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Managing Risk Taking with Interest Rate Policy and Macroprudential Regulations^{*†}

Simona E. Cociuba Malik Shukayev Alexander Ueberfeldt

September, 2017

Abstract

We develop a model in which a financial intermediary's investment in risky assets—*risk taking*—is excessive due to limited liability and deposit insurance, and characterize the policies that implement efficient risk taking. In the calibrated model, combining interest rate policy with state-contingent macroprudential regulations—either capital or leverage regulation, and a tax on profits—achieves efficiency. Interest rate policy mitigates excessive risk taking by altering the return and the supply of collateralizable safe assets. In contrast to commonly-used capital regulation, leverage regulation has stronger effects on risk taking and calls for higher interest rates.

Keywords: *Financial intermediation, risk taking, interest rate policy, macroprudential regulations, capital requirements, leverage ratio.* **JEL-Code:** *E44, E52, G11, G18.*

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1 Introduction

In the aftermath of the recent financial crisis, many countries adopted a new financial regulatory framework—known as Basel III—which increased capital requirements, allowed them to vary over the business cycle and complemented them with a leverage ratio (Basel Committee on Banking Supervision (2011)).¹ These changes were aimed at strengthening capital regulation and improving the management of financial sector risks. In this paper, we evaluate the efficiency and the welfare implications of such policies.

We develop a model in which financial intermediaries’ investments in risky assets—*risk taking*—may exceed the social optimum due to limited liability and deposit insurance. Risk taking over the business cycle is influenced by monetary policy and macroprudential policies, namely financial regulations on capital or leverage, and profit taxes.² Our main contribution is to show that the macroprudential policies needed to eliminate excessive risk taking are countercyclical: they alleviate the moral hazard of intermediaries during expansions, while being more lenient in recessions. Moreover, the optimal policies are interdependent. Monetary policy rates are higher in the presence of leverage regulation compared to capital regulation. And, there is a trade-off between profit taxes and financial regulations: incorporating taxes in the macroprudential policy toolkit allows for looser financial regulations.³

Our theoretical framework enriches the dynamic general equilibrium model with aggregate and idiosyncratic uncertainty in Cociuba, Shukayev, and Ueberfeldt (2016) (henceforth, CSU) to allow for capital and leverage regulations, and a tax on financial intermediaries’ profits. We examine how these macroprudential policies impact intermediaries’ investments into

¹Regulatory capital was raised from 8 percent of risk-weighted assets under Basel II to 10.5 percent under Basel III. A countercyclical buffer in the range of 0 – 2.5 percent may be imposed at the discretion of national authorities if excessive credit growth is judged to lead to a buildup of risk and potential future losses. Lastly, Basel III introduced a “a simple, non-risk based” leverage ratio which doesn’t vary over time.

²Evidence on the effectiveness of macroprudential policies is limited. Damar and Molico (2016), Cerutti, Claessens, and Laeven (2015) and Lim, Columba, Costa, Kongsamut, Otani, Saiyid, Wezel, and Wu (2011) provide cross-country overviews of macroprudential policies (cyclical vs. structural, fixed vs. time-varying, broad-based vs. sectoral) and conclude that they help mitigate financial sector risks.

³Taxation of financial institutions to help finance the cost of financial crises has been suggested by International Monetary Fund (2010). The macroprudential role of taxes is also analyzed in Jeanne and Korinek (2013), Bianchi and Mendoza (2013) and Keister (2016).

safe bonds and risky projects. The latter are investments in the production technologies of firms and can be of two types: high-risk and low-risk projects. High-risk projects are more productive during good aggregate states and less productive during bad aggregate states compared to low-risk projects. In this environment, we define risk taking as excessive if investments in high-risk projects exceed the social optimum.

Each period, intermediaries make two portfolio choices. At the first portfolio decision, aggregate productivity and the idiosyncratic type of intermediaries' risky projects are unknown, and investments are subject to financial regulations. At the second portfolio decision, aggregate productivity is still unknown, but the type of risky projects is revealed, and intermediaries use bonds as collateral in an interbank market to adjust the scale of these projects. The rationale for modeling collateralized interbank borrowing is the empirical observation that intermediaries borrow in the sale and repurchase market (i.e., the *repo market*) to alter their portfolio risk (Adrian and Shin (2010)). During an expansion, when aggregate productivity is expected to be high, intermediaries with high-risk projects (i.e., *high-risk intermediaries*) trade bonds to invest more in these projects. These projects are attractive from a social point of view due to high expected returns, and are attractive for intermediaries because potential losses in the event of a contraction are avoided through limited liability (as in Allen and Gale (2000)). Low-risk intermediaries on the other side of the transaction accept bonds and reduce exposure to their risky projects with lower expected returns.

An important feature of our model is that interbank market transactions are not subject to financial regulations. The interpretation is that intermediaries comply with regulations at the first portfolio decision, which coincides with the quarterly public reporting of balance sheets. Between reporting periods, regulatory arbitrage allows intermediaries to increase risky investments and disregard regulations.⁴ This modeling choice is motivated by evidence that repo transactions are used by banks to temporarily “appear safer and less levered”

⁴The first working paper of the Basel Committee on Banking Supervision, Jackson et al. (1999), evaluates the impact of Basel I and discusses the ability of banks to reduce their capital charges via regulatory arbitrage. Kashyap, Stein, and Hanson (2010) review more recent capital arbitrage strategies.

before quarterly public disclosure periods (Munyan (2015)).^{5,6} Although interbank market transactions in our model are unregulated, they are constrained by the amount of collateral bonds chosen at the first portfolio decision, which is subject to financial regulations.

In our framework, a consolidated monetary and financial authority optimally chooses interest rate policy, capital or leverage regulation, and taxes on intermediaries' profits to maximize household welfare. Thus, optimal policies are interdependent. The interest rate policy alters the bond return, and profit taxes alter the return on intermediaries' equity. Capital regulation imposes a lower bound on intermediaries' equity to risky investment ratio, while leverage regulation imposes an upper bound on intermediaries' total assets to equity ratio. Moreover, all policies are allowed to vary over time. The state-contingent nature of our model's regulatory capital is in line with Basel III, which introduces time-variation via countercyclical capital buffers. For symmetry, we allow our model's leverage regulation to be state-contingent, although Basel III calls for a fixed leverage ratio. Our paper focuses on time-variation in financial regulations and abstracts from risk weighting of capital.⁷

To illustrate the interdependence between policies, we examine a simplified version of our model with i.i.d. aggregate shocks, where we derive analytical results. Here, as in the full model, bankruptcy may occur if intermediaries do not pay the promised rate of return to depositors and use their limited liability to shield themselves from losses. We find that implementing the social optimum in a competitive equilibrium with bankruptcy requires

⁵Other examples of regulatory arbitrage from the recent financial crisis are: the use of Repo 105 by Lehman Brothers “for no articulate business purpose except to reduce balance sheet at the quarter-end” (Valukas (2010, vol. 1)), and the use of special purpose entities to allow banks to move assets off their balance sheets and reduce capital requirements (Acharya and Schnabl (2009)). Dubecq, Mojon, and Ragot (2015) model regulatory arbitrage as imperfect information about risk-weighted capital, to capture the idea that capital regulation is difficult to implement as it requires banks to evaluate their own risk exposures.

⁶Munyan (2015) suggests that capital requirements and the leverage ratio introduced in Basel III should be calculated based on averages of daily data, to disincentivize intermediaries from adjusting their balance sheets at quarter-end, and to improve the effectiveness of financial regulations. Current regulations use quarter-end observations for capital or an average of three month-end observations for leverage. In 2014, the U.S. passed Federal Register rule 79 FR 57725 to establish daily averaging for the leverage ratio effective 2018. However, given the “operational burden” of daily calculations, off-balance sheet exposures in the leverage ratio will still be computed as the average of three month-end observations.

⁷This modeling choice is motivated by Hellwig (2010), who argues for a thorough overhaul of capital regulation because, over time, modifications of the Basel accords designed to improve the risk calibration of assets actually enabled banks to reduce regulatory capital.

(i) either capital or leverage regulations to bind, (ii) interest rates to be higher if leverage regulation is in place and (iii) profit taxes to be *weakly* positive. Moreover, there is a trade-off between profit taxes and financial regulations. Implementing efficient risk taking with zero taxes requires either higher regulatory capital or lower leverage. The negative relationship between taxes and regulations in the optimal policy toolkit carries over to our model with persistent aggregate shocks.

To quantitatively evaluate the optimal policies, we calibrate the model with persistent aggregate shocks to the U.S. economy and its financial sector, and examine two numerical experiments. The *optimal CAP* experiment implements the social optimum with interest rate policy, capital regulation and profit taxes, whereas the policies in the *optimal LEV experiment* are interest rate policy, leverage regulation and profit taxes. We find that financial regulations only bind in good aggregate states, when high-risk intermediaries have incentives to engage in excessive risk taking. Moreover, interest rates are lower in the optimal CAP experiment because capital regulation directly affects the asset composition of intermediaries and distorts the equilibrium bond return. Lastly, optimal leverage regulation implements the social optimum with more equity compared to optimal capital regulation, despite no explicit restrictions on the composition of assets.

We conduct additional experiments to highlight differences between capital and leverage regulations. We show that variations in the capital regulation bound—which restricts the equity to risky investment ratio—in the range contemplated by policymakers (i.e., from 8 percent in Basel II to 10.5 percent in Basel III) have a weak effect on risk taking in the economy. However, variations in the leverage regulation bound—which restricts the total assets to equity ratio—have a stronger impact on risk taking, because bond returns are higher under leverage regulation. From a practical point of view, a reason to prefer leverage regulation is that it is easier to implement than capital regulation, which requires assessing the riskiness of all assets on an intermediary’s balance sheet.

The banking literature has previously acknowledged that time-variation in capital require-

ments or leverage restrictions should be incorporated in financial regulation. For example, Kashyap and Stein (2004) argue that time-varying capital requirements are the optimal outcome if the goal is to reduce costs of default, while also maintaining bank lending during recessions. Blum (2008) shows that a risk-independent leverage ratio is necessary to induce truthful reporting of risk and to implement Basel II effectively.

The contribution of our paper is threefold. First, we establish that time-varying financial regulations allow to implement efficient risk taking. Then, we compare the effectiveness of countercyclical capital or leverage regulations in deterring risk taking, in spite of the fact that intermediaries can borrow in an unregulated interbank market to alter the composition of their portfolios. Lastly, we measure welfare implications of alternate financial regulations. Through these contributions, our paper relates to the literature that integrates banking regulation into macro models. Van den Heuvel (2009) measures the welfare cost of capital requirements in a model in which bank moral hazard arises due to deposit insurance. Christensen, Meh, and Moran (2011) study a model in which bank capital arises endogenously to solve an asymmetric information problem between banks and creditors. In their model, countercyclical capital regulation is welfare improving, especially when financial shocks are an important part of economic fluctuations. Angeloni and Faia (2013) study a model with bank runs and nominal rigidities and show that maximizing social welfare requires countercyclical capital regulation and a monetary policy rule that responds to financial conditions. Benes and Kumhof (2015) show that countercyclical capital buffers are welfare improving in a model in which bank loans are risky because the lending rate is not state-contingent. Collard, Dellas, Diba, and Loisel (2017) show that optimal capital regulation is procyclical and covaries negatively with monetary policy in a model in which the latter has no impact on bank risk taking. However, when their model allows monetary policy to have an impact on risk taking, optimal capital regulation and monetary policy are both countercyclical. Unlike these aforementioned papers, our model distinguishes between capital and leverage regulation constraints and allows for a comparison of their effectiveness.

The paper is organized as follows. Section 2 presents the decentralized environment and the social planner’s problem. Section 3 presents results from a simplified version of our model in which we analytically derive policies that implement the social optimum as a competitive equilibrium. Section 4 describes the quantitative analysis and Section 5 concludes.

2 Model Economy

We enrich the model in CSU to allow for capital and leverage regulations, as well as a tax on financial intermediaries’ profits. Our goal is to examine the effectiveness of financial regulations in controlling the risk taking of intermediaries.

The economy is populated by households, financial intermediaries, nonfinancial firms and a government. The existence of intermediaries is motivated by the assumption that households cannot invest directly in some of the economy’s risky assets (Gale (2004)).

Time is discrete and infinite. Each period, the economy is subject to an exogenous aggregate shock that affects the productivity of all firms. The aggregate shock $s_t \in \{\bar{s}, \underline{s}\}$ follows a first-order Markov process and is persistent. The history of aggregate shocks up to time t is s^t . In addition, financial intermediaries are subject to idiosyncratic shocks that determine their type. The idiosyncratic shock $j \in \{h, l\}$ is i.i.d. across time and across financial intermediaries. Figure 1 summarizes the timing of events in our model.

2.1 Financial Sector

Financial intermediaries choose portfolios of safe and risky investments to maximize expected profits. Similar to CSU, intermediaries have limited liability and are partly funded through insured deposits. These features create a moral hazard problem, which makes risky investments attractive for intermediaries. Moreover, in each period, after type j is revealed, intermediaries can adjust the scale of risky investments by borrowing or lending against collateral in an interbank market. The novelty of this paper relative to CSU is that we model

profit taxes and financial regulations to limit intermediaries' risk taking incentives.

The risky projects of intermediaries are investments into the production technologies of firms.⁸ With probability π_j , a risky project is of type $j \in \{h, l\}$ and has productivity $q_j(s_t)$. We assume (i) the probabilities, π_h and $\pi_l = 1 - \pi_h$, are time and state invariant and known, (ii) the high-risk projects are more productive during a good aggregate state and less productive during a bad aggregate state compared with low-risk projects, $q_h(\bar{s}) > q_l(\bar{s}) \geq q_l(\underline{s}) > q_h(\underline{s})$, and (iii) intermediaries cannot trade contingent claims on their projects.

Each period, financial intermediaries make two portfolio decisions. At the time of the first portfolio decision, the aggregate shock, s_t , and the type, j , are unknown and intermediaries are subject to financial regulation constraints. Intermediaries are identical and make the same portfolio investments in government bonds, $b(s^{t-1})$, and risky projects, $k(s^{t-1})$. At the time of the second portfolio decision, the aggregate shock s_t is unknown, while the type $j \in \{h, l\}$ is revealed. Intermediaries are referred to as being high-risk or low-risk, based on the type j of their risky projects. Intermediaries can trade bonds in an interbank market in order to adjust the amount of resources invested in the risky projects. The resulting capital is $k_j(s^{t-1}) \equiv k(s^{t-1}) + \tilde{p}(s^{t-1}) \tilde{b}_j(s^{t-1})$, where $k(s^{t-1})$ is the initial risky investment and $\tilde{b}_j(s^{t-1})$ are bonds traded at the interbank market price $\tilde{p}(s^{t-1})$. The second portfolio decisions are not subject to financial regulation constraints. Implicitly, we assume that the first portfolio decision coincides with the quarterly public reporting of balance sheets, and intermediaries abide by the financial regulations at this time. Between reporting periods, regulatory arbitrage allows intermediaries to increase their risky investments.

The assumption regarding the timing of the aggregate and idiosyncratic shocks is crucial for the existence of an interbank market in this model, and captures the idea that information about the riskiness of projects evolves over time.⁹ As a result, intermediaries adjust their portfolios, but may be constrained in their choices by the amount of bonds, $b(s^{t-1})$, available

⁸For simplicity, we abstract from loans between intermediaries and firms, and information asymmetries à la Bernanke and Gertler (1989). We assume intermediaries operate the firms' production technology directly.

⁹If s_t and j were known at the beginning of each period, resources from households would be allocated so as to equalize intermediaries' marginal rates of return, and there would be no need for an interbank market.

as collateral for interbank borrowing. The need for collateral in interbank borrowing is motivated by a debt enforcement problem à la Kiyotaki and Moore (1997).

After the two portfolio decisions, the aggregate shock s_t realizes at the beginning of period t . Intermediaries choose labor demand for the risky projects, $l_j(s^t)$, and produce using technology $q_j(s_t) [k_j(s^{t-1})]^\theta [l_j(s^t)]^{1-\theta-\alpha}$, where $1 - \alpha - \theta \geq 0$ and $\alpha, \theta \in [0, 1]$. If $\alpha > 0$ there is a fixed factor of production, whose returns are paid to equity holders. The fixed factor prevents a corner solution in the intermediaries' problem and helps the calibrated model match the equity to total asset ratio and the debt to total assets ratio of the U.S. financial sector. Following production, intermediaries unable to pay the promised rate of return on deposits declare bankruptcy.

