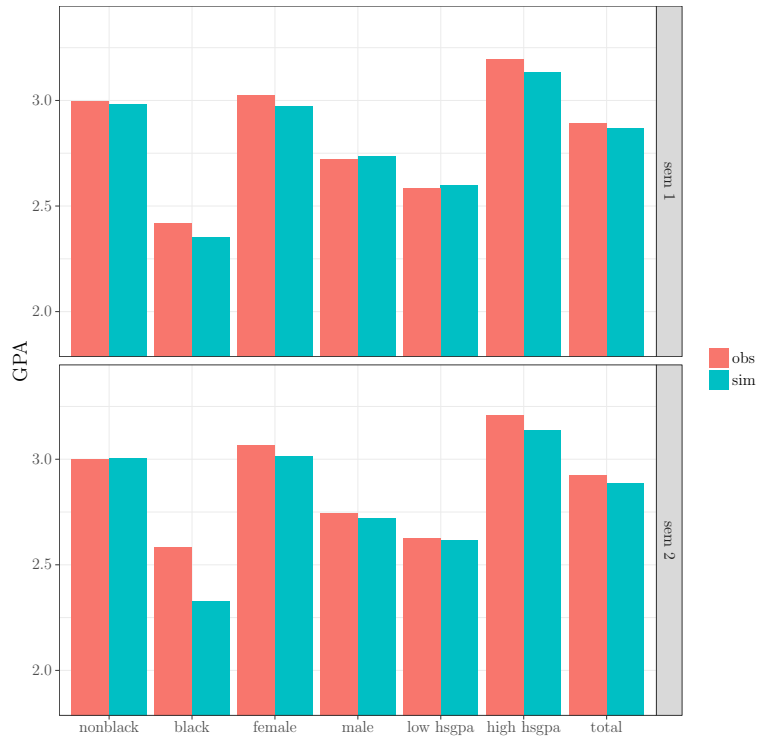


Figure 11: In- and-Out-of-sample fit; own vs. friend study time

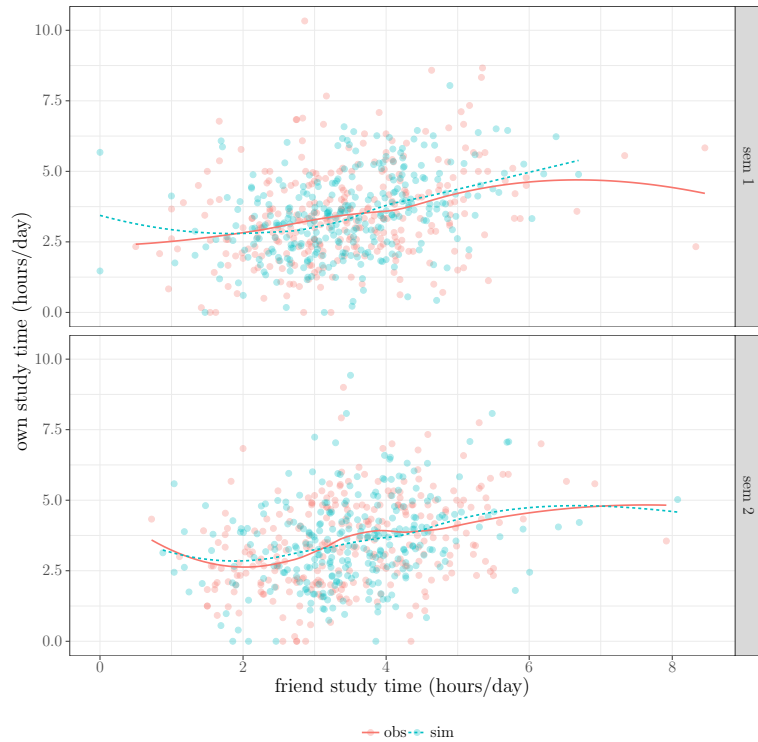


Table 12: Study time regressions controlling for different sets of characteristics, pooled over both semesters