Portfolio Choice in the Bond Market

At the time of the first portfolio decision, the aggregate shock, s_t , and the type, j , are unknown. There is a measure $1 - \pi_m$ of identical financial intermediaries that choose deposit demand, $d(s^{t-1})$, safe bonds, $b(s^{t-1})$, and risky investments, $k(s^{t-1})$, to maximize the expected profits net of taxes given in problem (P1) subject to financial regulation constraints.

$$\max_{\{d(s^{t-1}), b(s^{t-1}), k(s^{t-1})\}} \sum_{j \in \{h, l\}} \pi_j \sum_{s^t | s^{t-1}} \lambda(s^t) \cdot [1 - \tau(s^{t-1})] V_j(s^t) \quad (\text{P1})$$

subject to:

$$z(s^{t-1}) + d(s^{t-1}) = k(s^{t-1}) + p(s^{t-1}) b(s^{t-1}) \quad (1)$$

$$V_j(s^t) = \max \left\{ \left[\begin{array}{l} q_j(s_t) \left[k(s^{t-1}) + \tilde{p}(s^{t-1}) \tilde{b}_j(s^{t-1}) \right]^\theta [l_j(s^t)]^{1-\theta-\alpha} \\ + q_j(s_t) (1 - \delta) \left[k(s^{t-1}) + \tilde{p}(s^{t-1}) \tilde{b}_j(s^{t-1}) \right] \\ + \left[b(s^{t-1}) - \tilde{b}_j(s^{t-1}) \right] - W_j(s^t) l_j(s^t) - R^d(s^{t-1}) d(s^{t-1}) \end{array} \right], 0 \right\} \quad (2)$$

$$\frac{z(s^{t-1})}{k(s^{t-1})} \geq \eta^{CAP}(s^{t-1}) \quad (3)$$

$$\frac{z(s^{t-1})}{d(s^{t-1})} \geq \eta^{LEV}(s^{t-1}) \quad (4)$$

In problem (P1), $V_j(s^t)$ are gross profits for intermediary j at history s^t and are taxed at rate, $\tau(s^{t-1})$. Since households own the financial intermediaries, profits at history s^t are valued at the households' marginal utility of consumption (weighted by the probability of history s^t), denoted by $\lambda(s^t)$. Intermediaries take as given $\lambda(s^t)$, the bond price, $p(s^{t-1})$, the interbank market price, $\tilde{p}(s^{t-1})$, the wage rate, $W_j(s^t)$, the return on deposits, $R^d(s^{t-1})$, the tax rate, $\tau(s^{t-1})$, the regulatory bounds, $\eta^{CAP}(s^{t-1})$ and $\eta^{LEV}(s^{t-1})$, the bonds traded in the interbank market, $\tilde{b}_j(s^{t-1})$, the labor input, $l_j(s^t)$, and the equity chosen by households, $z(s^{t-1})$.¹⁰ Note that $\tilde{b}_j(s^{t-1})$ is chosen after the type, j , is realized, while $l_j(s^t)$ and $W_j(s^t)$ are determined after the type, j , and the aggregate shock, s_t , are realized.

The balance sheet of an intermediary (equation (1)) shows that portfolio investments are funded through equity, $z(s^{t-1})$, and deposits, $d(s^{t-1})$. Equity returns are contingent on the realization of the aggregate state in the period when they are paid, while returns on deposits are not (i.e., $V_j(s^t)$ depends on s_t , while $R^d(s^{t-1})$ does not). In addition, equity returns are bounded below by zero due to the limited liability of intermediaries (i.e., $V_j(s^t)$ cannot be negative, as seen in equation (2)), while deposit returns are guaranteed by deposit insurance. The limited liability introduces an asymmetry that allows intermediaries to be profitable in good aggregate states while shielding them from losses in bad aggregate states.

Gross profits of intermediaries (equation (2)) equal revenues from investments net of payments to labor and to deposits. Note that the value of the undepreciated capital stock invested in the risky projects (i.e., $q_j(s_t)(1-\delta)\left[k(s^{t-1})+\tilde{p}(s^{t-1})\tilde{b}_j(s^{t-1})\right]$, where δ is the depreciation rate), fluctuates with the productivity level, as in Merton (1973) and Gertler and Kiyotaki (2010), to capture the idea that while capital may not depreciate in a physical sense during contraction periods, it depreciates in an economic sense.¹¹

We augment the model in CSU by introducing profit taxes, $\tau(s^{t-1})$, and two types of financial regulations. Capital regulation (equation (3)) requires financial intermediaries to

¹⁰Due to limited liability and deposit insurance, financial intermediaries prefer to be funded via deposits rather than equity. We assume that equity in our model is determined by households.

¹¹For supporting empirical evidence, see Ramey and Shapiro (2001) and Eisfeldt and Rampini (2006).

hold a ratio of equity to risky investment at history s^{t-1} of at least $\eta^{CAP}(s^{t-1})$. This minimum regulatory capital is state-contingent, in line with Basel III, which introduces time-variation via countercyclical capital buffers (Basel Committee on Banking Supervision (2011)). Leverage regulation (equation (4)) restricts the amount of deposit liabilities financial intermediaries are able to accept to a fraction $\frac{1}{\eta^{LEV}(s^{t-1})}$ of equity. To understand why equation (4) is a constraint on leverage, recall that leverage is defined as the ratio of total assets to equity. Using the notation in Problem (P1), leverage is $\frac{k(s^{t-1})+p(s^{t-1})b(s^{t-1})}{z(s^{t-1})} = \frac{z(s^{t-1})+d(s^{t-1})}{z(s^{t-1})} = 1 + \frac{d(s^{t-1})}{z(s^{t-1})}$. Hence, leverage regulation puts an upper bound on the ratio of deposit borrowing to equity. The Basel III regulation introduces a fixed leverage ratio as a supplement to capital regulation. In our framework, we allow leverage regulation to be state-contingent. We show that either state-contingent capital or leverage regulation implements the social optimum when combined with a tax on intermediaries' profits and optimally chosen interest rate policy. The profit tax on financial intermediaries allows for marginal products of capital to be aligned across different technologies of production in competitive equilibria that implement the social optimum.¹²

Portfolio Adjustments via the Interbank Market

At the time of the second portfolio decision, the aggregate shock, s_t , is unknown, while the type, $j \in \{h, l\}$, is known. High-risk ($j = h$) and low-risk ($j = l$) intermediaries choose whether to adjust the riskiness of their portfolios by trading bonds, $\tilde{b}_j(s^{t-1})$, in an interbank market. Intermediaries choose $\tilde{b}_j(s^{t-1})$ and, implicitly, $k_j(s^{t-1}) \equiv k(s^{t-1}) + \tilde{p}(s^{t-1})\tilde{b}_j(s^{t-1})$ to solve problem (P2), taking as given the initial portfolio decisions, $d(s^{t-1})$, $b(s^{t-1})$, $k(s^{t-1})$,

¹²The non-financial sector in our model is fully equity funded. The financial sector is funded via both equity and debt. The tax rate on intermediaries reduces the return to financial sector equity to allow for equalization of the marginal products of capital across sectors. Without taxes, the equity required in the financial sector to implement the social optimum would be higher.

as well as $\lambda(s^t)$, $p(s^{t-1})$, $\tilde{p}(s^{t-1})$, $W_j(s^t)$, $R^d(s^{t-1})$, $\tau(s^{t-1})$, $l_j(s^t)$, and $z(s^{t-1})$.

$$\begin{aligned} & \max_{\{\tilde{b}_j(s^{t-1}), k_j(s^{t-1})\}} \sum_{s^t | s^{t-1}} \lambda(s^t) \cdot [1 - \tau(s^{t-1})] V_j(s^t) & \text{(P2)} \\ \text{subject to: } & -\frac{k(s^{t-1})}{\tilde{p}(s^{t-1})} \leq \tilde{b}_j(s^{t-1}) \leq b(s^{t-1}) \end{aligned}$$

where $V_j(s^t)$ is defined in equation (2). Inada conditions guarantee that $k_j(s^{t-1}) \equiv k(s^{t-1}) + \tilde{p}(s^{t-1})\tilde{b}_j(s^{t-1}) > 0$, and hence the only potentially binding constraint in problem (P2) is $\tilde{b}_j(s^{t-1}) \leq b(s^{t-1})$.¹³ Here, $\tilde{b}_j(s^{t-1})$ can be interpreted as sales of bonds or, alternatively, as repurchasing agreements (repos).¹⁴ For this reason, we use the terms interbank market and repo market interchangeably. As in CSU, we abstract from haircuts on collateral.

The capital and leverage regulation constraints in (3) and (4) are not imposed in problem (P2). Our implicit assumption is that intermediaries report profits and pay profit taxes to the government, but they need not abide by financial regulations throughout the period. Indeed, Munyan (2015) shows that the repo market allows for *window dressing*, the practice of adjusting investments prior to public disclosure periods to make balance sheets seem safer. Using daily tri-party repo transactions from 2008 to 2014, Munyan (2015) documents a pronounced decline in repo borrowing at quarter-ends and a subsequent rebound at the beginning of next quarter. The repo window dressing documented by Munyan (2015) is different from the Repo 105 transactions that Lehman Brothers used to hide true leverage. While Repo 105 may be an accounting trick unique to Lehman, it gives an idea of the innovations possible within the banking industry to undermine financial regulations.

¹³The assumption that interbank (repo) borrowing is collateralized, $\tilde{b}_j(s^{t-1}) \leq b(s^{t-1})$, is motivated by a debt enforcement problem à la Kiyotaki and Moore (1997). Namely, lenders in the interbank market cannot force borrowers to repay debts unless these debts are secured by collateral.

¹⁴While we model $\tilde{b}_j(s^{t-1})$ as bond sales, incorporating explicitly the repurchase of bonds—which is typical in a repo agreement—would yield identical results. Specifically, if no bankruptcy occurs, then intermediaries have the resources necessary to repurchase the bonds from the counterparty. This simply amounts to a reshuffling of assets among intermediaries before profits are paid as returns to equity holders. When some intermediaries go bankrupt, they are unable to repurchase the bonds and the counterparty keeps them, as is true in the data. Equity holders receive no returns from bankrupt intermediaries. In either case, payments to equity holders are identical regardless of whether we model the repurchase of bonds or not.

Our model is consistent with evidence that repos are an important margin of balance sheet adjustment by intermediaries (Adrian and Shin (2010)) and that repos allow participants to “hedge against market risk exposures arising from other activities” (Financial Stability Board (2012)). In our model, repo borrowing is socially beneficial as it reallocates resources towards intermediaries who are expected to be more productive. In expansions, high-risk intermediaries lower their bond holdings to invest more in their risky projects. In contractions, low-risk intermediaries make similar changes to their portfolios.

While repos are beneficial, they may enable intermediaries to take advantage of their limited liability and overinvest in risky projects. More bond purchases at the time of the first portfolio decision make balance sheets seem safer, but may later lead to increased risk taking through collateralized borrowing. Although intermediaries start out as identical each period, the funds they receive from households vary with the aggregate state, allowing for interesting model dynamics, such as sustained high investments in high-risk projects.

Labor Demand and Production

After the two portfolio decisions, the aggregate shock, $s_t \in \{\bar{s}, \underline{s}\}$, is realized. Financial intermediaries choose labor demand, $l_j(s^t)$, to equate the wage rate with the marginal product of labor, i.e., $W_j(s^t) = (1 - \theta - \alpha) q_j(s_t) [k_j(s^{t-1})]^\theta [l_j(s^t)]^{-\theta-\alpha}$. Production takes place, returns on assets are paid and bankruptcy may occur.

We note that labor is an essential input into production. If we abstract from labor, then expected returns on financial sector equity in our model are larger than expected returns on deposits, pushing households to choose zero deposits, which is counterfactual. We assume the labor input is chosen after the intermediaries know j and s_t , for computational simplicity.

2.2 Nonfinancial sector

There is a measure π_m of identical nonfinancial firms that choose capital, $k_m(s^{t-1})$, and labor, $l_m(s^t)$, to maximize profits.

$$\begin{aligned} \max_{\{k_m(s^{t-1}), l_m(s^t)\}} \{ & y_m(s^t) + q_m(s_t)(1 - \delta)k_m(s^{t-1}) - R^m(s^t)k_m(s^{t-1}) - W_m(s^t)l_m(s^t) \} \\ \text{subject to: } & y_m(s^t) = q_m(s_t) [k_m(s^{t-1})]^\theta [l_m(s^t)]^{1-\theta} \end{aligned}$$

Here, capital is funded entirely through household equity, $k_m(s^{t-1}) = M(s^{t-1})/\pi_m$, the wage rate is $W_m(s^t)$, and the return to capital (equity), $R^m(s^t)$, depends on the productivity of the technology, $q_m(s_t)$, which satisfies: $q_h(\bar{s}) \geq q_m(\bar{s}) > q_l(\bar{s}) \geq q_l(\underline{s}) > q_m(\underline{s}) > q_h(\underline{s})$.

The nonfinancial sector is introduced to allow our model to be consistent with U.S. data, showing a high equity to deposit ratio for households and a low equity to deposit ratio in the financial sector, and to match the relative importance of the two sectors in U.S. production.

2.3 Households

There is a measure one of identical households who maximize expected utility.

$$\begin{aligned} \max_{\{C(s^t), D_h(s^t), Z(s^t), M(s^t)\}} & \sum_{t=0}^{\infty} \sum_{s^t} \beta^t \varphi(s^t) \log C(s^t) \\ \text{subject to: } w(s^t) = & R^d(s^{t-1})D_h(s^{t-1}) + R^z(s^t)Z(s^{t-1}) + R^m(s^t)M(s^{t-1}) \\ & + \pi_m W_m(s^t) + (1 - \pi_m)\pi_l W_l(s^t) + (1 - \pi_m)\pi_h W_h(s^t) + T(s^t) \\ w(s^t) = & C(s^t) + M(s^t) + D_h(s^t) + Z(s^t) \end{aligned}$$

Here, β is the discount factor and $\varphi(s^t)$ is the probability of history s^t . At the beginning of period t , the aggregate state s_t is revealed, and household wealth, $w(s^t)$, composed of returns on previous period investments, wage income and lump-sum taxes ($T(s^t) < 0$) or transfers ($T(s^t) \geq 0$) from the government, is realized. Households spend their wealth on

consumption, $C(s^t)$, and investments that will pay returns next period.

Investments take the form of deposits, financial sector equity and nonfinancial sector equity. Deposits, $D_h(s^{t-1})$, earn a fixed return, $R^d(s^{t-1})$, which is guaranteed by deposit insurance. Equity invested in the financial sector, $Z(s^{t-1})$, is a risky investment that gives households a state-contingent claim to the profits of the intermediaries. The return per unit of equity is $R^z(s^t) = \frac{1}{z(s^{t-1})} \sum_{j \in \{h,l\}} \pi_j [1 - \tau(s^{t-1})] V_j(s^t)$. Similarly, the equity invested in the nonfinancial sector, $M(s^{t-1})$, receives a state-contingent return, $R^m(s^t)$. An interior solution in which households invest in all three assets requires that expected returns on deposits and equity are equalized. Formally, $\sum_{s^{t+1}|s^t} \frac{\beta^{t+1} \varphi(s^{t+1})}{C(s^{t+1})} [R^z(s^{t+1}) - R^d(s^t)] = \sum_{s^{t+1}|s^t} \frac{\beta^{t+1} \varphi(s^{t+1})}{C(s^{t+1})} [R^z(s^{t+1}) - R^m(s^{t+1})] = 0$.

Each household supplies one unit of labor inelastically. We assume that labor markets are segmented. Fraction π_m of a household's time is spent working in the nonfinancial sector, and fraction $1 - \pi_m$ is spent in the financial sector. Within the financial sector, a household's time is split between high-risk and low-risk intermediaries according to shares π_j , where $\pi_h + \pi_l = 1$. Given that there are measure one of households and measure one of firms, labor supplied to each firm is one unit for any realization of the aggregate state.

2.4 Government

The government issues bonds that financial intermediaries hold as an investment or use as a medium of exchange in the repo market. The government sells bonds, $B(s^{t-1})$, at price, $p(s^{t-1})$, and deposits the proceeds with financial intermediaries. Each intermediary purchases risk-free assets $b(s^{t-1}) = B(s^{t-1}) / (1 - \pi_m)$ and receives $D_g(s^{t-1}) / (1 - \pi_m)$ of government deposits, where $D_g(s^{t-1}) = p(s^{t-1}) B(s^{t-1})$. To guarantee the return on deposits the government provides deposit insurance at zero price, which is financed through household taxation and taxes on intermediaries' profits.¹⁵ The government balances its bud-

¹⁵Pennacchi (2006, pg. 14) documents that, since 1996 and prior to the crisis, deposit insurance has been essentially free for U.S. banks. In our model, the assumption of a zero price of deposit insurance is not crucial. What matters is that the insurance is not priced in a way to eliminate moral hazard. This means,

get after production takes place at the beginning of period t .

$$T(s^t) + B(s^{t-1}) + \Delta(s^t) = R^d(s^{t-1}) D_g(s^{t-1}) + \tau(s^{t-1}) \cdot (1 - \pi_m) \sum_{j \in \{h, l\}} \pi_j V_j(s^t)$$

Here, $\Delta(s^t)$ is deposit insurance necessary to guarantee the return on deposits, $R^d(s^{t-1})$. Given limited liability, intermediaries may pay a deposit return smaller than $R^d(s^{t-1})$, which ensures that they break even, while the remainder is covered by deposit insurance.

2.5 Market clearing

The *labor market clearing conditions* state that labor demanded by financial intermediaries and nonfinancial firms equals labor supplied by households: $\pi_m l_m(s^t) = \pi_m$ and $(1 - \pi_m) \pi_j l_j(s^t) = (1 - \pi_m) \pi_j$ for each $j \in \{h, l\}$. This implies $l_m(s^t) = l_h(s^t) = l_l(s^t) = 1$.

The *goods market clearing condition* equates total output produced with aggregate consumption and investment. Output produced by nonfinancial firms is $\pi_m q_m(s^t) [k_m(s^{t-1})]^\theta$, while output produced by financial firms is $(1 - \pi_m) \sum_{j \in \{l, h\}} \pi_j q_j(s^t) [k_j(s^{t-1})]^\theta$, where $k_j(s^{t-1})$ are resources allocated to the risky projects after repo market trading.

$$\begin{aligned} C(s^t) + M(s^t) + D_h(s^t) + Z(s^t) &= \pi_m q_m(s_t) \left[[k_m(s^{t-1})]^\theta + (1 - \delta) k_m(s^{t-1}) \right] \\ &\quad + (1 - \pi_m) \sum_{j \in \{l, h\}} \pi_j q_j(s_t) \left[[k_j(s^{t-1})]^\theta + (1 - \delta) k_j(s^{t-1}) \right] \end{aligned}$$

There are *four financial market clearing conditions*. Deposits demanded by intermediaries equal deposits from households and the government: $D_h(s^{t-1}) + D_g(s^{t-1}) = D(s^{t-1}) = (1 - \pi_m) d(s^{t-1})$. Bond sales by the government equal the bond purchases by financial intermediaries: $B(s^{t-1}) = (1 - \pi_m) b(s^{t-1})$. Interbank repo market trades between the different types of intermediaries must balance: $\sum_{j \in \{l, h\}} \pi_j \tilde{b}_j(s^{t-1}) = 0$. Lastly, total equity invested by households in the financial and nonfinancial sectors is distributed over the firms:

for example, that deposit insurance cannot be contingent on the portfolio decisions of the intermediaries.

$$M(s^{t-1}) = \pi_m k_m(s^{t-1}) \text{ and } Z(s^{t-1}) = (1 - \pi_m) z(s^{t-1}).$$

2.6 Social Planner

We examine a social planner's problem to determine the efficient allocation of resources. We maintain the assumption on the timing of shocks to allow the social planner's environment to be comparable to the decentralized one. In a slight abuse of language, we refer to the technologies available to the social planner as belonging to financial and nonfinancial sectors.

At the beginning of period t , the aggregate shock, s_t , is revealed and production takes place using capital that the planner has allocated to the different technologies of production: $k_m(s^{t-1})$ for the nonfinancial sector and $k_h(s^{t-1})$ and $k_l(s^{t-1})$ for the high-risk and low-risk technologies of the financial sector. Output is then split between consumption and capital to be used in production at $t + 1$. At the time of this decision, the type, j , and the aggregate shock, s_{t+1} , are unknown, and the social planner allocates $k_b(s^t)$ resources to all financial sector technologies. Once j is revealed, the social planner reallocates resources between the high-risk and low-risk technologies.

The social planner (SP) solves the problem below.

$$\max E \sum_{t=0}^{\infty} \beta^t \log C(s^t)$$

subject to:

$$\begin{aligned} C(s^t) + \pi_m k_m(s^t) + (1 - \pi_m) k_b(s^t) &= \pi_m q_m(s_t) \left[[k_m(s^{t-1})]^\theta + (1 - \delta) k_m(s^{t-1}) \right] \\ &+ (1 - \pi_m) \sum_{j \in \{h, l\}} \pi_j q_j(s_t) \left[[k_j(s^{t-1})]^\theta + (1 - \delta) k_j(s^{t-1}) \right] \\ k_l(s^t) &= k_b(s^t) - \frac{\pi_h}{\pi_l} n(s^t) \\ k_h(s^t) &= k_b(s^t) + n(s^t) \end{aligned}$$

Here, $n(s^t)$ are resources given to (or taken from) each high-risk production technology, and $\frac{\pi_h}{\pi_l} n(s^t)$ are resources taken away from (or given to) each low-risk technology. Resources

flow towards intermediaries who are expected to be more productive, i.e., high-risk intermediaries during expansion periods and low-risk intermediaries during contractions.

2.7 Government Policies

The government is a consolidated monetary and financial authority. The government's objective is to find policies that maximize household welfare. Such policies implement the social optimum as a competitive equilibrium. By implementation we mean finding the interest rate policy, $1/p(s^t)$, the regulatory bounds, $\eta^{CAP}(s^t)$ or $\eta^{LEV}(s^t)$, and the profit tax, $\tau(s^t)$, such that the allocations in the competitive equilibrium with $\{1/p(s^t), \eta^{CAP}(s^t), \eta^{LEV}(s^t), \tau(s^t)\}$ coincide with those from the social planner's problem. Since the monetary and financial authority have the common goal of maximizing the welfare of households, the interest rate policy and financial regulations are interdependent.

3 Results from a Simplified Version of the Model

In this section, we consider a simplified version of our full model from Section 2, which allows us to derive analytically the policies that implement the social optimum. Moreover, we discuss implications for the full model.

Assumptions A1 : (i) The aggregate productivity shock, s_t , is i.i.d. The probability of the good aggregate state, \bar{s} , is ϕ and the probability of the bad aggregate state, \underline{s} , is $1 - \phi$. (ii) Households are risk neutral. (iii) Depreciation is full, $\delta = 1$. (iv) There is no fixed factor in financial intermediaries' production, $\alpha = 0$. (v) Productivity levels satisfy $q_h(\bar{s}) > q_l(\bar{s}) = q_l(\underline{s}) > q_h(\underline{s})$. Moreover, high-risk projects have higher expected productivity than low-risk projects, $\phi q_h(\bar{s}) + (1 - \phi) q_h(\underline{s}) > q_l(\bar{s}) = q_l(\underline{s})$.

Proposition 1 shows that bankruptcy may occur in equilibrium. Intermediaries declare bankruptcy if they are unable to pay the promised rate of return to depositors.

Proposition 1 *Under assumption A1 (v), in a competitive equilibrium with an active interbank market, either there is no bankruptcy, or only high-risk intermediaries are bankrupt in a bad aggregate state.*

Proof. See Appendix A. ■

The policies that implement the social optimum depend on whether or not there is bankruptcy in the competitive equilibrium. We analyze these two cases separately.

Proposition 2 characterizes the policies that implement the social optimum as a competitive equilibrium with no bankruptcy and highlights some equilibrium properties.

Proposition 2 *Under assumptions A1, if the allocation in a competitive equilibrium with no bankruptcy coincides with the social planner's allocation, then (i) the capital and leverage regulations do not bind, (ii) the interest rate policy is $\frac{1}{p(s^t)} = \frac{1}{\beta}$ and (iii) the tax on intermediaries' profits is zero. In addition, (iv) the collateral constraints of intermediaries do not bind and (v) the intermediaries' equity to risky capital ratio satisfies: $\frac{z(s^t)}{k(s^t)} > 1 - \left(\phi \frac{q_h(\bar{s})}{q_h(s)} + 1 - \phi \right)^{-1}$.*

Proof. See Appendix A. ■

Proposition 2 shows that, if equity is high enough, the moral hazard of financial intermediaries is reduced and there is no bankruptcy, as most of the intermediaries' liabilities are state-contingent. As a result, the social optimum can be implemented with a single and unique policy tool, the interest rate β^{-1} , while financial regulations or taxes are not needed. Moreover, since high equity reduces intermediaries' risk taking incentives, only a subset of bonds are traded in the interbank market (i.e. collateral constraints are slack).

When we calibrate our full model from Section 2 to match financial intermediaries' equity levels observed in U.S. data, the model features bankruptcy. Proposition 3 characterizes the policies that implement the social optimum as a competitive equilibrium with bankruptcy of high-risk intermediaries, and shows that the collateral constraint of high-risk intermediaries binds to restrict risk taking.

Proposition 3 *Under assumptions A1, different combinations of policies implement the social optimum as a competitive equilibrium with bankruptcy. First, binding capital regulation, interest rate policy $\frac{1}{p(s^t)} < \frac{1}{\beta}$, and profit taxes $\tau(s^t) \geq 0$ implement the social optimum. Alternatively, binding leverage regulation, interest rate policy $\frac{1}{p(s^t)} = \frac{1}{\beta}$, and profit taxes $\tau(s^t) \geq 0$ implement the social optimum. In either case, there is a trade-off between taxes and financial regulations. Implementations with positive taxes allow for smaller financial regulatory bounds, i.e., $\eta^{CAP}(s^t)$ or $\eta^{LEV}(s^t)$, than implementations with zero taxes. Moreover, in these competitive equilibria, the collateral constraint of high-risk intermediaries binds.*

Proof. See Appendix A. ■

There are several important implications from Proposition 3. First, either binding capital regulation or binding leverage regulation are necessary to reduce the moral hazard of high-risk intermediaries and to implement the social optimum in a competitive equilibrium with bankruptcy.¹⁶ Second, taxes are not needed to implement the social optimum, but if used, they allow for looser financial regulation constraints. Indeed, in the proof of Proposition 3, we show that the social optimum can be implemented with interest rate policy and combinations of profit taxes and financial regulations that satisfy equation (5):

$$\frac{1}{1 - \tau(s^t)} = Q_1^i + Q_2^i \frac{1}{\eta^i(s^t)}, \quad i \in \{CAP, LEV\} \quad (5)$$

where the coefficients Q_1^i, Q_2^i for $i \in \{CAP, LEV\}$ are functions of parameters $\phi, \theta, \pi_j, q_j(\bar{s})$ and $q_j(\underline{s})$ for $j \in \{h, l\}$.¹⁷ Since $Q_1^i > 0, Q_2^i > 0$, for $i \in \{CAP, LEV\}$, it is easy to show that higher taxes lower the financial regulatory bounds, i.e., $\frac{\partial \eta^{CAP}(s^t)}{\partial \tau(s^t)} < 0$ and $\frac{\partial \eta^{LEV}(s^t)}{\partial \tau(s^t)} < 0$.

Moreover, Proposition 3 shows that implementing the social optimum in a competitive equilibrium with bankruptcy requires that the high-risk intermediaries' collateral constraint

¹⁶The proof of Proposition 3 shows that if bankruptcy is possible at time t , then financial regulation binds at $t - 1$. We conjecture that regulation binds in expansions, because the aggregate state may switch, leading high-risk intermediaries to default. We confirm this conjecture in our quantitative analysis (Section 4).

¹⁷The proof of Proposition 3 shows that: $Q_1^{LEV} = \pi_l + \phi \pi_h \frac{q_h(\bar{s})}{\phi q_h(\bar{s}) + (1 - \phi) q_h(\underline{s})}$, $Q_2^{LEV} = \frac{\phi \pi_h (1 - \phi) [q_h(\bar{s}) - q_h(\underline{s})]}{\phi q_h(\bar{s}) + (1 - \phi) q_h(\underline{s})}$, $Q_1^{CAP} = \pi_l + \phi \pi_h$ and $Q_2^{CAP} = \phi \pi_h (1 - \phi) [q_h(\bar{s}) - q_h(\underline{s})] \frac{[\phi q_h(\bar{s}) + (1 - \phi) q_h(\underline{s})]^{1 - \theta}}{\sum_j \pi_j [\phi q_j(\bar{s}) + (1 - \phi) q_j(\underline{s})]^{1 - \theta}}$.

binds to restrict risk taking via the interbank market. In contrast, in Proposition 2, high levels of equity provide high-risk intermediaries with incentives to not go bankrupt and to choose the socially optimal portfolio.

Lastly, Proposition 3 shows that the optimal interest rate policy varies with the financial regulation in place. In particular, interest rates are lower under capital regulation than under leverage regulation. To understand this result, note that under assumptions A1, the interbank market bond return, $1/\tilde{p}(s^t)$ —which influences the composition of intermediaries’ portfolios after repo trades—is equated with β^{-1} , the expected return on investments in the social planner’s problem. When the social optimum is implemented with binding capital regulation, the equilibrium bond return is lower than the interbank market bond return, i.e., $1/p(s^t) < 1/\tilde{p}(s^t)$, because bonds have a liquidity value, as they can be traded in the interbank market and they directly change the capital position of intermediaries. In contrast, when the social optimum is implemented with leverage regulation, bonds cannot be used to relax the binding leverage constraint and the equilibrium bond return is set equal to the interbank market return, i.e., $1/p(s^t) = 1/\tilde{p}(s^t)$. To sum up, interest rate policy is β^{-1} if the social optimum is implemented with leverage regulation, or less than β^{-1} if it is implemented with capital regulation (for analytical details, see the proof of Proposition 3).

4 Quantitative Analysis

We calibrate the model to match key features of the U.S. economy and its financial sector. We solve the model numerically and characterize the policies that implement the social optimum in our decentralized economy. We then perform experiments to quantify the impact of deviating from the optimal policies on intermediaries’ risk taking and the macroeconomy. We define risk taking as the percentage deviation in the resources invested in the high-risk projects in a competitive equilibrium, i.e., $k_h^{CE}(s^t)$, relative to the social planner, i.e., $k_h^{SP}(s^t)$. Formally, $r(s^t) = \frac{k_h^{CE}(s^t) - k_h^{SP}(s^t)}{k_h^{SP}(s^t)} \cdot 100$, where a positive value of $r(s^t)$ indicates

excessive risk taking in the competitive equilibrium, while a negative value indicates too little risk taking. We also report an aggregate measure of risk taking, defined as an average over expansions and contractions, i.e., $r \equiv E[r(s^t)]$. To quantify the macroeconomic impact of suboptimal policies, we use a standard welfare measure, the lifetime consumption equivalent (LTCE), defined as the percentage decrease in the planner's consumption required to give consumers the same welfare as the consumption from the competitive equilibrium.

4.1 Calibration

We parameterize the model to the U.S. economy, similar to CSU. Specifically, we identify our model's total output with the U.S. business sector value added and our model's nonfinancial sector with the U.S. corporate nonfinancial sector.¹⁸

Table 1 reports the calibrated discount factor, β , the capital share, θ , the aggregate shock transition matrix, Φ , and the fraction of high-risk intermediaries, π_h . The remaining parameters, $Q \equiv \{\pi_m, \alpha, \delta, q_h(\underline{s}), q_m(\bar{s}), q_m(\underline{s}), q_l(\bar{s}), q_l(\underline{s})\}$, are jointly estimated to match eight U.S. data moments using problem (P3). Table 2 reports the matched moments and the estimated parameters.

$$\begin{aligned}
 Q^* &= \arg \min_Q \sum_{i=1}^8 \left(\frac{\Omega_i - \tilde{\Omega}_i}{\tilde{\Omega}_i} \right)^2 & (P3) \\
 \text{s.t.} &: q_h(\underline{s}) < q_m(\underline{s}) < q_l(\underline{s}) \leq q_l(\bar{s}) < q_m(\bar{s}) \leq q_h(\bar{s}) = 1 \text{ and} \\
 &\Omega_i \text{ is implied in a competitive equilibrium, given policies } \Lambda^*, \\
 &\text{where } \Lambda^*(s^{t-1}) \equiv \{p^*(s^{t-1}), \eta^{CAP} = 0.08, \eta^{LEV} = 0, \tau = 0\}
 \end{aligned}$$

In problem (P3), Ω_i is a model moment, $\tilde{\Omega}_i$ is the corresponding data moment, and the productivity parameters are ordered as discussed in Section 2, with the productivity of

¹⁸We treat the remainder of the U.S. business sector (the corporate financial and the noncorporate businesses) as the model's financial intermediation sector. In U.S. data, noncorporate businesses are strongly dependent on the financial sector for funding. In the past three decades, bank loans and mortgages were 60 to 80 percent of noncorporate businesses' liabilities. For simplicity, we do not model these loans, and assume that intermediaries are endowed with the production technology of noncorporate businesses.

the high-risk intermediary in the good aggregate state normalized to unity. Moreover, the policies are given in $\Lambda^*(s^{t-1})$, where the values for η^{CAP} , η^{LEV} , and τ are set to capture the Basel II capital regulation, and where $p^*(s^{t-1})$ solves problem (P4).¹⁹

$$p^*(s^{t-1}) = \arg \max_{p(s^{t-1})} \sum_{t=0}^{\infty} \sum_{s^t} \beta^t \varphi(s^t) \log C(s^t) \quad (\text{P4})$$

s.t.: $C(s^t)$ is part of a competitive equilibrium given parameters Q^* ,
and policies $\Lambda(s^{t-1}) = \{p(s^{t-1}), \eta^{CAP} = 0.08, \eta^{LEV} = 0, \tau = 0\}$

Table 2 shows that the model matches the data moments well. The first three data moments pin down π_m , α and δ , respectively. We note that δ is chosen so that our model's stochastic depreciation rate, $\frac{\pi_m q_{m,t} \delta k_{m,t} + (1 - \pi_m)(\pi_h q_{h,t} \delta k_{h,t} + \pi_l q_{l,t} \delta k_{l,t})}{\pi_m k_{m,t} + (1 - \pi_m)(\pi_h k_{h,t} + \pi_l k_{l,t})}$, matches the data. The remaining moments help pin down the productivity parameters. Note that low-risk projects are estimated to be virtually riskless, while high-risk projects have a large variance of returns. This suggests that the moral hazard problem is important for high-risk intermediaries.