	<i>Dependent variable: Own study</i>			
	(1)	(2)	(3)	(4)
Male	-0.369*** (0.136)	-0.328** (0.140)	-0.391*** (0.135)	
Black	0.116 (0.186)	0.333* (0.192)	0.324* (0.172)	
HS GPA	0.413*** (0.149)	0.392** (0.156)		
ACT	-0.032 (0.021)	-0.029 (0.022)		
HS study	0.043*** (0.006)			
Expected study	-0.002 (0.006)			
Friends study	0.166*** (0.037)	0.198*** (0.039)	0.202*** (0.039)	0.228*** (0.038)
Constant	1.915*** (0.671)	2.167*** (0.679)	2.850*** (0.172)	2.648*** (0.152)
Observations	574	574	574	574
R ²	0.169	0.087	0.076	0.058

Note: *p<0.1; **p<0.05; ***p<0.01 GPA is measured in GPA points (0-4). HS study and expected study are measured in hours/week. Own and friend study are measured in hours/day. The variable “Friend z ” for student i in period t is the average of the variable z across i 's friends in period t .

E Dyadic, Separate Networks with Homogeneous Best Responses

To make the test statistic more concrete, in this section we develop an example environment with dyadic, separate networks with homogeneous best responses.

Table 13: Study time regressions, pooled over both semesters

	<i>Dependent variable: Own study</i>	
	(1)	(2)
Male	-0.369*** (0.136)	-0.365*** (0.137)
Black	0.116 (0.186)	0.115 (0.187)
HS GPA	0.413*** (0.149)	0.389*** (0.150)
ACT	-0.032 (0.021)	-0.034 (0.021)
HS study	0.043*** (0.006)	0.041*** (0.006)
Expected study	-0.002 (0.006)	-0.002 (0.006)
Own share science courses		0.349 (0.390)
Friend study	0.166*** (0.037)	0.157*** (0.038)
Avg. friend share science courses		0.880 (0.562)
Constant	1.915*** (0.671)	1.873*** (0.684)
Observations	574	574
R ²	0.169	0.176

Note: *p<0.1; **p<0.05; ***p<0.01 GPA is measured in GPA points (0-4). Own and friend HS study and expected study are measured in hours/week. Own and friend study are measured in hours/day. The variable “Friend z ” for student i in period t is the average of the variable z across i 's friends in period t .

Example 1 (Dyadic, separate networks with homogeneous best responses). *Consider the following special case, with*

$$F_1(\Gamma_2) = X\lambda_1 \quad (41)$$

$$W_t(X; \Gamma_2) = W\lambda_2 \quad (42)$$

$$\Pi(X) = X\lambda_3, \quad (43)$$

where λ_1, λ_2 are scalars, λ_3 is a matrix of parameters, and $W = I_N \otimes I_2$ is a block diagonal matrix with I_2 (i.e., two-by-two Identity matrices) along the diagonal, representing the fact that each student is friends with exactly one other student. Then (31) would become

$$\tilde{\epsilon} \approx \{(I - W\tilde{\lambda}_2)^{-1}[X(\lambda_1 + \lambda_3)] - (I - W\tilde{\lambda}_2)^{-1}[X\hat{\lambda}_1]\} + (I - W\lambda_2)^{-1}u + \eta_s. \quad (44)$$

Note that $\text{plim } \hat{\lambda}_1 = (\lambda_1 + \lambda_3)$, i.e., there will be no prediction bias, meaning we are in Case (i) above. Because W is block diagonal, it is sufficient to consider the top-left 2×2 block, representing the first friendship dyad. The expression (44) for these students then, eliminating the η_s , which are independently distributed from all other variables and therefore qualitatively immaterial in the following calculation, is

$$\begin{bmatrix} \tilde{\epsilon}_1 \\ \tilde{\epsilon}_2 \end{bmatrix} \approx \frac{1}{1 - \lambda_2^2} \begin{bmatrix} 1 & \lambda_2 \\ \lambda_2 & 1 \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix} = \frac{1}{1 - \lambda_2^2} \begin{bmatrix} u_1 + \lambda_2 u_2 \\ \lambda_2 u_1 + u_2 \end{bmatrix}, \quad (45)$$

giving the product of residuals for students in the first dyad: $\left(\frac{1}{1 - \lambda_2^2}\right)^2 (\lambda_2 u_1^2 + (1 + \lambda_2^2)u_1 u_2 + \lambda_2 u_2^2)$. Under the maintained assumption that $\lambda \geq 0$, the expectation of this product can only be zero if $u_1 u_2 < 0$, i.e., own and friend errors u are negatively correlated, and in exactly the right way.

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