4.2 Analytical Results and Simulations from the Full Model

We show analytically that different combinations of policies—i.e., either $(\frac{1}{p}, \eta^{CAP}, \tau)$ or $(\frac{1}{p}, \eta^{LEV}, \tau)$ —implement the social optimum as a competitive equilibrium. We simulate the model and discuss the key characteristics of the policies. Lastly, we vary the regulatory ratios, η^{CAP} or η^{LEV} , and the tax rate away from their optimal levels and evaluate the impact on intermediaries' balance sheets, on risk taking and welfare.²⁰

We solve the model numerically using Carroll (2006)'s endogenous grid method with occasionally binding nonlinear constraints due to the limited liability of intermediaries and

¹⁹Solving problem (P3) involves a two-step procedure as in CSU, because the model is nonlinear and the initial guess is very important in finding a competitive equilibrium. Given $\eta^{CAP} = 8\%$, $\eta^{LEV} = 0$, $\tau = 0$, an initial set of parameter values, call it Q_1^* , and an initial guess for our competitive equilibrium allocation (e.g. the social planner allocation), we find the optimal bond price, p_1^* , that solves problem (P4). Then, given p_1^* , we find Q_2^* that solves problem (P3). We continue this iterative process until convergence is achieved.

²⁰Deviations from the optimal interest rate policy were analyzed in detail in CSU, in a model without financial regulations.

the possibility of a constrained interbank market or binding financial regulation constraints.

4.2.1 Implementing the Social Optimum with Capital or Leverage Regulation

We construct prices, asset returns and policies that implement the socially optimal allocation as a competitive equilibrium. The social optimum can be implemented with interest rate policy, capital regulation and profit taxes, $(\frac{1}{p}, \eta^{CAP}, \tau)$. We refer to this implementation as the *optimal CAP experiment*. Alternatively, the *optimal LEV experiment* implements the social optimum with interest rate policy, leverage regulation and profit taxes, $(\frac{1}{p}, \eta^{LEV}, \tau)$.

Propositions 4 and 5 present some analytical results of these two implementations under specific assumptions regarding the bankruptcy of intermediaries.²¹ Subsequently, we use numerical simulations to confirm the bankruptcy patterns assumed in the propositions, and to discuss the key characteristics of the policies. The parameters used in our numerical simulations are those from Tables 1 and 2, while the financial regulation bounds, η^{CAP} or η^{LEV} , and the tax rate, τ , are constructed to implement the social optimum.

Implementing the social optimum requires financial regulations to bind in expansions (Proposition 4), but not in recessions (Proposition 5). Moreover, there is a trade-off between the tax rate and the regulatory bounds that implement the social optimum (Proposition 4).

Proposition 4 *Let the aggregate state at t be $s_t = \bar{s}$. Assume that if $s_{t+1} = \underline{s}$, the high-risk intermediaries are bankrupt at $t + 1$. Implementing the social optimum requires that (i) financial regulations bind at t , and (ii) the financial regulation bounds and the tax rate satisfy:*

$$\frac{1}{1 - \tau(s^t | s_t = \bar{s})} = Q_1^i(s^t) + Q_2^i(s^t) \frac{1}{\eta^i(s^t | s_t = \bar{s})}, \quad i \in \{CAP, LEV\} \quad (6)$$

where the coefficients $Q_1^i(s^t)$, $Q_2^i(s^t)$ for $i \in \{CAP, LEV\}$ are functions of the social planner's allocations and parameters $\beta, \delta, \theta, \alpha, \Phi, \pi_j, q_j(\bar{s})$ and $q_j(\underline{s})$ for $j \in \{h, l\}$.

²¹For high productivity states, i.e. $s_t = \bar{s}$, it is possible to analytically derive all prices and asset returns that implement the social optimum as a competitive equilibrium. These details are not included in Proposition 4, but are available upon request from the authors.

Proof. See Appendix A. ■

Proposition 5 *Let the aggregate state at t be $s_t = \underline{s}$. Assume that no intermediary is bankrupt at $t + 1$ for any realization of $s_{t+1} \in \{\bar{s}, \underline{s}\}$. Then, financial regulations do not bind at t in implementations of the social optimum.*

Proof. See Appendix A. ■

In what follows, we present results from the optimal CAP and optimal LEV experiments—the two implementations we consider—for a sequence of 100 draws of the aggregate shock. We discuss the features of the policies that implement the social optimum, including the trade-offs between the financial regulation bounds and the tax rate implied by equation (6).

Figure 2 plots the policies that implement the social optimum: either $\left(\frac{1}{p}, \eta^{CAP}, \tau\right)$ in the optimal CAP experiment, or $\left(\frac{1}{p}, \eta^{LEV}, \tau\right)$ in the optimal LEV experiment. The net annualized interest rate policy, i.e., $100 \cdot [(1/p)^4 - 1]$, is procyclical (upper left subplot in Figure 2) and depends on the financial regulations in place. Specifically, during booms, interest rates in the optimal CAP experiment are 1.9 percentage points lower, on average, than in the optimal LEV experiment. During recessions, the interest rates in the two implementations are equal. The intuition for these results is the same as in the simple model of Section 3. The interbank market bond returns, $1/\tilde{p}$, in the two experiments are equated with the expected return on investments in the social optimum. Under binding leverage regulation, the bond return, $1/p$, is equal to $1/\tilde{p}$. However, binding capital regulation during booms alters the composition of intermediaries' assets and lowers the bond return relative to the interbank market bond return.

Unlike interest rate policy, the financial regulations and tax rates that implement the social optimum are not unique, as shown in Proposition 4. The state-dependent nature of the coefficients in equation (6) implies that either the profit tax rate, τ , or the regulatory bounds, η^{CAP} or η^{LEV} , must also depend on the model's state variables: household wealth, w_t , and aggregate productivity, s_t . In implementing the social optimum, we restrict the profit

tax rate to vary only with aggregate productivity and let the regulatory bounds absorb any variation in wealth (i.e., compute $\eta^{CAP}(w_t, s_t = \bar{s})$ or $\eta^{LEV}(w_t, s_t = \bar{s})$ from (6)).

Specifically, we set $\tau(\bar{s}) = 0.0361$ to obtain an average minimum regulatory capital of 10.5 percent during high productivity periods, consistent with the Basel III regulation currently implemented in many countries (upper right subplot in Figure 2). We set the tax rate for the low productivity periods to $\tau(\underline{s}) = 0.0007$ to minimize the business cycle variation in the intermediaries' equity to risky capital ratio, i.e., z/k , in the implementation with capital regulation. We keep tax rates at the same level when implementing the social optimum with leverage regulation, and then back out $\eta^{LEV}(w_t, s_t = \bar{s})$ from equation (6).

Figure 2 plots the minimum regulatory capital necessary to implement the social optimum and the actual equity to risky capital ratio in the optimal CAP experiment (lower left subplot), as well as the actual and the minimum required equity to deposit ratio in the optimal LEV experiment (lower right subplot). Note that our model calls for financial regulation constraints to be relaxed during recessions. Since financial regulations only bind in high productivity periods, we exogenously set the required regulatory ratios to zero in low productivity periods.²² Although we allow the regulatory bounds computed from equation (6) to vary with household wealth, the numerical results show that, during high productivity periods when wealth increases, $\eta^{CAP}(w_t, s_t = \bar{s})$ and $\eta^{LEV}(w_t, s_t = \bar{s})$ are flat. This result is desirable from a policymaker's perspective, since regulations that are independent of the model's endogenous state variable (i.e., wealth) are easier to implement in practice.

Figure 3 compares simulation results from the optimal CAP and the optimal LEV experiments, for a sequence of 100 draws of the aggregate state. One important difference between the two implementations is that equity constitutes a larger fraction of total liabilities under optimal leverage regulation than under optimal capital regulation (upper right subplot). Since the fraction of assets invested in risky projects is the same across the two experiments (middle right subplot), the capital regulation constraint from the optimal CAP

²²Alternatively, the required capital can be set to 8 percent or any lower number, as it would not bind.

experiment is satisfied under the optimal LEV experiment. Thus, optimal leverage regulation imposes a stricter requirement on equity compared to optimal capital regulation, allowing the implementation of the social optimum without explicit restrictions on the composition of assets. A second difference between the optimal CAP and optimal LEV experiments is that the spread between the deposit rate and the government bond rate is positive in high productivity periods under optimal capital regulation, whereas it is always zero under optimal leverage regulation (lower right subplot). The positive spread is driven by differences in the bond rates across the two experiments; deposit rates are identical because they equal the expected return on investments in the social planner’s problem (lower left subplot).

4.2.2 Variations in the Optimal Policies

We vary the financial regulatory bounds and the tax rates away from their optimal levels and evaluate the impact on the balance sheet composition of intermediaries, on asset returns, risk taking and welfare. Moreover, we use these numerical experiments to highlight similarities and differences between capital and leverage regulation.

Tables 3 and 4 report results from several experiments. The benchmark—labelled experiment 1 in the tables—is the economy calibrated as in Section 4.1, where the interest rate policy is chosen optimally, and $\eta^{CAP} = 0.08$, $\eta^{LEV} = 0$, $\tau = 0$ in line with the Basel II capital regulation. The optimal CAP and the optimal LEV experiments—labelled experiments 2 and 3 in the tables—are the two implementations of the social optimum discussed in Section 4.2.1. In addition, we conduct experiments in which we change the financial policies relative to the optimal CAP or optimal LEV experiments, while keeping the other policies at their optimal levels. For example, we keep $\frac{1}{p}$ and τ as in the optimal CAP experiment, but change the minimum regulatory capital, η^{CAP} , to 1 percent (experiment 2a) or 25 percent (experiment 2b). Or, we keep $\frac{1}{p}$ and η^{CAP} as in the optimal CAP experiment, but set taxes, τ , to zero (experiment 2c). Analogously, we change η^{LEV} to either 1 percent or 20 percent in experiments 3a and 3b, and set taxes to zero in experiment 3c.

Table 3 reports the intermediaries’ balance sheet composition before and after interbank market repo trades. Compared with the benchmark—which is calibrated to match an average equity to asset ratio of 19 percent—the optimal CAP and optimal LEV experiments have lower equity to asset ratios, due to the incorporation of profit taxes in the optimal toolkit. Indeed, experiments 2*c* and 3*c* with zero taxes have equity to asset ratios comparable to those in the benchmark economy. Although the initial asset composition of intermediaries varies across experiments, once repo trades take place, high-risk intermediaries invest a fairly constant fraction of their balance sheet in risky assets, i.e., $k_h/(z + d)$ is on average 84 percent in all experiments. As a result, the total amount of resources allocated to high-risk investments, k_h , and risk taking relative to the social planner depend on the size of the balance sheet.

We investigate our numerical results further by changing one financial policy tool at a time (i.e., either η^{CAP} or τ) away from its level in the optimal CAP experiment. Lowering the minimum regulatory capital to 1 percent in experiment 2*a* allows intermediaries to hold less equity, about 2 percent of liabilities, compared to about 8 percent in the optimal CAP experiment (Table 3). Given more deposits, the moral hazard of intermediaries is more pronounced and risk taking is about 1.8 percent higher relative to the social optimum (Table 4). Similarly, raising the minimum regulatory capital to 25 percent in experiment 2*b* causes welfare losses since risk taking is now 3.4 percent lower relative to the social optimum. Lastly, eliminating the profit tax in experiment 2*c* raises the returns to equity and the amount of equity on intermediaries’ balance sheet. Risk taking, welfare and the balance sheet composition of intermediaries are similar to those in the benchmark model (see Tables 3 and 4).

Next, we establish similarities and differences between capital and leverage regulations. A first difference between the financial policies is that changes in leverage regulation away from its optimal level have stronger effects on risk taking and welfare than do changes in capital regulation. To establish this result, we compare two sets of experiments. In

experiments *2a* and *3a*, we choose η^{CAP} and η^{LEV} so that equity represents about 2 percent of the intermediaries' balance sheet. In experiments *2b* and *3b*, we choose η^{CAP} and η^{LEV} so that equity represents about 15 percent of intermediaries' balance sheet. In each pair of experiments, it is important to keep the equity share comparable, since equity directly affects the moral hazard of intermediaries. Table 4 shows that bond returns under leverage regulation are higher than under capital regulation. In experiment *3a*, the higher bond returns lead intermediaries to expand their balance sheet and increase risk taking relative to experiment *2a*. To understand why, we rewrite the balance sheet of the financial sector as $Z + D = Z + D_h + D_g = Z + D_h + pB$. Equity and household deposits (not shown in Table 3) are comparable across experiments *2a* and *3a*. However, the higher returns under leverage regulation lead to a higher pB , and thus an expansion of the balance sheet and the total resources allocated to high-risk investments, k_h . Risk taking is 59 percent higher than the optimum in experiment *3a* and only 1.8 percent higher in experiment *2a* (Table 4). In contrast, in experiment *3b*, despite higher bond returns intermediaries purchase fewer bonds than in experiment *2b*. The reason is that government seigniorage from bond issuance, $R^d D_g - B = (R^d - 1/p) pB$, is negative in experiment *3b* because $R^d - 1/p$ is negative (Table 4). Bond purchases, the balance sheet of intermediaries and risk taking are all lower in experiment *3b* than in *2b*.

A second difference between the financial policies is that lowering taxes to zero has stronger effects on risk taking and welfare in the presence of leverage regulation (experiment *3c*) than in the presence of capital regulation (experiment *2c*). The intuition is comparable to that of experiments *2a* and *3a*. Namely, under leverage regulation (experiment *3c*), bond returns are higher and intermediaries buy more bonds, have larger balance sheets and engage in more risk taking than under capital regulation (experiment *2c*).

To show that the results in Tables 3 and 4 hold more generally, we consider a wide range of variations in η^{CAP} and η^{LEV} relative to their levels in the optimal CAP or optimal LEV experiments. Figure 4 reports welfare and risk taking relative to the social planner from

experiments where the value of the capital regulation bound, η^{CAP} , varies from 1 percent to 99 percent, while interest rate policy and taxes are maintained at their optimal CAP levels. Similarly, we perform experiments where η^{LEV} varies from 1 percent to 25 percent—which corresponds to an increase in intermediaries’ deposit to equity ratio (i.e., leverage) between 4 and 100—while interest rate policy and taxes are maintained at their optimal LEV levels.

The left subplots in Figure 4 show that small variations in η^{CAP} around its Basel III level of 10.5 percent have a small impact on risk taking and welfare. However, consistent with previous literature, large increases in η^{CAP} are very costly (Van den Heuvel (2009)). The right plots in Figure 4 show that changing the leverage regulation has a bigger impact on risk taking than changing the capital regulation, while the magnitude of welfare losses is considerably smaller. As expected, looser leverage constraints (e.g. η^{LEV} around 1 percent, or leverage around 100) increase intermediaries’ risk taking.

We conclude that changing financial policies away from their optimal levels affects the bond return, $\frac{1}{p}$, government seigniorage, $(R^d - 1/p) pB$, and the size of intermediaries’ balance sheet. Since intermediaries invest a fairly constant fraction of their balance sheet in risky projects, the size of the balance sheet ultimately determines risk taking and welfare relative to the social planner.

5 Conclusion

In this paper, we develop a model in which financial intermediaries’ risky investments (i.e., *risk taking*) over the business cycle may exceed the social optimum owing to limited liability and deposit insurance. Our main contribution is to characterize optimal policies that achieve efficient risk taking when the model is calibrated to the U.S. economy.

We show that the social optimum can be implemented in our calibrated economy either with (i) interest rate policy, capital regulation and profit taxes, or with (ii) interest rate policy, leverage regulation and profit taxes. Our model’s monetary and financial authorities

are consolidated and have the goal of maximizing households welfare. As a results, the optimal policies are interdependent. First, the level of interest rates depends on the financial regulation in place. Specifically, bond rates are higher in the implementation with leverage regulation because capital regulation distorts the equilibrium bond return, as it directly affects the asset composition of intermediaries. Second, there is a trade-off between profit taxes and the financial regulatory bounds. Lower taxes require tighter financial regulation constraints in order to implement the social optimum.

There are other interesting results regarding the optimal policies. Namely, all policies are countercyclical. Interest rates are higher during expansions; capital and leverage regulations bind in expansions and are relaxed during contractions; taxes are higher during expansions when moral hazard is elevated and intermediaries have incentives to engage in excessive risk taking. In addition, optimal leverage regulation imposes a stricter requirement on equity than the optimal capital regulation, allowing the implementation of the social optimum without explicit restrictions on the composition of assets of financial intermediaries.

We conduct additional experiments to evaluate the impact of deviating from the optimal policies. We find that variations in the capital requirement in the range contemplated by policymakers have a small impact on risk taking in the economy. However, variations in leverage regulation have a stronger impact on risk taking relative to comparable experiments with capital regulation, since bond returns are higher under leverage regulation. We conclude that leverage regulation is a promising alternative for controlling excessive risk taking of intermediaries, since it is easier to implement in practice compared to capital regulation, which requires assessing the riskiness of all assets on an intermediary's balance sheet.

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A Appendix: Proofs

To simplify notation in our derivations, we use subscript $t - 1$ as short-hand notation for dependence on history s^{t-1} . For example, we define $d_{t-1} \equiv d(s^{t-1})$ and $\tilde{b}_{j,t-1} \equiv \tilde{b}_j(s^{t-1})$. Moreover, we define $q_{j,t} \equiv q_j(s_t)$ but note that productivity depends only on the current realization of the aggregate shock.

Proof of Proposition 1.

In an interior competitive equilibrium, expected returns on deposits are positive and equal to the expected returns on financial equity (i.e., expected profits per unit of equity).

$$R_{t-1}^d \sum_{s^t | s^{t-1}} \lambda_t = \sum_{s^t | s^{t-1}} \lambda_t R_t^z = \sum_{s^t | s^{t-1}} \lambda_t \frac{1-\tau_{t-1}}{z_{t-1}} [\pi_h V_{h,t} + \pi_l V_{l,t}] > 0$$

Thus, some intermediary j makes strictly positive profits for some aggregate state s_t .

Using the result that wage rates equal the marginal product of labor and that $l_{j,t} = 1$ in equilibrium, equation (2) can be written as in equation (A.1), where notice that all variables except for $q_{j,t}$ depend on the shock from $t - 1$.

$$V_{j,t} = \max \left\{ \left[\begin{array}{l} (\theta + \alpha) q_{j,t} \left(k_{t-1} + \tilde{p}_{t-1} \tilde{b}_{j,t-1} \right)^\theta + q_{j,t} (1 - \delta) \left(k_{t-1} + \tilde{p}_{t-1} \tilde{b}_{j,t-1} \right) \\ + b_{t-1} - \tilde{b}_{j,t-1} - R_{t-1}^d d_{t-1} \end{array} \right], 0 \right\} \quad (\text{A.1})$$

The ranking of productivity levels and equation (A.1) imply that profits in a good state are at least as big as profits in a bad state: $V_{h,t}(\bar{s}) > V_{h,t}(\underline{s})$ and $V_{l,t}(\bar{s}) = V_{l,t}(\underline{s})$. Let $I_{j,t}$ be an indicator function that equals 1 if intermediary j 's gross profit, i.e., the term in the square bracket in equation (A.1), is positive. Then, either $I_{h,t}(\bar{s}) = 1$ or $I_{l,t}(\bar{s}) = 1$ or both. If low-risk intermediaries default in both states, there are no trades in the interbank market. We rule out this uninteresting case. It follows that, at least in the good aggregate state, there is no default: $I_{h,t}(\bar{s}) = I_{l,t}(\bar{s}) = 1$. Since $V_{l,t}(\bar{s}) = V_{l,t}(\underline{s})$, the low-risk intermediary does not default in the bad state, $I_{h,t}(\bar{s}) = I_{l,t}(\bar{s}) = I_{l,t}(\underline{s}) = 1$ for all t . Lastly, in a bad aggregate state, high-risk intermediaries may either default, or not, $I_{h,t}(\underline{s}) \in \{0, 1\}$.

Proof of Proposition 2.

(i) Let superscript SP index variables that pertain to the social planner's problem. If the competitive equilibrium allocation coincides with the social optimum then: $C_t = C_t^{SP}$, $k_{j,t-1} = k_{t-1} + \tilde{p}_{t-1} \tilde{b}_{j,t-1} = k_{j,t-1}^{SP}$ for $j \in \{h, l\}$, and $k_{m,t-1} = k_{m,t-1}^{SP}$. Comparing first order conditions in the two environments, we find $\lambda_t = \lambda_t^{SP}$, as well as equation (A.2).

$$\begin{aligned} \lambda_{t-1} &= \beta R_{t-1}^d \sum_{s^t | s^{t-1}} \lambda_t = \beta \sum_{s^t | s^{t-1}} \lambda_t^{SP} q_{j,t} \theta (k_{j,t-1})^{\theta-1} = \lambda_{t-1}^{SP} \text{ for } j \in \{h, l\} \\ 0 &= \sum_{s^t | s^{t-1}} \lambda_t^{SP} \left[q_{j,t} \theta (k_{j,t-1}^{SP})^{\theta-1} - R_{t-1}^d \right] \text{ for } j \in \{h, l\} \end{aligned} \quad (\text{A.2})$$

Dividing by λ_{t-1}^{SP} and using $\frac{\lambda_t^{SP}}{\lambda_{t-1}^{SP}} = \frac{\lambda_t}{\lambda_{t-1}} = \varphi(s^t|s^{t-1}) = \varphi(s_t)$, equation (A.2) becomes:

$$0 = \sum_{s^t|s^{t-1}} \varphi(s_t) \left[q_{j,t} \theta (k_{j,t-1}^{SP})^{\theta-1} - R_{t-1}^d \right] \text{ for } j \in \{h, l\} \quad (\text{A.3})$$

Using $\lambda_t = \lambda_t^{SP}$, $k_{j,t-1} = k_{j,t-1}^{SP}$ and the assumption that there is no bankruptcy in the competitive equilibrium, i.e., $I_j(s_t) = 1$ for all j and for all s_t , an intermediary's first order condition with respect to d_{t-1} becomes:

$$(1 - \tau_{t-1}) \cdot \sum_{j \in \{h, l\}} \pi_j \sum_{s^t|s^{t-1}} \lambda_t^{SP} \left[q_{j,t} \theta (k_{j,t-1}^{SP})^{\theta-1} - R_{t-1}^d \right] = \zeta_{t-1}^{CAP} \eta_{t-1}^{CAP} + \zeta_{t-1}^{LEV} \eta_{t-1}^{LEV} \quad (\text{A.4})$$

Comparing (A.2) and (A.4), it follows that an equilibrium implements the planner's allocation if $\zeta_{t-1}^{CAP} \eta_{t-1}^{CAP} + \zeta_{t-1}^{LEV} \eta_{t-1}^{LEV} = 0$. Since $\zeta_{t-1}^{CAP} \geq 0$, $\eta_{t-1}^{CAP} \geq 0$, $\zeta_{t-1}^{LEV} \geq 0$ and $\eta_{t-1}^{LEV} \geq 0$, it follows that either the capital and leverage regulations are absent ($\eta_{t-1}^{CAP} = \eta_{t-1}^{LEV} = 0$) or they do not bind ($\zeta_{t-1}^{CAP} = \zeta_{t-1}^{LEV} = 0$).

(ii) First, we show that in a competitive equilibrium in which capital regulation does not bind, the bond returns on the primary and the interbank market are equal, i.e., $\frac{1}{p_{t-1}} = \frac{1}{\tilde{p}_{t-1}}$.

The first order condition with respect to b_{t-1} is:

$$(1 - \tau_{t-1}) \left(1 - \frac{\tilde{p}_{t-1}}{p_{t-1}} \right) \cdot \Xi_t - \zeta_{t-1}^{CAP} \eta_{t-1}^{CAP} = 0 \quad (\text{A.5})$$

where $\Xi_t \equiv \sum_{j \in \{h, l\}} \pi_j \sum_{s^t|s^{t-1}} \frac{\lambda_t}{\lambda_{t-1}} I_{j,t} q_{j,t} \theta \left(z_{t-1} + d_{t-1} - p_{t-1} b_{t-1} + \tilde{p}_{t-1} \tilde{b}_{j,t-1} \right)^{\theta-1}$. Note that $\Xi_t > 0$, because not all intermediaries are bankrupt in equilibrium. Moreover, $\tau_{t-1} \in [0, 1)$. As a result, in the absence of capital regulation ($\eta_{t-1}^{CAP} = 0$), or if this regulation does not bind ($\zeta_{t-1}^{CAP} = 0$), the primary and interbank market bond prices are equated, $p_{t-1} = \tilde{p}_{t-1}$. In particular, since η_{t-1}^{LEV} does not enter equation (A.5), leverage regulation doesn't drive a wedge between p_{t-1} and \tilde{p}_{t-1} .

Next, we show that to implement the social optimum as a competitive equilibrium, the return on deposits and the interbank market bond return must satisfy, $R_{t-1}^d = \frac{1}{\tilde{p}_{t-1}}$.

The assumption that high-risk intermediaries have higher expected productivity (see assumption A1 (v)) means that low-risk intermediaries purchase bonds on the interbank market. Thus, $\tilde{b}_{l,t-1} < 0 < b_{t-1}$ and the complimentary slackness conditions imply that the collateral constraint does not bind for low-risk intermediaries, i.e. $\mu_{l,t-1} = 0$. Then, the first order condition with respect to $\tilde{b}_{l,t-1}$ becomes:

$$\frac{1 - \tau_{t-1}}{\lambda_{t-1}^{SP}} \sum_{s^t|s^{t-1}} \lambda_t^{SP} \left[q_{l,t} \theta (k_{l,t-1}^{SP})^{\theta-1} - \frac{1}{\tilde{p}_{t-1}} \right] = 0 \quad (\text{A.6})$$

where we have used $\lambda_t = \lambda_t^{SP}$, $k_{l,t} = k_{l,t}^{SP}$ and $I_{l,t} \equiv I_l(s_t) = 1$ for all s_t .

Combining (A.2) and (A.6) gives $R_{t-1}^d = \frac{1}{\tilde{p}_{t-1}}$. We have shown that $R_{t-1}^d = \frac{1}{\tilde{p}_{t-1}} = \frac{1}{p_{t-1}}$. Under assumptions A1, the households' first order conditions give $R_{t-1}^d = \frac{1}{\beta}$. Thus, $\frac{1}{p_{t-1}} = \frac{1}{\beta}$.

(iii) In an interior competitive equilibrium, expected returns on deposits are equal to the expected returns on financial equity (i.e., expected profits per unit of equity).

$$\begin{aligned} R_{t-1}^d \sum_{s^t|s^{t-1}} \lambda_t &= \sum_{s^t|s^{t-1}} \lambda_t \frac{1-\tau_{t-1}}{z_{t-1}} [\pi_h V_{h,t} + \pi_l V_{l,t}] \\ R_{t-1}^d \sum_{s^t|s^{t-1}} \lambda_t &= \sum_{s^t|s^{t-1}} \lambda_t \frac{1-\tau_{t-1}}{z_{t-1}} [\pi_h \theta q_{h,t} k_{h,t-1}^\theta + \pi_l \theta q_{l,t} k_{l,t-1}^\theta + b_{t-1} - R_{t-1}^d d_{t-1}] \end{aligned}$$

To obtain the last equation, we used the definition of $V_{j,t}$, the fact that $\pi_h + \pi_l = 1$, as well as the market clearing condition $\pi_h \tilde{b}_{h,t-1} + \pi_l \tilde{b}_{l,t-1} = 0$. Rearranging terms, we find:

$$\left(\frac{z_{t-1}}{1-\tau_{t-1}} + d_{t-1} \right) R_{t-1}^d \sum_{s^t|s^{t-1}} \lambda_t = \sum_{s^t|s^{t-1}} \lambda_t \left(\sum_{j \in \{h,l\}} \pi_j \theta q_{j,t} k_{j,t-1}^\theta \right) + b_{t-1} \sum_{s^t|s^{t-1}} \lambda_t$$

Next, use equation (A.2), that is: $R_{t-1}^d \sum_{s^t|s^{t-1}} \lambda_t = \sum_{s^t|s^{t-1}} \lambda_t \theta q_{j,t} k_{j,t-1}^{\theta-1}$, to write:

$$(\pi_h k_{h,t-1} + \pi_l k_{l,t-1}) R_{t-1}^d \sum_{s^t|s^{t-1}} \lambda_t = \pi_h \sum_{s^t|s^{t-1}} \lambda_t \theta q_{h,t} k_{h,t-1}^\theta + \pi_l \sum_{s^t|s^{t-1}} \lambda_t \theta q_{l,t} k_{l,t-1}^\theta$$

Thus, we find:

$$\begin{aligned} \left(\frac{z_{t-1}}{1-\tau_{t-1}} + d_{t-1} \right) R_{t-1}^d \sum_{s^t|s^{t-1}} \lambda_t &= (\pi_h k_{h,t-1} + \pi_l k_{l,t-1}) R_{t-1}^d \sum_{s^t|s^{t-1}} \lambda_t + b_{t-1} \sum_{s^t|s^{t-1}} \lambda_t \\ \frac{z_{t-1}}{1-\tau_{t-1}} + d_{t-1} &= \pi_h k_{h,t-1} + \pi_l k_{l,t-1} + \frac{1}{R_{t-1}^d} b_{t-1} \end{aligned}$$

As shown in (ii), to implement the social optimum as a competitive equilibrium, it must be that $R_{t-1}^d = \frac{1}{\tilde{p}_{t-1}}$. Moreover, as shown in (ii), when capital and leverage regulations do not bind, bond prices satisfy $\frac{1}{\tilde{p}_{t-1}} = \frac{1}{p_{t-1}}$. Thus, we get $\frac{z_{t-1}}{1-\tau_{t-1}} + d_{t-1} = \pi_h k_{h,t-1} + \pi_l k_{l,t-1} + p_{t-1} b_{t-1}$.

Moreover, $\pi_h k_{h,t-1} + \pi_l k_{l,t-1} = k_{t-1}$. Aggregating $k_{t-1} + p_{t-1} b_{t-1} = z_{t-1} + d_{t-1}$ yields $(1 - \pi_m) k_{t-1} + p_{t-1} B_{t-1} = Z_{t-1} + D_{h,t-1} + D_{g,t-1}$, or $(1 - \pi_m) k_{t-1} = Z_{t-1} + D_{h,t-1}$ and so:

$$\frac{z_{t-1}}{1-\tau_{t-1}} + d_{t-1} = k_{t-1} + p_{t-1} b_{t-1} = \frac{Z_{t-1} + D_{h,t-1}}{1-\pi_m} + \frac{p_{t-1} B_{t-1}}{1-\pi_m} = \frac{Z_{t-1} + D_{h,t-1} + D_{g,t-1}}{1-\pi_m} = z_{t-1} + d_{t-1}$$

Thus, $\tau_{t-1} = 0$.

(iv) Using equation (A.2) for $j \in \{h, l\}$, we find

$$\sum_{s^t|s^{t-1}} \lambda_t^{SP} q_{h,t} \theta (k_{h,t-1}^{SP})^{\theta-1} = \sum_{s^t|s^{t-1}} \lambda_t^{SP} q_{l,t} \theta (k_{l,t-1}^{SP})^{\theta-1}$$

As a result, equation (A.6) becomes (A.7).

$$\frac{1-\tau_{t-1}}{\lambda_{t-1}^{SP}} \sum_{s^t|s^{t-1}} \lambda_t^{SP} \left[q_{h,t} \theta (k_{h,t-1}^{SP})^{\theta-1} - \frac{1}{\tilde{p}_{t-1}} \right] = 0 \quad (\text{A.7})$$

The first order condition with respect to $\tilde{b}_{h,t-1}$ is (A.8).

$$(1 - \tau_{t-1}) \sum_{s^t|s^{t-1}} \frac{\lambda_t}{\lambda_{t-1}} \left[\tilde{p}_{t-1} q_{h,t} \theta (k_{h,t-1})^{\theta-1} - 1 \right] = \mu_{h,t-1} \quad (\text{A.8})$$

Since $\lambda_t = \lambda_t^{SP}$ and $k_{h,t-1} = k_{h,t-1}^{SP}$, equations (A.7) and (A.8) imply that $\mu_{h,t-1} = 0$. As shown in (ii) we also have $\mu_{l,t-1} = 0$, and thus the collateral constraints of the financial intermediaries do not bind.

(v) It is sufficient to derive conditions under which high-risk intermediaries do not go bankrupt in the event of a bad aggregate state. Then, as argued in Proposition 1, no intermediary goes bankrupt, i.e., $I_j(s_t) = 1$ for all $j \in \{h, l\}$ and for all $s_t \in \{\bar{s}, \underline{s}\}$.

Using equation (2), the condition $V_{h,t} \geq 0$ is equivalent to $\theta q_{h,t} k_{h,t-1}^\theta + b_{t-1} - \frac{1}{\tilde{p}_{t-1}} (k_{h,t-1} - k_{t-1}) - R_{t-1}^d d_{t-1} \geq 0$, where we have used the fact that $k_{h,t-1} = k_{t-1} + \tilde{p}_{t-1} \tilde{b}_{h,t-1}$. Let x_{t-1} be the fraction of resources an intermediary retains for risky investments in the primary market portfolio decision. Namely, $k_{t-1} = x_{t-1} (z_{t-1} + d_{t-1})$ and $p_{t-1} b_{t-1} = (1 - x_{t-1}) (z_{t-1} + d_{t-1})$. The no default condition for high-risk intermediaries is:

$$\theta q_{h,t} k_{h,t-1}^\theta - \frac{1}{\tilde{p}_{t-1}} k_{h,t-1} + \frac{1}{p_{t-1}} (1 - x_{t-1}) (z_{t-1} + d_{t-1}) + \frac{1}{\tilde{p}_{t-1}} x_{t-1} (z_{t-1} + d_{t-1}) - R_{t-1}^d d_{t-1} \geq 0 \quad (\text{A.9})$$

As shown in (iv), if a competitive equilibrium with no bankruptcy implements the social optimum, then $\tilde{b}_{j,t-1} < b_{t-1}$, and $\mu_{j,t-1} = 0$. Moreover, since $R_{t-1}^d = \frac{1}{p_{t-1}} = \frac{1}{\tilde{p}_{t-1}}$, equation (A.9) becomes: $\theta q_{h,t} k_{h,t-1}^\theta + R_{t-1}^d (z_{t-1} - k_{h,t-1}) \geq 0$.

The level of equity at which the high-risk intermediary doesn't go bankrupt is:

$$\begin{aligned} z_{t-1} &\geq k_{h,t-1} - \frac{1}{R_{t-1}^d} \theta q_{h,t} k_{h,t-1}^\theta \\ z_{t-1} &\geq k_{h,t-1} \left[1 - \tilde{p}_{t-1} \theta q_{h,t} k_{h,t-1}^{\theta-1} \right] \end{aligned} \quad (\text{A.10})$$

Assuming no bankruptcy, $I_j(s_t) = 1$ for all j and for all s_t , and using the result that $\mu_{j,t-1} = 0$, the first order condition with respect to $\tilde{b}_{j,t-1}$ can be written as:

$$k_{j,t-1} \equiv k_{t-1} + \tilde{p}_{t-1} \tilde{b}_{j,t-1} = \left[\frac{1}{\tilde{p}_{t-1} \theta} \cdot \frac{\sum_{s^t|s^{t-1}} \frac{\lambda_t}{\lambda_{t-1}}}{\sum_{s^t|s^{t-1}} \frac{\lambda_t}{\lambda_{t-1}} q_{j,t}} \right]^{\frac{1}{\theta-1}} = \left[\frac{1}{\tilde{p}_{t-1} \theta} \cdot \frac{1}{\phi q_j(\bar{s}) + (1-\phi) q_j(\underline{s})} \right]^{\frac{1}{\theta-1}}$$

where we have used $\frac{\lambda_t}{\lambda_{t-1}} = \varphi(s^t|s^{t-1}) = \varphi(s_t)$ and $\sum_{s^t|s^{t-1}} \varphi(s_t) = 1$.

Equation (A.10) becomes:

$$z_{t-1} \geq k_{h,t-1} \left[1 - \frac{q_h(s_t)}{\phi q_h(\bar{s}) + (1-\phi) q_h(\underline{s})} \right] \text{ for all } s_t \in \{\bar{s}, \underline{s}\} \quad (\text{A.11})$$

Using $q_h(\bar{s}) > q_h(\underline{s})$, the inequality in (A.11) becomes: $\frac{z_{t-1}}{k_{h,t-1}} \geq 1 - \frac{1}{\phi \frac{q_h(\bar{s})}{q_h(\underline{s})} + 1 - \phi}$.

Since high-risk intermediaries sell bonds on the interbank market, we have $k_{h,t-1} > k_{t-1}$ and thus $z_{t-1}/k_{t-1} > z_{t-1}/k_{h,t-1} \geq 1 - \frac{1}{\phi \frac{q_h(\bar{s})}{q_h(\underline{s})} + 1 - \phi}$.

Proof of Proposition 3.

First, we show that either binding capital regulation or binding leverage regulation are necessary to implement the social optimum as a competitive equilibrium with bankruptcy of high-risk intermediaries. Let $I_{j,t}$ be an indicator function which equals 1 if intermediary j 's gross profit at time t (i.e., the term in the square bracket in equation (A.1)) is positive. Assume that for some t , $I_{h,t}(\underline{s}) = 0$ and $I_{h,t}(\bar{s}) = I_{l,t}(\bar{s}) = I_{l,t}(\underline{s}) = 1$. The first order condition with respect to deposits evaluated at the optimal allocation (i.e., using $\lambda_t = \lambda_t^{SP}$ and $k_{j,t-1} = k_{j,t-1}^{SP}$) and using $\frac{\lambda_t}{\lambda_{t-1}} = \varphi(s^t | s^{t-1}) = \varphi(s_t)$, becomes:

$$\begin{aligned} \zeta_{t-1}^{CAP} \eta_{t-1}^{CAP} + \zeta_{t-1}^{LEV} \eta_{t-1}^{LEV} &= (1 - \tau_{t-1}) \pi_h \cdot \varphi(\bar{s}) \left[q_h(\bar{s}) \theta (k_{h,t-1}^{SP})^{\theta-1} - R_{t-1}^d \right] \\ &\quad + (1 - \tau_{t-1}) \pi_l \cdot \sum_{s^t | s^{t-1}} \frac{\lambda_t^{SP}}{\lambda_{t-1}^{SP}} \left[q_{l,t} \theta (k_{l,t-1}^{SP})^{\theta-1} - R_{t-1}^d \right] \\ \zeta_{t-1}^{CAP} \eta_{t-1}^{CAP} + \zeta_{t-1}^{LEV} \eta_{t-1}^{LEV} &= (1 - \tau_{t-1}) \pi_h \cdot \phi \left[q_h(\bar{s}) \theta (k_{h,t-1}^{SP})^{\theta-1} - R_{t-1}^d \right] \end{aligned} \quad (A.12)$$

where to obtain (A.12) we used (A.2) as well as $\varphi(\bar{s}) = \phi$.

Using (A.2) again for $j = h$, we can express R^d as below.

$$R_{t-1}^d = \frac{\sum_{s^t | s^{t-1}} \lambda_t^{SP} q_{h,t} \theta (k_{h,t-1}^{SP})^{\theta-1}}{\sum_{s^t | s^{t-1}} \lambda_t^{SP}} = \frac{\sum_{s^t | s^{t-1}} \frac{\lambda_t^{SP}}{\lambda_{t-1}^{SP}} q_{h,t} \theta (k_{h,t-1}^{SP})^{\theta-1}}{\sum_{s^t | s^{t-1}} \frac{\lambda_t^{SP}}{\lambda_{t-1}^{SP}}} = \sum_{s^t | s^{t-1}} \varphi(s_t) q_{h,t} \theta (k_{h,t-1}^{SP})^{\theta-1}$$

With this expression for R_{t-1}^d , equation (A.12) simplifies further as shown below.

$$\frac{\zeta_{t-1}^{CAP} \eta_{t-1}^{CAP} + \zeta_{t-1}^{LEV} \eta_{t-1}^{LEV}}{(1 - \tau_{t-1}) \pi_h \cdot \phi} = (1 - \phi) \theta (k_{h,t-1}^{SP})^{\theta-1} [q_h(\bar{s}) - q_h(\underline{s})] > 0$$

Thus, $\zeta_{t-1}^{CAP} \eta_{t-1}^{CAP} + \zeta_{t-1}^{LEV} \eta_{t-1}^{LEV} > 0$, which means that to implement the social optimum in an equilibrium with bankruptcy, either the capital regulation binds ($\zeta_{t-1}^{CAP} > 0$) or the leverage regulation binds ($\zeta_{t-1}^{LEV} > 0$), or both.

Next, we show that interest rate policy $\frac{1}{p_{t-1}} < \frac{1}{\beta}$, binding capital regulation, i.e., $z_{t-1} = \eta_{t-1}^{CAP} k_{t-1}$, and a profit tax, $\tau_{t-1} \geq 0$, implement the social optimum as a competitive equilibrium with bankruptcy. Moreover, we show there is a trade-off between capital regulation and taxes, i.e., $\frac{\partial \eta_{t-1}^{CAP}}{\partial \tau_{t-1}} < 0$. If tax rates are low, the minimum regulatory capital necessary to implement the social optimum is high.

If capital regulation binds, equation (A.5) implies that $\frac{1}{p_{t-1}} < \frac{1}{\bar{p}_{t-1}}$. Moreover, the proof of Proposition 2 shows that in order to implement the social optimum as a competitive equilibrium, we must have $R_{t-1}^d = \frac{1}{\bar{p}_{t-1}} = \frac{1}{\beta}$. Thus, with binding capital regulation in place, the interest rate policy satisfies $\frac{1}{p_{t-1}} < \frac{1}{\beta}$.

In an interior equilibrium, expected returns on deposits and financial equity are equated.

$$R_{t-1}^d \sum_{s^t | s^{t-1}} \lambda_t = \sum_{s^t | s^{t-1}} \lambda_t R_t^z = \sum_{s^t | s^{t-1}} \lambda_t \frac{1 - \tau_{t-1}}{z_{t-1}} [\pi_h V_{h,t} + \pi_l V_{l,t}] > 0$$

Dividing both sides by λ_{t-1} , and using $\frac{\lambda_t}{\lambda_{t-1}} = \varphi(s^t|s^{t-1}) = \varphi(s_t)$ and $\sum_{s^t|s^{t-1}} \varphi(s_t) = 1$, we find: $R_{t-1}^d = \sum_{s^t|s^{t-1}} \varphi(s_t) \frac{1-\tau_{t-1}}{z_{t-1}} [\pi_h V_{h,t} + \pi_l V_{l,t}]$.

Using $I_h(\underline{s}) = 0$ and $I_h(\bar{s}) = I_l(\bar{s}) = I_l(\underline{s}) = 1$, $\tilde{b}_{h,t-1} = b_{t-1}$ and $\tilde{b}_{l,t-1} = -\frac{\pi_h}{\pi_l} b_{t-1}$, and evaluating the expression at the optimal allocation (i.e., using $k_{j,t-1} = k_{j,t-1}^{SP}$), we find:

$$\begin{aligned} R_{t-1}^d &= \frac{1-\tau_{t-1}}{z_{t-1}} \cdot \varphi(\bar{s}) \pi_h \left[\theta q_h(\bar{s}) (k_{h,t-1}^{SP})^\theta - R_{t-1}^d d_{t-1} \right] \\ &\quad + \frac{1-\tau_{t-1}}{z_{t-1}} \cdot \sum_{s^t|s^{t-1}} \varphi(s_t) \pi_l \left[\theta q_l(s_t) (k_{l,t-1}^{SP})^\theta + \frac{b_{t-1}}{\pi_l} - R_{t-1}^d d_{t-1} \right] \end{aligned} \quad (A.13)$$

As shown in the proof of Proposition 2, in order to implement the social optimum as a competitive equilibrium, we must have $R_{t-1}^d = \frac{1}{\tilde{p}_{t-1}} = \frac{1}{\beta}$. Then,

$$b_{t-1} = \frac{k_{h,t-1} - k_{l,t-1}}{\tilde{p}_{t-1}} = \frac{k_{h,t-1} - (\pi_h k_{h,t-1} + \pi_l k_{l,t-1})}{\tilde{p}_{t-1}} = R_{t-1}^d \pi_l (k_{h,t-1}^{SP} - k_{l,t-1}^{SP})$$

Using (A.2), and the equation above, (A.13) becomes:

$$\begin{aligned} \frac{z_{t-1}}{1-\tau_{t-1}} R_{t-1}^d &= \varphi(\bar{s}) \pi_h \left[\theta q_h(\bar{s}) (k_{h,t-1}^{SP})^\theta - R_{t-1}^d d_{t-1} \right] + k_{l,t-1}^{SP} \pi_l R_{t-1}^d \sum_{s^t|s^{t-1}} \varphi(s_t) \\ &\quad + \pi_l R_{t-1}^d (k_{h,t-1}^{SP} - k_{l,t-1}^{SP}) \sum_{s^t|s^{t-1}} \varphi(s_t) - \pi_l R_{t-1}^d d_{t-1} \sum_{s^t|s^{t-1}} \varphi(s_t) \\ &= \varphi(\bar{s}) \pi_h \left[\theta q_h(\bar{s}) (k_{h,t-1}^{SP})^\theta - R_{t-1}^d d_{t-1} \right] + \pi_l R_{t-1}^d (k_{h,t-1}^{SP} - d_{t-1}) \end{aligned}$$

where we have used $\sum_{s^t|s^{t-1}} \varphi(s_t) = 1$. Divide by $R_{t-1}^d = \frac{1}{\beta}$ and use $\varphi(\bar{s}) = \phi$ to get:

$$\begin{aligned} \frac{z_{t-1}}{1-\tau_{t-1}} &= \phi \pi_h \left[\beta \theta q_h(\bar{s}) (k_{h,t-1}^{SP})^\theta - d_{t-1} \right] + \pi_l (k_{h,t-1}^{SP} - d_{t-1}) \\ \frac{z_{t-1}}{1-\tau_{t-1}} &= k_{h,t-1}^{SP} \left[\phi \pi_h q_h(\bar{s}) \beta \theta (k_{h,t-1}^{SP})^{\theta-1} + \pi_l \right] - (\phi \pi_h + \pi_l) d_{t-1} \end{aligned}$$

Using $k_{h,t-1}^{1-\theta} = \beta \theta [\phi q_h(\bar{s}) + (1-\phi) q_h(\underline{s})]$ we find

$$\frac{z_{t-1}}{1-\tau_{t-1}} = k_{h,t-1}^{SP} \left[\phi \pi_h \frac{q_h(\bar{s})}{\phi q_h(\bar{s}) + (1-\phi) q_h(\underline{s})} + \pi_l \right] - (\phi \pi_h + \pi_l) d_{t-1} \quad (A.14)$$

Using $k_{h,t-1}^{SP} = z_{t-1} + d_{t-1}$ and $z_{t-1} = \eta_{t-1}^{CAP} k_{t-1}$, we find

$$\begin{aligned} \frac{\eta_{t-1}^{CAP} k_{t-1}}{1-\tau_{t-1}} &= k_{h,t-1}^{SP} \left[\phi \pi_h \frac{q_h(\bar{s})}{\phi q_h(\bar{s}) + (1-\phi) q_h(\underline{s})} + \pi_l \right] - (\phi \pi_h + \pi_l) (k_{h,t-1}^{SP} - \eta_{t-1}^{CAP} k_{t-1}) \\ &= k_{h,t-1}^{SP} \left[\phi \pi_h \frac{q_h(\bar{s})}{\phi q_h(\bar{s}) + (1-\phi) q_h(\underline{s})} - \phi \pi_h \right] + (\phi \pi_h + \pi_l) \eta_{t-1}^{CAP} k_{t-1} \\ &= \phi \pi_h k_{h,t-1}^{SP} \cdot \frac{(1-\phi)[q_h(\bar{s}) - q_h(\underline{s})]}{\phi q_h(\bar{s}) + (1-\phi) q_h(\underline{s})} + (\phi \pi_h + \pi_l) \eta_{t-1}^{CAP} k_{t-1} \end{aligned}$$

Simplifying, we find

$$\frac{1}{1-\tau_{t-1}} = \pi_l + \phi\pi_h + \frac{\pi_h k_{h,t-1}^{SP}}{k_{t-1}} \cdot \frac{\phi(1-\phi)[q_h(\bar{s})-q_h(\underline{s})]}{\phi q_h(\bar{s})+(1-\phi)q_h(\underline{s})} \frac{1}{\eta_{t-1}^{CAP}}$$

Using $k_{j,t-1}^{1-\theta} = \beta\theta [\phi q_j(\bar{s}) + (1-\phi)q_j(\underline{s})]$ and also $k_{t-1} = \pi_h k_{h,t-1} + \pi_l k_{l,t-1}$ we find

$$\frac{1}{1-\tau_{t-1}} = \pi_l + \phi\pi_h + \frac{\phi(1-\phi)[q_h(\bar{s})-q_h(\underline{s})]}{\phi q_h(\bar{s})+(1-\phi)q_h(\underline{s})} \cdot \frac{\pi_h [\phi q_h(\bar{s})+(1-\phi)q_h(\underline{s})]^{\frac{1}{1-\theta}}}{\sum_j \pi_j [\phi q_j(\bar{s})+(1-\phi)q_j(\underline{s})]^{\frac{1}{1-\theta}}} \cdot \frac{1}{\eta_{t-1}^{CAP}}$$

Equivalently, $\frac{1}{1-\tau_{t-1}} = Q_1^{CAP} + Q_2^{CAP} \frac{1}{\eta_{t-1}^{CAP}}$, where the coefficients depend on parameters,

$$Q_1^{CAP} = \pi_l + \phi\pi_h \in (0, 1) \text{ and } Q_2^{CAP} = \phi\pi_h (1-\phi) [q_h(\bar{s}) - q_h(\underline{s})] \cdot \frac{[\phi q_h(\bar{s})+(1-\phi)q_h(\underline{s})]^{\frac{\theta}{1-\theta}}}{\sum_j \pi_j [\phi q_j(\bar{s})+(1-\phi)q_j(\underline{s})]^{\frac{1}{1-\theta}}}.$$

Since $Q_1^{CAP} > 0$ and $Q_2^{CAP} > 0$, it is easy to see that $\frac{\partial \eta_{t-1}^{CAP}}{\partial \tau_{t-1}} < 0$. In particular, if taxes are eliminated, i.e., $\tau_{t-1} = 0$, the minimum regulatory capital is higher, i.e., $\eta_{t-1}^{CAP} = \frac{Q_2^{CAP}}{1-Q_1^{CAP}}$.

Next, we show that interest rate policy $\frac{1}{p_{t-1}} = \frac{1}{\beta}$, binding leverage regulation, i.e., $z_{t-1} = \eta_{t-1}^{LEV} d_{t-1}$, and a profit tax, i.e., $\tau_{t-1} \geq 0$, implement the social optimum as a competitive equilibrium with bankruptcy. Moreover, we show there is a trade-off between leverage regulation and taxes, i.e., $\frac{\partial \eta_{t-1}^{LEV}}{\partial \tau_{t-1}} < 0$. If tax rates are low, the maximum regulatory leverage, $1/\eta_{t-1}^{LEV}$, necessary to implement the social optimum is low.

If leverage regulation binds, equation (A.5) implies that $\frac{1}{p_{t-1}} = \frac{1}{\bar{p}_{t-1}}$. Moreover, the proof of Proposition 2 shows that in order to implement the social optimum as a competitive equilibrium, we must have $R_{t-1}^d = \frac{1}{\bar{p}_{t-1}} = \frac{1}{\beta}$. Thus, with binding leverage regulation in place, the interest rate policy satisfies $\frac{1}{p_{t-1}} = \frac{1}{\beta}$.

Equation (A.14) becomes:

$$\frac{\eta_{t-1}^{LEV} d_{t-1}}{1-\tau_{t-1}} = k_{h,t-1}^{SP} \left[\phi\pi_h \frac{q_h(\bar{s})}{\phi q_h(\bar{s})+(1-\phi)q_h(\underline{s})} + \pi_l \right] - (\phi\pi_h + \pi_l) d_{t-1}$$

Using $k_{h,t-1}^{SP} = z_{t-1} + d_{t-1} = \eta_{t-1}^{LEV} d_{t-1} + d_{t-1}$ and dividing by $\eta_{t-1}^{LEV} d_{t-1}$ we find

$$\begin{aligned} \frac{1}{1-\tau_{t-1}} &= \frac{\eta_{t-1}^{LEV} d_{t-1} + d_{t-1}}{\eta_{t-1}^{LEV} d_{t-1}} \left[\phi\pi_h \frac{q_h(\bar{s})}{\phi q_h(\bar{s})+(1-\phi)q_h(\underline{s})} + \pi_l \right] - (\phi\pi_h + \pi_l) \frac{d_{t-1}}{\eta_{t-1}^{LEV} d_{t-1}} \\ &= \left(1 + \frac{1}{\eta_{t-1}^{LEV}} \right) \left[\phi\pi_h \frac{q_h(\bar{s})}{\phi q_h(\bar{s})+(1-\phi)q_h(\underline{s})} + \pi_l \right] - (\phi\pi_h + \pi_l) \frac{1}{\eta_{t-1}^{LEV}} \\ &= \pi_l + \phi\pi_h \frac{q_h(\bar{s})}{\phi q_h(\bar{s})+(1-\phi)q_h(\underline{s})} + \frac{\phi\pi_h(1-\phi)[q_h(\bar{s})-q_h(\underline{s})]}{\phi q_h(\bar{s})+(1-\phi)q_h(\underline{s})} \frac{1}{\eta_{t-1}^{LEV}} \end{aligned}$$

Equivalently, $\frac{1}{1-\tau_{t-1}} = Q_1^{LEV} + Q_2^{LEV} \cdot \frac{1}{\eta_{t-1}^{LEV}}$, where $Q_1^{LEV} = \pi_l + \phi\pi_h \frac{q_h(\bar{s})}{\phi q_h(\bar{s})+(1-\phi)q_h(\underline{s})} > 0$ and $Q_2^{LEV} = \frac{\phi\pi_h(1-\phi)[q_h(\bar{s})-q_h(\underline{s})]}{\phi q_h(\bar{s})+(1-\phi)q_h(\underline{s})} > 0$. It is easy to see that $\frac{\partial \eta_{t-1}^{LEV}}{\partial \tau_{t-1}} < 0$. In particular, if taxes are eliminated, i.e., $\tau_{t-1} = 0$, the maximum regulatory leverage is lower, i.e., $\frac{1}{\eta_{t-1}^{LEV}} = \frac{1-Q_1^{LEV}}{Q_2^{LEV}}$.

Lastly, we show that the collateral constraint of high-risk intermediaries binds. Using $\frac{\lambda_t}{\lambda_{t-1}} = \varphi(s^t|s^{t-1}) = \varphi(s_t)$, Equation (A.7) can be restated as:

$$\tilde{p}_{t-1} = \frac{1}{\theta (k_{h,t-1}^{SP})^{\theta-1} [\phi q_h(\bar{s}) + (1-\phi) q_h(\underline{s})]} = \beta$$

where the result $\tilde{p}_{t-1} = \beta$ has been shown in the proof of Proposition 2.

Given bankruptcy patterns, i.e. $I_{h,t}(\bar{s}) = 1$ and $I_{h,t}(\underline{s}) = 0$, and using $\tilde{p}_{t-1} = \beta$ and $(k_{h,t-1}^{SP})^{1-\theta} = \theta\beta [\phi q_h(\bar{s}) + (1-\phi) q_h(\underline{s})]$, the first order condition for $\tilde{b}_{h,t-1}$ becomes

$$\begin{aligned} \frac{\mu_{h,t-1}}{\varphi(\bar{s})(1-\tau_{t-1})} &= \tilde{p}_{t-1} q_h(\bar{s}) \theta (k_{h,t-1}^{SP})^{\theta-1} - 1 = \frac{q_h(\bar{s})}{[\phi q_h(\bar{s}) + (1-\phi) q_h(\underline{s})]} - 1 \\ &= \frac{(1-\phi)[q_h(\bar{s}) - q_h(\underline{s})]}{\phi q_h(\bar{s}) + (1-\phi) q_h(\underline{s})} > 0 \end{aligned}$$

Thus, $\mu_{h,t-1} > 0$ which means the collateral constraint of high-risk intermediaries binds.

Proof of Proposition 4.

First, we prove that financial regulations bind in good aggregate states, i.e., at all t such that $s_t = \bar{s}$. Given the assumption that high-risk intermediaries are bankrupt at $t+1$ if $s_{t+1} = \underline{s}$, the first order condition with respect to deposits evaluated at the optimal allocation is similar to equation (A.12) in Proposition 3.

$$\frac{\zeta_t^{CAP} \eta_t^{CAP} + \zeta_t^{LEV} \eta_t^{LEV}}{(1-\tau_t)\pi_h \lambda_{t+1}^{SP}(\bar{s})} = q_h(\bar{s}) \left[\theta (k_{h,t}^{SP})^{\theta-1} + 1 - \delta \right] - R_t^d$$

where $\lambda_{t+1}^{SP}(\bar{s}) \equiv \lambda^{SP}(s^{t+1}|s_{t+1} = \bar{s})$.

Moreover, similar to Proposition 3, $R_t^d = \left[\theta (k_{h,t}^{SP})^{\theta-1} + 1 - \delta \right] \cdot \frac{\sum_{s^{t+1}|s^t} \lambda_{t+1}^{SP} q_{h,t+1}}{\sum_{s^{t+1}|s^t} \lambda_{t+1}^{SP}}$.

Combining the two equations we find

$$\begin{aligned} \frac{\zeta_t^{CAP} \eta_t^{CAP} + \zeta_t^{LEV} \eta_t^{LEV}}{(1-\tau_t)\pi_h \lambda_{t+1}^{SP}(\bar{s})} &= \left[\theta (k_{h,t}^{SP})^{\theta-1} + 1 - \delta \right] \left[q_h(\bar{s}) - \frac{\lambda_{t+1}^{SP}(\bar{s}) q_h(\bar{s}) + \lambda_{t+1}^{SP}(\underline{s}) q_h(\underline{s})}{\lambda_{t+1}^{SP}(\bar{s}) + \lambda_{t+1}^{SP}(\underline{s})} \right] \\ &= \left[\theta (k_{h,t}^{SP})^{\theta-1} + 1 - \delta \right] \frac{\lambda_{t+1}^{SP}(\underline{s}) [q_h(\bar{s}) - q_h(\underline{s})]}{\lambda_{t+1}^{SP}(\bar{s}) + \lambda_{t+1}^{SP}(\underline{s})} > 0 \end{aligned}$$

Thus, to implement the social optimum in good aggregate states, either the capital regulation binds ($\zeta_{t-1}^{CAP} > 0$) or the leverage regulation binds ($\zeta_{t-1}^{LEV} > 0$), or both.

Next, suppose the social optimum in good aggregate states is implemented with binding capital regulation. Similar to equation (A.13) in Proposition 3, we can show that:

$$\begin{aligned} \frac{1}{1-\tau_t} &= \frac{1}{z_t R_t^d} \sum_{s^{t+1}|s^t} \lambda_{t+1} \pi_h \left\{ q_h(\bar{s}) \left[(\theta + \alpha) (k_{h,t})^\theta + (1-\delta) k_{h,t} \right] - R_t^d d_t \right\} \\ &\quad + \frac{1}{z_t R_t^d} \sum_{s^{t+1}|s^t} \lambda_{t+1} \pi_l \left[q_{l,t+1} \left[(\theta + \alpha) (k_{l,t})^\theta + (1-\delta) k_{l,t} \right] + \frac{b_t}{\pi_l} - R_t^d d_t \right] \end{aligned}$$

Next, we transform this equation using $z_t = k_t \eta_t^{CAP}$, $\frac{d_t}{z_t} = \frac{k_{h,t} - k_t \eta_t^{CAP}}{k_t \eta_t^{CAP}} = \frac{k_{h,t}}{k_t \eta_t^{CAP}} - 1$, the households first order condition $R_t^d \sum_{s^{t+1}|s^t} \lambda_{t+1} = \frac{\lambda_t}{\beta}$, the fact that $b_t = \frac{k_{h,t} - k_t}{\tilde{p}_t}$, and the expression for $\tilde{p}_t = \frac{\sum_{s^{t+1}|s^t} \lambda_{t+1}}{[\theta(k_{i,t}^{SP})^{\theta-1} + 1 - \delta] \cdot \sum_{s^{t+1}|s^t} \lambda_{t+1} q_{l,t+1}}$ (derived from the first order condition with respect to $\tilde{b}_{l,t}$). We obtain:

$$\begin{aligned}
\frac{1}{1-\tau_t} &= \frac{\lambda_{t+1}(\bar{s}) + \lambda_{t+1}(s) \pi_l}{\sum_{s^{t+1}|s^t} \lambda_{t+1}} - \frac{\lambda_{t+1}(\bar{s}) + \lambda_{t+1}(s) \pi_l}{\sum_{s^{t+1}|s^t} \lambda_{t+1}} \cdot \frac{k_{h,t}}{k_t} \cdot \frac{1}{\eta_t^{CAP}} \\
&+ \frac{\beta \lambda_{t+1}(\bar{s})}{\lambda_t} \cdot \frac{1}{k_t} \sum_{j \in \{h,l\}} \pi_j q_j(\bar{s}) \left[(\theta + \alpha) (k_{j,t})^\theta + (1 - \delta) k_{j,t} \right] \cdot \frac{1}{\eta_t^{CAP}} \\
&+ \frac{\beta \lambda_{t+1}(s)}{\lambda_t} \cdot \frac{1}{k_t} \pi_l q_l(s) \left[(\theta + \alpha) (k_{l,t})^\theta + (1 - \delta) k_{l,t} \right] \cdot \frac{1}{\eta_t^{CAP}} \\
&+ \frac{\beta}{\lambda_t} \cdot \left[\left[\theta (k_{l,t})^{\theta-1} + 1 - \delta \right] \cdot \sum_{s^{t+1}|s^t} \lambda_{t+1} q_{l,t+1} \right] \left(\frac{k_{h,t}}{k_t} - 1 \right) \cdot \frac{1}{\eta_t^{CAP}}
\end{aligned} \tag{A.15}$$

Note that equation (A.15) takes the form $\frac{1}{1-\tau_t} = Q_{1,t}^{CAP} + Q_{2,t}^{CAP} \cdot \frac{1}{\eta_t^{CAP}}$.

Next, suppose the social optimum in good aggregate states is implemented with binding leverage regulation. Going through similar steps as the ones above, we can show that $\frac{1}{1-\tau_t} = Q_{1,t}^{LEV} + Q_{2,t}^{LEV} \cdot \frac{1}{\eta_t^{LEV}}$.

Proof of Proposition 5.

Given the assumption that no intermediary is bankrupt at $t+1$ for any $s_{t+1} \in \{\bar{s}, \underline{s}\}$, the first order condition with respect to deposits evaluated at the optimal allocation is:

$$\zeta_t^{CAP} \eta_t^{CAP} + \zeta_t^{LEV} \eta_t^{LEV} = (1 - \tau_t) \sum_{j \in \{h,l\}} \pi_j \sum_{s^{t+1}|s^t} \lambda_{t+1} \left\{ q_{j,t+1} \left[\theta (k_{j,t})^{\theta-1} + 1 - \delta \right] - R_t^d \right\}$$

If the competitive equilibrium allocation coincides with the social optimum, then the first order conditions in these two environments yield $\sum_{s^{t+1}|s^t} \lambda_{t+1} \left[q_{j,t+1} \left(\theta (k_{j,t})^{\theta-1} + 1 - \delta \right) - R_t^d \right] = 0$ for any $j \in \{h, l\}$. Thus, we find that $\zeta_t^{CAP} \eta_t^{CAP} + \zeta_t^{LEV} \eta_t^{LEV} = 0$, i.e., financial regulations do not bind in a bad aggregate state.

Table 1: CALIBRATED PARAMETERS

Parameter/Value	Moment ¹
$\beta = \left(\frac{1}{1.04}\right)^{1/4}$	Annual real interest rate of 4 percent
$\theta = 0.29$	Average capital income share for U.S. business sector, 1948–2014
$\Phi = \begin{bmatrix} 0.950 & 0.050 \\ 0.256 & 0.744 \end{bmatrix}$	Average length and number of expansions and contractions of U.S. business sector, 1947Q1–2015Q2
$\pi_h = 0.15, \pi_l = 0.85$	Share of financial assets of brokers and dealers, 1987Q1–2015Q2

¹Sources of data: U.S. National Income and Product Accounts and U.S. Flow of Funds accounts. For more details, see Cociuba, Shukayev, and Ueberfeldt (2016).

Table 2: ESTIMATED PARAMETERS

PANEL A

PARAMETER	VALUE
Share of nonfinancial firms	$\pi_m = 0.6632$
Fixed factor income share	$\alpha = 0.0002$
Depreciation rate	$\delta = 0.0257$
Productivity parameters	
nonfinancial firms	$q_m(\bar{s}) = 0.98608$
	$q_m(\underline{s}) = 0.94955$
low-risk financial firms	$q_l(\bar{s}) = 0.94968$
	$q_l(\underline{s}) = 0.94957$
high-risk financial firms	$q_h(\bar{s}) = 1$
	$q_h(\underline{s}) = 0.38221$

PANEL B

MOMENTS TARGETED ¹	Data ⁴ (in %)	Model (in %)
Average value added share of corporate nonfinancial sector	67.6	70.8
Average equity to asset ratio of the financial sector	23.0	19.0
Average capital depreciation rate in economy	2.5	2.5
Average peak-to-trough decline in output during contractions ²	6.4	7.7
Coefficient of variation of output ³	4.6	3.9
Coefficient of variation of household net worth ³	8.5	8.6
Average deposits over total household financial assets	16.4	17.5
Recovery rate in bankruptcy	42.0	42.0

¹Sources of data: U.S. National Income and Product Accounts and U.S. Flow of Funds accounts. The recovery rate in bankruptcy is from Acharya, Bharath, and Srinivasan (2003).

²Total output is measured as the real value added for the U.S. business sector. We detrend output by the average growth rate over the period 1947Q1–2015Q2. ³We calculate statistic after detrending the variable by the average growth rate over the period 1987Q1–2015Q2.

⁴For more details on the data moments, see Cociuba, Shukayev, and Ueberfeldt (2016).

Table 3: FINANCIAL INTERMEDIARIES' BALANCE SHEETS BEFORE AND AFTER REPO TRADES

	BALANCE SHEET								
	SIZE ⁷	COMPOSITION (in %)				ASSETS			
		LIABILITIES		ASSETS BEFORE REPOS		ASSETS AFTER REPOS			
$Z + D$	$\frac{z}{z+d}$	$\frac{d}{z+d}$	$\frac{k}{z+d}$	$\frac{pb}{z+d}$	$\frac{k_b}{z+d}$	$\frac{pb-\tilde{p}\tilde{b}_h}{z+d}$	$\frac{k_l}{z+d}$	$\frac{pb-\tilde{p}\tilde{b}_l}{z+d}$	
EXPERIMENT ¹									
1. Benchmark ²	101.8	19.0	81.0	78.6	21.4	84.3	15.7	77.6	22.4
2. Optimal CAP ³ : $\left(\frac{1}{p}, \eta^{CAP}, \tau\right)$	100.0	7.8	92.2	75.7	24.3	84.2	15.8	74.2	25.8
a. Lower η^{CAP} to 1 percent ⁴	101.8	1.9	98.1	78.8	21.2	84.3	15.7	77.8	22.2
b. Raise η^{CAP} to 25 percent ⁵	96.5	15.9	84.1	72.2	27.8	84.0	16.0	70.1	29.9
c. Lower τ to zero ⁶	101.7	20.6	79.4	78.5	21.5	84.3	15.7	77.5	22.6
3. Optimal LEV ³ : $\left(\frac{1}{p}, \eta^{LEV}, \tau\right)$	100.0	9.9	90.1	75.8	24.2	84.3	15.7	74.3	25.7
a. Lower η^{LEV} to 1 percent ⁴	160.1	2.1	97.9	55.9	44.1	84.3	15.7	50.9	49.1
b. Raise η^{LEV} to 20 percent ⁵	77.5	15.3	84.7	93.1	6.9	84.3	15.7	94.6	5.4
c. Lower τ to zero ⁶	153.4	22.5	77.5	57.3	42.7	84.3	15.7	52.5	47.5

¹All statistics are averages over simulations of 5,000 periods. ²The benchmark experiment has an optimally chosen interest rate policy, and $\eta^{CAP} = 0.08$, $\eta^{LEV} = 0$, $\tau = 0$. ³Optimal CAP implements the social optimum with interest rate policy, taxes and capital regulation. Optimal LEV is defined analogously, with leverage regulation instead of capital regulation. ⁴Financial regulation bounds, η^{CAP} or η^{LEV} , are lowered to 0.01, while interest rate policy and taxes are as in the optimal CAP/LEV experiments. ⁵The regulation bounds are either $\eta^{CAP} = 0.25$ or $\eta^{LEV} = 0.2$, while interest rate policy and taxes are as in the optimal CAP/LEV experiments. ⁶Taxes are set to zero, while interest rate policy and financial regulation bounds are as in the optimal CAP/LEV experiments. ⁷The financial sector's balance sheet size, i.e., $Z + D = (1 - \pi_m)(z + d)$, in the optimal CAP experiment is, on average, 2.435 and is normalized to 100.

Table 4: RATES OF RETURN, RISK TAKING AND WELFARE

EXPERIMENT ¹	$\frac{1}{p}$ (in %)	$R^d - \frac{1}{p}$	Risk taking ² (in %)	Welfare ²
1. Benchmark	2.21	1.78	1.73	-0.0162
2. Optimal CAP: $\left(\frac{1}{p}, \eta^{CAP}, \tau\right)$	2.40	1.60	0.03	0.0000
<i>a.</i> Lower η^{CAP} to 1 percent	2.21	1.79	1.78	-0.0175
<i>b.</i> Raise η^{CAP} to 25 percent	2.65	1.34	-3.37	-0.0339
<i>c.</i> Lower τ to zero	2.22	1.78	1.66	-0.0147
3. Optimal LEV: $\left(\frac{1}{p}, \eta^{LEV}, \tau\right)$	4.00	0.00	0.03	0.0000
<i>a.</i> Lower η^{LEV} to 1 percent	3.57	0.42	59.11	-0.1970
<i>b.</i> Raise η^{LEV} to 20 percent	4.16	-0.16	-22.05	-0.0429
<i>c.</i> Lower τ to zero	3.62	0.37	52.60	-0.1609

¹See footnotes to Table 3 for a description of the experiments. We average rates of return from simulations of 5,000 periods, and then annualize. The return on deposits is 4 percent in all experiments. ²The risk taking and welfare measures are averages over 5,000 simulations of 1,000 periods each.

Figure 1: TIMING OF MODEL EVENTS

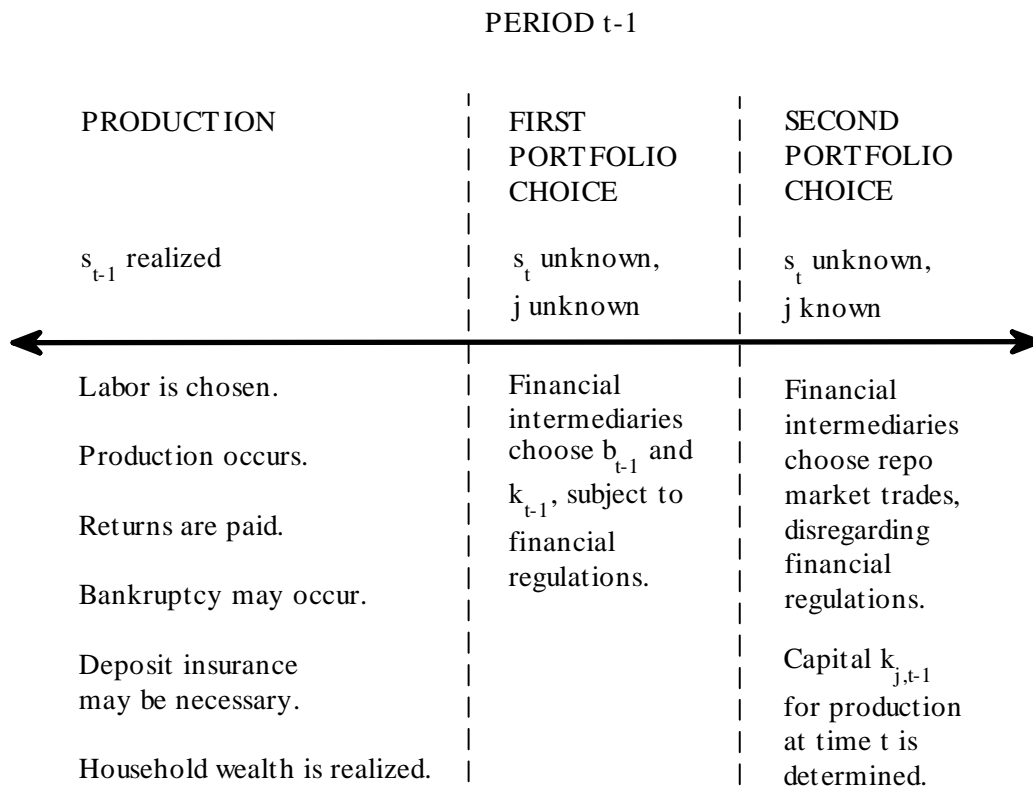


Figure 2: SOCIAL OPTIMUM CAN BE IMPLEMENTED WITH $\left(\frac{1}{p}, \eta^{CAP}, \tau\right)$ OR $\left(\frac{1}{p}, \eta^{LEV}, \tau\right)$

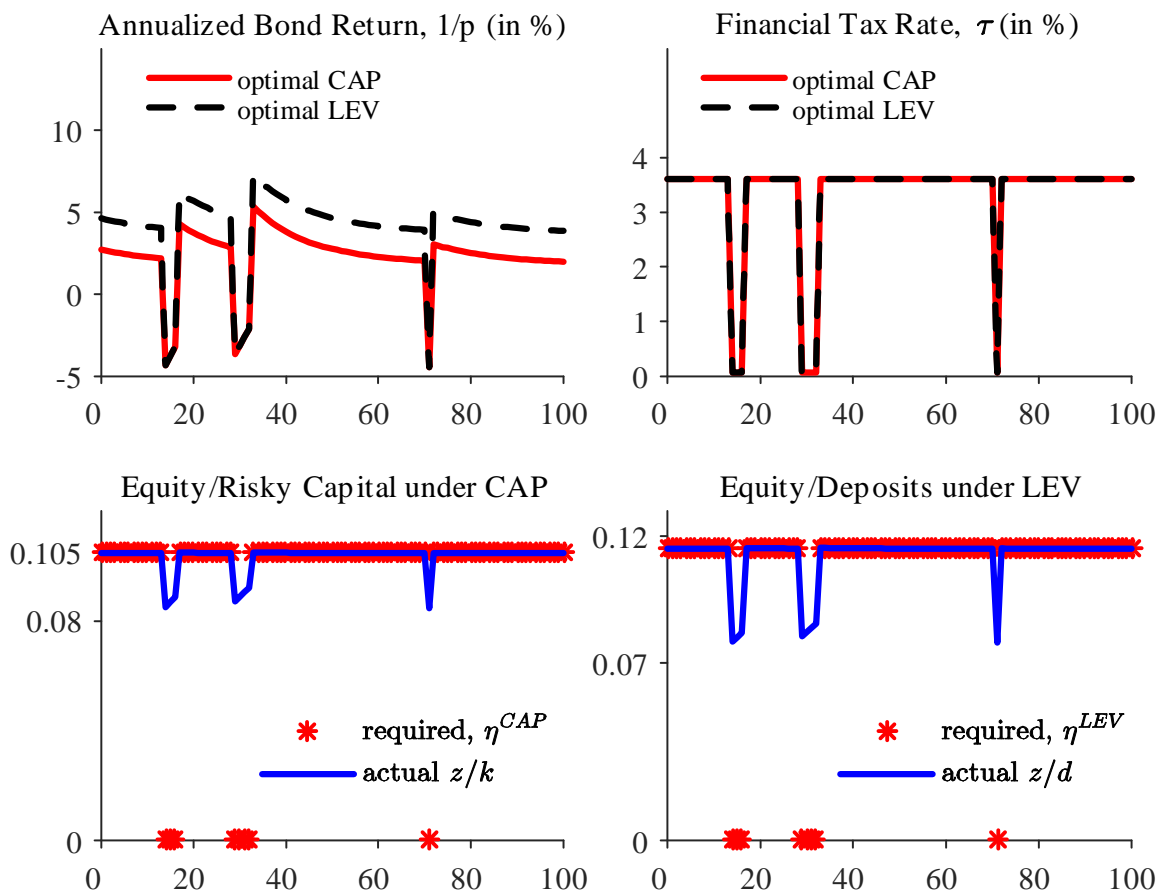


Figure 3: OPTIMAL CAP AND OPTIMAL LEV ECONOMIES: BALANCE SHEET COMPOSITION AND ASSET RETURNS

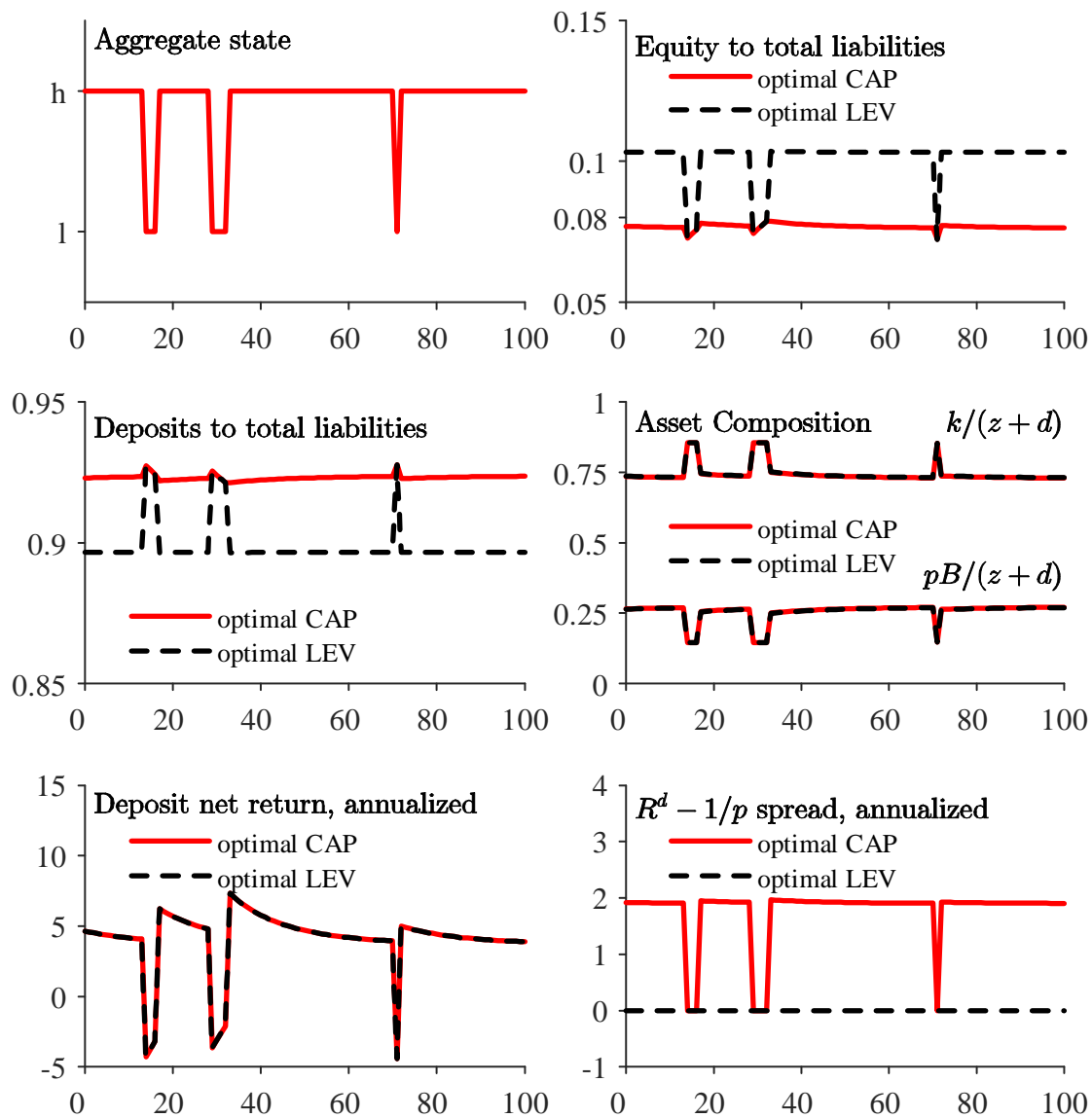


Figure 4: WELFARE AND RISK TAKING RELATIVE TO THE SOCIAL PLANNER

